Research Article

Study on the Characteristics of Electromagnetic Noise of Axial Flux Permanent Magnet Synchronous Motor

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The normal electromagnetic force distribution in stator system of axial flux permanent magnet synchronous motor (PMSM) has been thoroughly analyzed in this paper. The main composition of force wave causing vibration and noise has been proposed, and at the same time a calculation method of stator natural frequency of axial flux PMSM has been raised. Through this method electromagnetic force wave, natural frequency, vibration response, and electromagnetic noise of a 15kW axial flux PMSM with 22 poles and 24 slots have been calculated; calculations and measured values are consistent by comparison. The noise sources of axial flux PMSM have been found in this paper, which provides the theoretical support for the suppression of electromagnetic noise of axial flux PMSM.

1. Introduction

Currently, noise, water pollution, and exhaust gas have been the three public hazards of environmental pollution. With the implementation of ISO14001 standard, the motor noise level has been listed as an important indicator of measuring its quality. Therefore, low noise motor will surely become one of the key products to in the 21st century. Internationally, for the motor, the merits and defects of noise control have become a domain factor of market competition for electronic motor, which has been widely recognized by this industry. The level of controlling motor noise has attracted more and more attention of manufacturers and users. And the laws and regulations connected with the working environment noise are becoming more rigid.

Various reasons cause the motor vibration, which are mainly divided into electromagnetic noise, mechanical noise, and aerodynamic noise. A research on how to apply effective fault diagnosis method to make noise fault diagnosis is very significant [1–8]. And the first problem to be solved is how to effectively calculate the vibration and noise of the motor. Compared with the electrical excitation motors, permanent magnet motors, especially rare earth permanent magnet motors, have simple structure, reliable operation, small volume, light weight, low loss, high efficiency, and diverse shapes and sizes as well as other remarkable advantages [5]. PMSM with multiphase, multipole, and few slots (especially the ratio of poles to slots was 1 to 1) has been applied more and more widely at present. However, compared with the traditional motor, the number and amplitude of air gap harmonics magnetic field, the intensity and frequency of electromagnetic noise, and the adapted suppression methods of this kind of PMSM have distinctive difference.

Although the research about the electromagnetic vibration and noise of motors has made great achievements [6–25], there are still no mature methods to analyze and calculate the modal and natural frequency of axial flux PMSM. Thus this paper will explore the electromagnetic noise of PMSM with multipole and few slots.

2. The Generation Mechanism of Electromagnetic Noise

The normal electromagnetic force, which consists of different frequencies and different distribution rotation force waves
caused by the mutual action of stator and rotor and acting on the inner surface of stator core, is the main source of motors vibration and electromagnetic noise.

According to Maxwell law, the instantaneous value of normal electromagnetic force per unit area can be expressed as

\[
p_r (\theta, t) = \frac{b^2 (\theta, t)}{2 \mu_0},
\]

where \(\mu_0\) is the permeability of vacuum and \(b(\theta, t)\) is the air gap flux density, which was superposed by stator flux and rotor flux, and can be expressed as

\[
b (\theta, t) = b_r (\theta, t) + b_p (\theta, t)
= \sum_y B_y \cos \left( \nu \theta - \omega_1 t - \phi_{yr} \right)
+ \sum_\mu B_\mu \cos \left( \mu \theta - \omega_r t - \phi_{\mu r} \right),
\]

where \(b_r(\theta, t), b_p(\theta, t)\), respectively, represent the instantaneous value of flux density produced at stator side and rotor side which changed with position angle and time. Then substitute (2) into (1), the following equation can be obtained:

\[
p_r (\theta, t)
= \frac{1}{2 \mu_0} \left\{ \sum_\nu B^2_\nu \cos^2 \left( \nu \theta - \omega_1 t - \phi_{yr} \right)
+ \sum_\mu B^2_\mu \cos \left( \mu \theta - \omega_r t - \phi_{\mu r} \right)
+ 2 \sum_{\nu, r} B_\nu B_r \cos \left( \nu_\nu \theta - \omega_1 t - \phi_{\nu r} \right)
\times \cos \left( \nu_2 \theta - \omega_1 t - \phi_{\nu r} \right)
+ 2 \sum_{\nu, \mu, r} B_\nu B_\mu \cos \left( \mu_\mu \theta - \omega_r t - \phi_{\mu r} \right)
\times \cos \left( \nu_2 \theta - \omega_r t - \phi_{\nu r} \right)
+ 2 \sum_{\mu, \nu, r} B_\nu B_\mu \cos \left( \mu_\mu \theta - \omega_r t - \phi_{\mu r} \right)
\times \cos \left( \nu_2 \theta - \omega_r t - \phi_{\nu r} \right) \right\}.
\]

According to (3), the normal electromagnetic force acting on the stator tooth consists of five parts. And the force waves with large amplitude and low order are the primary sources. To PMSM, the electromagnetic force waves, caused by the interaction between rotor and stator harmonic magnetic flux density (the fourth item) and the interaction of various harmonic magnetic flux density produced by permanent magnet (the fifth item), are the major sources of electromagnetic noise.

