DESIGN OPTIMIZATION OF VERTICAL PIPE HANDLING SYSTEM

BY

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CONFIDENTIAL

This Master’s Thesis is carried out as a part of the education at the University of Agder and is therefore approved as a part of this education. However, this does not imply that the University answers for the methods that are used or the conclusions that are drawn.

DEPARTMENT OF ENGINEERING

FACULTY OF TECHNOLOGY AND SCIENCE
Abstract

Due to the demand for high performance and reliability of the offshore systems from the industry the concern about finding the optimal components in a system is increasing. What is called optimal could vary, but keywords that are repeated include, performance, reliability, price and maintenance. To be able to predict the consequences of parameter changes and to a greater extent be able to improve the system in the most cost-effective way, it is a key factor to have robust and accurate simulation models.

This project is based on the vertical pipe handler from Aker Solutions MH. A simulation model for this system is created in Matlab Simulink. The simulation model components are simulated and compared to data specification sheets to obtain correct properties. The motion control valve VAA-B-SICN-ST-250 is also lab-tested to verify and adjust the simulation model. The test was conducted to verify crack pressure settings, define spring stiffness, and obtain a realistic spool response.

The study explores the possibility of implementing the model in an optimization routine. The model used in optimization is simplified to only contain one of the drive lines of the bridge crane (the bridge travel). The simplified model contains a servo valve, over center valve, motors, and inertias and friction models describing the physical system. The model is used together with the so-called Complex optimization algorithm. The optimization examines the effect of changes in the controller parameter, valve frequency, load, and motion control valve parameters such as spring stiffness and pilot ratio. The results indicate that the optimal controller parameters are highly dependent on the load case. The investigation of the controller also showed that adding a velocity feedback gain to the existing controller (velocity forward gain and a position feedback PI-regulator) will improve accuracy with about 70%. The investigation of the directional servo valve response discovered that an improvement from 8.2Hz to 12Hz will improve the toolpoint position accuracy with over 20%.
Preface

I would like to express special thanks to the supervisor, Michael R. Hansen. In addition, I would like to thank Morten Bak for the help I have received with the execution of the experimental tests, and Anne Muller for guidance on the design and structure of the report.
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Chapter 1

Introduction

1.1 Motivation

The current vertical pipe handling system (VPHS) of Aker Solutions, is basically a combination of two machines (bridge crane and lower guiding arm (fig 1.1). They must move in a coordinated manner in order to move pipe stands to or from the drill center. There is an increasing demand for improved performance with the dominant criteria being reliability. Other important criteria are: price, speed, accuracy, ease of maintenance and efficiency.
Figure 1.1: Bridge crane and lower guiding arm [9]
CHAPTER 1. INTRODUCTION

1.2 Goal

The project has mainly three goals. Firstly, precise and accurate models of the components in the bridge crane and lower guiding arm should be created. To ensure the accuracy of the models experimental test work will be introduced. The test results will verify or lead to modifications on the simulation model such that the model will maintain a sufficient accuracy. In this context a sufficiently accurate model is one that can be used for design optimization. This test will focus on the motion control valves. The motion control valves are essential in the hydraulic sub-systems, and is located between the hydraulic actuator and the directional valve (fig 1.2).

Secondly, the obtained simulation components will be assembled to create a model of the VPHS. Thirdly, an optimization routine should be performed to discover how the system parameters could be changed to improve the system performance. This will demand a simulation model where the complexity have been reduced with a view to reduce simulation time without compromising accuracy.
1.3 Thesis outline

The thesis starts with the development of the simulation model components. This involves assumptions and modeling methods that are used to simulate the system components. These components are combined to yield the model of the lower guiding arm (LGA) and the bridge crane (BC). Next the experimental work is presented with the test procedures to verify and calibrate the simulation model of the motion control valve (MCV). The results are compared to the simulation model and evaluated. In the end of the thesis the Complex optimization algorithm is introduced, and is applied to optimize part of the bridge crane.