Under plane radiation, the power of electromagnetic noise caused by electromagnetism acting on stator teeth can be expressed as

\[
W = 2 \rho c^2 f_r^2 Y^2 S_0,
\]

where \(\rho\) is the medium density of sound, \(c\) is the velocity of sound in medium density, \(f_r\) is the frequency of electromagnetic force wave, and \(S_0\) is the vibrating area in vertical direction of the sound wave propagation. \(Y\) is the displacement of vibration under stator electromagnetic force and \(Y = P'/K - \omega_0^2 M\) when damping neglected. \(P'\) is the amplitude of electromagnetic force wave acting on stator teeth. \(K\) is the stiffness of stator system. \(M\) is the mass of fixed system. \(\omega_0\) is the angular frequency of electromagnetic force wave.

### 3. The Analysis of Electromagnetic Force Wave of Axial Flux PMSM

The rotating force wave per unit area, causing the electromagnetic noise, can be expressed as

\[
p_r (\theta, t) = \sum_r P_r \cos \left( \omega_r t - r \theta + \phi_{nr} \right),
\]

where \(P_r, r (r = 1, 2, 3, \ldots)\) represent the amplitude and the order of electromagnetic force wave.

In a moment of time, the distribution of normal electromagnetic force from zero to third harmonic of axial flux PMSM is shown in Figure 1, where solid dots stand for outward and crossing lines stand for inward. Different sizes of solid dots and crossing lines signify the size and direction of electromagnetic force.

After further clarification of fourth and fifth formulas in formula (3), the main values of electromagnetic force in the realm of amplitude, order, and frequency can be obtained.

\[
p_r (\theta, t)
= \frac{1}{2 \mu_0} \left\{ 2 \sum_{\nu, \mu, r} B_\nu B_\mu \cos \left( \nu \theta - \omega_1 t - \phi_{\nu r} \right)
\times \cos \left( \mu \theta - \omega_r t - \phi_{\mu r} \right)
+ 2 \sum_{\nu, r} B_\nu B_r \cos \left( \nu \theta - \omega_1 t - \phi_{\nu r} \right)
\times \cos \left( \nu \theta - \omega_1 t - \phi_{\nu r} \right)
+ 2 \sum_{\mu, r} B_\mu B_r \cos \left( \mu \theta - \omega_r t - \phi_{\mu r} \right)
\times \cos \left( \nu \theta - \omega_1 t - \phi_{\nu r} \right) \right\}.
\]
Abstract and Applied Analysis

Remark: $k_1, k_2, k_3, k_4$ are defined as 0, 1, 2, 3, ..., respectively. $f_1$ is fundamental frequency; $\nu_p$ is harmonic order produced by stator winding.

Table 1: Main normal electromagnetic force.

<table>
<thead>
<tr>
<th>Harmonic source</th>
<th>Amplitude</th>
<th>Frequency Item</th>
<th>Order</th>
</tr>
</thead>
<tbody>
<tr>
<td>The interaction between rotor and stator harmonic</td>
<td>$(1/2\mu_0) B_r B_{\mu_1}$</td>
<td>$2k_1 f_1$</td>
<td>$(2k_1 + 1) p_1 + Z_1 t$ - $\nu_p$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$2(k_1 + 1) f_1$</td>
<td>$(2k_1 + 1) p_1 + Z_1 t$ + $\nu_p$</td>
</tr>
<tr>
<td>The interaction of different rotor harmonic</td>
<td>$(1/2\mu_0) B_r B_{\mu_2}$</td>
<td>$2(k_1 - k_3) f_1$</td>
<td>$2 (k_1 - k_3) p_1 + (k_3 + k_4) Z_1 t$</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$2(k_1 + k_3 + 1) f_1$</td>
<td>$2 (k_1 + k_3 + 1) p_1 + (k_3 + k_4) Z_1 t$</td>
</tr>
</tbody>
</table>

Table 2: Main electromagnetic force with 22 Poles and 24 Slots.

<table>
<thead>
<tr>
<th>$\nu_1$</th>
<th>$\mu_1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>4/2$f_1$</td>
</tr>
<tr>
<td>-7</td>
<td>4/2$f_1$</td>
</tr>
<tr>
<td>11</td>
<td>2/2$f_1$</td>
</tr>
<tr>
<td>(-13)</td>
<td>4/4$f_1$</td>
</tr>
<tr>
<td>17</td>
<td>4/2$f_1$</td>
</tr>
<tr>
<td>29</td>
<td>4/2$f_1$</td>
</tr>
<tr>
<td>-31</td>
<td>2/4$f_1$</td>
</tr>
<tr>
<td>(35)</td>
<td>2/2$f_1$</td>
</tr>
<tr>
<td>[-37]</td>
<td>4/4$f_1$</td>
</tr>
<tr>
<td>41</td>
<td>4/2$f_1$</td>
</tr>
</tbody>
</table>

As for PMSM, the main electromagnetic force was from the interactions of different harmonic waves of rotor in which the electromagnetic force generated from the interactions between fundamental harmonic magnetic flux density and first-order tooth harmonic magnetic density of permanent magnet was the most important. The frequency of the electromagnetic force was 2 multiple of fundamental frequency. The order of the electromagnetic force $r$ is

$$r = (p_1 + (p_1 - Z_1)) t = (2p_1 - Z_1) t.$$  \hfill (7)

A 15 kW axial flux PMSM with 22 poles and 24 slots was taken as an example in this paper. The frequency and order of the electromagnetic force were shown in Table 2, where ( ) stands for first slot harmonic, [ ] stands for second slot harmonic, the subscripts out of parentheses represent that the slot harmonic in parentheses was generated by its interactions, and $\nu_1, \mu_1$ were the harmonic order of stator side and rotor. Also, low-order harmonic force wave would be generated from the interactions between $\mu_1$ and $\mu_2$. The harmonic order with bold font also represented $\nu_1$ and $\mu_2$.

As seen from Table 2, firstly, the electromagnetic force wave, which order is 2 and frequency is 2$f_1$, has been generated from the interactions between 11th fundamental harmonic of permanent magnet and first slot harmonic magnetic flux density (−13) of stator and rotor. Secondly, low-order force wave generated from the interactions between 11th fundamental harmonic of stator and first slot harmonic magnetic flux density (−13) of rotor was equally important. Thirdly, another electromagnetic force wave was the second gear force wave (the frequency was 2$f_1$) which was generated from the interactions between 33rd harmonic (the flux density was 3 times of fundamental wave) and 35th step first slot harmonic wave of rotor. The above will be the largest sources of force wave.

The power spectral density of electromagnetic force wave (the step was less than 4) could be derived by using analytic method. The fundamental frequency ($f_1$) of motor was 82.5 Hz. As seen in Figure 2, each frequency of electromagnetic force was an even multiple of fundamental frequency, where the energy of electromagnetic force whose frequency was 2 multiple of fundamental frequency was the biggest, which was consistent with analysis of Table 2.
4. The Analysis of Natural Frequency of Stator System of Axial Flux PMSM

4.1. The Analysis of Natural Frequency. The vibrating direction of axial flux PMSM stator system was axial. Based on the analysis, the vibration characteristics of stator yoke were similar to doughnut-shaped steel plate, so choosing the circular plate as a replacement. The stator structure and the stress direction of stator tooth were shown in Figures 3 and 4.

With reference to calculative method of stator natural frequency for radial flux PMSM, the calculation formula of stator natural frequency of axial flux PMSM was presented as follows:

\[
f_m = \frac{1}{2\pi} \sqrt{\frac{K_m^{(c)} + K_m^{(f)}}{M_m^{(c)} + \Delta M_m^{(f)}}},
\]

where \(K_m^{(c)}\) is the equivalent stiffness of stator core, \(K_m^{(f)}\) is the equivalent stiffness of the cover, \(M_m^{(c)}\) is the equivalent mass of stator core, \(M_m^{(f)}\) is the equivalent mass of the cover, \(\Delta = 1 + (M_t + M_w)/M_m^{(c)}\) is the additional coefficient of core mass, \(M_t, M_w\) is the mass of stator tooth and stator winding, \(\Delta_f = 1 + M_f/K_m^{(f)}\) is the additional coefficient of the cover, and \(M_f\) is the mass of shell.

From (8), we can see that the key to getting stator natural frequency was how to determine the equivalent stiffness of iron core and cover in different vibrational modes.

When computed through the distribution of the quality system and the centralized quality system, the calculation formula of natural frequency of annular plate was presented as follows:

\[
f_m = \frac{a_{ns}^2}{2\pi a^2} \sqrt{\frac{D}{\rho_A}} = \frac{1}{2\pi} \sqrt{\frac{a_{ns}^2 D \pi (a^2 - b^2)}{a^4 \rho_A \pi (a^2 - b^2)}} = \frac{1}{2\pi} \sqrt{\frac{K_m}{M_m}},
\]

(9)

where \(D\) is the bending rigidity of plate and \(E\) is the modulus of elasticity of plate. \(h\) is the thickness of laminated plate and \(\mu\) is Poisson’s ratio. \(a\) is the outer radius of annular plates, \(\rho_A\) is the surface density of circular plate with a radius of \(a\), and \(a_{ns}\) is the frequency constants, determined by boundary conditions, vibrational mode, and the ratio of inside to outside diameter.

According to (9),

\[
f_m = \frac{a_{ns}^2}{2\pi a^2} \sqrt{\frac{D}{\rho_A}} = \frac{1}{2\pi} \sqrt{\frac{a_{ns}^2 D \pi (a^2 - b^2)}{a^4 \rho_A \pi (a^2 - b^2)}} = \frac{1}{2\pi} \sqrt{\frac{K_m}{M_m}},
\]

(10)

where

\[
K_m = \frac{a_{ns}^2 D \pi (a^2 - b^2)}{a^4},
\]

(11)

and

\[
M_m = \rho_A \pi (a^2 - b^2),
\]

(12)

where \(b\) the inside radius of the annular plate.

4.2. The Calculations of Stator System Natural Frequency of a 15 kW Axial Flux PMSM. The natural frequency of a 15 kW axial flux PMSM was calculated in this paper. The structure parameters of stator system were listed in Table 3 and the computational results of equivalent stiffness and natural frequency were listed in Table 4. To verify the effectiveness
of the calculation method presented in this paper, the 15 kW axial flux PMSM was tested by using PULSE system produced by Denmark B&K company. Figure 5 was stator system for 15 kW motor. Figures 6, 7, and 8 were, respectively, curves of excitation, response, and transfer functions. According to Figure 8, the natural frequency of stator system can be obtained, and test results were listed in Table 4.

The natural frequency of stator system must be away from the electromagnetic force wave; otherwise the motor will cause resonance, resulting in serious consequences.

Table 3: Parameters of stator system of 15 kW motor.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Outer diameter of stator</td>
<td>250 mm</td>
</tr>
<tr>
<td>Inner diameter of stator</td>
<td>144 mm</td>
</tr>
<tr>
<td>Height of iron core yoke</td>
<td>12.7 mm</td>
</tr>
<tr>
<td>Weight of stator tooth</td>
<td>2.4 kg</td>
</tr>
<tr>
<td>Weight of iron core yoke</td>
<td>2.9 kg</td>
</tr>
<tr>
<td>Weight of stator winding</td>
<td>3.4 kg</td>
</tr>
</tbody>
</table>

5. The Analysis of Electromagnetic Noise of Axial Flux PMSM

5.1. The Dynamic Response of Motor. The vibration of motor caused by normal electromagnetic force acting on stator system is the main source of electromagnetic noise and an analytic relationship exists between the vibration and noise. Therefore it is very important to calculate the vibration of motor. When the motor was at work, vibration at every point was caused all by different electromagnetic forces, which synthesized by vibration waveform of different amplitudes and different frequencies. When a lumped parameter mechanical system suffered a harmonic force with \( \omega \), frequency and \( P_{rs} \) amplitude, the vibration velocity of the system can be expressed as follows:

\[
\dot{Y} = \frac{\omega_P_{rs}}{(K^{(c)}_r + K^{(f)}_r) - \omega^2 \left( \Delta \omega M^{(c)}_m + \Delta \omega M^{(f)}_m \right)},
\]

where \( K^{(c)}_r \), \( K^{(f)}_r \) is equivalent stiffness of stator core and shields with the same number between number of pitch diameter and force wave.

The spectrum curve of vibrator acceleration of motor cover was obtained through experiment, which is shown in Figure 9. We can obtain the amplitude of vibration acceleration in maximal frequency from curve. Calculation and...
measured value of vibration acceleration of motor shield were listed in Table 5.

The most important frequency component of the vibration acceleration level is 165 Hz and 330 Hz. From Table 5, the calculate errors $-5.2\%$ and $-0.47\%$ indicate that the calculation results are consistent with the actual value.

5.2. The Electromagnetic Noise. Four steps must be completed before obtaining electromagnetic noise: calculating magnetic field and its harmonic, calculating normal electromagnetic force, calculating natural frequency and vibratory response of stator system, and calculating noise power level. On the basis of the previous three steps, you can successfully get the electromagnetic noise of the motor. Under nonloaded operation, the electromagnetic noise of axial flux PMSM was calculated by author edited programming, and at the same time the electromagnetic noise of the motor was measured in an anechoic chamber which is shown in Figures 10 and 11. And the test value and calculated value were listed in Table 6.

The calculation results of acoustic noise in Table 6 have been modified, and the correction factor is 1.082. The noise of 165 Hz is the most significant from the measured spectrum of acoustic noise, and theoretical calculations have the same conclusion. So rationality about analysis and calculation methods of axial flux PMSM electromagnetic noise mentioned by this paper has been proved.

6. Conclusion

The methods of analyses and calculation for electromagnetic vibration and noise have been researched in this paper. Using a 15 kW axial flux PMSM with 22 poles and 24 slots as an example, a verification calculation has been completed. The conclusions are illustrated.

(1) The direction of electromagnetic vibration: the direction of electromagnetic vibration was axial; thus typical estimation method for calculating electromagnetic vibration is not suitable.
Table 5: Calculated and experimental values of accelerations level of 15 kW motor.

<table>
<thead>
<tr>
<th>Item</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frequency/Hz</td>
<td>165</td>
</tr>
<tr>
<td>Calculation/dB</td>
<td>94.5</td>
</tr>
<tr>
<td>Measured value/dB</td>
<td>99.7</td>
</tr>
<tr>
<td>Error/%</td>
<td>−5.2</td>
</tr>
</tbody>
</table>

Table 6: Comparison between calculated and measured values of Sound power lever.

<table>
<thead>
<tr>
<th>Frequency/Hz</th>
<th>Calculation after correction/dB (A)</th>
<th>Measured value/dB (A)</th>
<th>Error/%</th>
</tr>
</thead>
<tbody>
<tr>
<td>165</td>
<td>72.60</td>
<td>72.6</td>
<td>0</td>
</tr>
<tr>
<td>330</td>
<td>59.73</td>
<td>59.1</td>
<td>1.06</td>
</tr>
<tr>
<td>660</td>
<td>48.15</td>
<td>48.5</td>
<td>−0.7</td>
</tr>
<tr>
<td>Combining</td>
<td>72.6</td>
<td>72.6</td>
<td>0</td>
</tr>
</tbody>
</table>

(2) The stator system structure of axial flux PMSM: the stator system of axial flux PMSM can be equivalent to annular steel plate and vibration mode was indicated by the number of pitch diameter and pitch, where the stator core thickness replaced with annular plate of stator yoke to calculate the height, teeth of the stator, and winding as additional quality were included in the stator core; shell as additional quality was included in the shield.

(3) The frequency of electromagnetic noise and vibration: the frequencies of electromagnetic noise and vibration were even multiple of fundamental wave. The frequency of vibration with highest energy was 2 times of fundamental frequency, which was caused by the normal electromagnetic force with frequency of double fundamental frequency. The main components of the electromagnetic force are listed below.

(a) One of the main components of the electromagnetic force: the low order force was caused by the interaction between fundamental flux density of permanent magnet and first-order slot harmonic magnetic density of rotor and stator.

(b) Another one of the main components of the electromagnetic force: the low order force was caused by the interaction between fundamental flux density of stator and first-order tooth harmonic magnetic density of rotor.

(c) The third main components of the electromagnetic force: the low order force was caused by the interaction between 3 times of the fundamental flux density of rotor and first-order slot harmonic magnetic density of rotor and stator.

(d) The forth main components of the electromagnetic force: the electromagnetic vibration and noise sources of axial flux PMSM have been presented in this paper, which provides the theoretical support for the suppression of electromagnetic noise of axial flux PMSM.

Conflict of Interests

The authors declare that there is no conflict of interests regarding the publication of this paper.

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