1.4 Project overview

- Simulation models of each component in the VPHS are created.
- A simulation model of the VPHS is developed. The model is made to simulate the dynamic behavior in the time domain.
- An experimental test is performed to explore and verify the parameters in the MCV used on the bridge crane.
- An optimization procedure and implementation is described.
Chapter 2

Simulation Model

2.1 Introduction

This chapter deals with the structure and composition of the two models, "bridge crane" and "lower guiding arm". To get a practical and fast running model it is useful to do some simplifications. It is important that the approximation is done properly to avoid large deviations from the exact physical result. The following 3 assumptions are made. First of all a stiff mechanical structure is assumed. This assumption says that the guide mast which connects the gripper head to the trolley is infinitely stiff. This is of course not completely true, but because the complex structure of the guide mast and the fact that it actually are quite stiff. It is assumed that this will not affect the overall model in any large scale. Secondly the ring line pressure supply is assumed constant and independent of flow consumption. Hence, it is assumed that the hydraulic power unit can deliver the required amount of flow without loosing the pressure. The ring line pressure is assumed to be 207bar. Finally the third assumption is the friction models. In motors, bearings, gears, sliders and so on the friction is represented as a simple coulomb or viscous friction force. No hysteresis or stiction models are used. It is assumed that this will not give any major deviations compared to the physical system, since the crane does not have any oscillating movement patterns and high velocities. If this
where the case a more advanced model should be used because the effect of the friction force would be larger.

The following sections in this chapter will deal with the modeling of each component in the vertical pipe handler. All models are created with Matlab simulink in time domain. The oil used in the hydraulic circuits has a fluid density of $850 \text{kg/m}^3$, a kinematic viscosity $1.8 \cdot 10^{-5} \text{m}^2/\text{s}$, and a bulk modulus of $8 \cdot 10^8 \text{Pa}$ (table 2.1)

<table>
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<td>Fluid density</td>
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</tr>
<tr>
<td>Kinematic viscosity</td>
<td>$1.8 \cdot 10^{-5} \text{m}^2/\text{s}$</td>
</tr>
<tr>
<td>Bulk modulus</td>
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Table 2.1: Oil specifications in simulation models.
CHAPTER 2. SIMULATION MODEL

2.2 Proportional Directional Valve, WRLE

2.2.1 Use and functionality

All three directions of the gripper head (trolley travel, bridge travel and slewing) on the bridge crane are controlled by the same type of directional valve, 4WRLE 16 WZ180SJ-3X/G24ETK0/A1M. This servo valve has a positive overlap and on-board electronics (fig 2.1).

![Servo solenoid valve 4WRLE-10...35](image)

Figure 2.1: Servo solenoid valve 4WRLE-10...35 [3]
2.2.2 Model

The valve is modeled as four variable area orifices in simulink. These four orifices are determined through the input signal and the given valve properties (appendix E and G). To obtain the correct dynamics for this valve, a second order transfer function is added to the input signal. This transfer function would then express the response of the spool as if it was a mass connected to a damper and a spring.

![Figure 2.2: Block diagram of the proportional valve](image)

The response block (fig 2.2) contains the second order valve response, described in the technical data sheet (see appendix E). To obtain this second order response as a transfer function with correct parameters, the response plot from the data sheet was converted manually to points. Then these points were used together with a general second order transfer function (eq; 2.1) inside an optimization algorithm (the complex method).

The 2nd order transfer function representing the spool response is,

$$TF_{2,nd} = \frac{\omega_n^2}{s + 2 \cdot \zeta \cdot \omega_n \cdot s + \omega_n^2}$$  \hspace{1cm} (2.1)

where $\zeta$ is the damping ratio and $\omega_n$ is the natural frequency. When using an optimization algorithm it is needed to have a cost function. This cost function represents the error of the results and the optimization algorithm tries to minimize it. In this case the cost function was set to be the sum of the squared error. Eleven points were read out from the data sheet curve, and the defined cost function were
dependent on deviation between each point and estimated step response. Thus,

\[ E = \sum_{i}^{n} E_i^2 \]  

(2.2)

where \( E_i \) is the deviation between the reading and simulated value at point \( i \), and \( n \) is the total amount of points, in this case 11.

The optimization gave a response that corresponds well to the response given in the data sheet[3]. In fig 2.3 the red dots indicate the values of the response curve in the data sheet, while the black line indicates the final simulated design. The blue lines indicates tested responses before the algorithm settles on the black line.

![Figure 2.3: Optimization of transfer function](image)

The result gave a response with a frequency about 52.6 rad/sec and a damping ratio of 0.90. This gave an error of \( E = 8.1 \cdot 10^{-4} \) due to the cost function eq.2.2.
CHAPTER 2. SIMULATION MODEL

Next, the maximum discharge areas and deadband was determined. These properties were obtained by looking at the flow charts in the data sheet (see "flow in mid position" and "technical spec" in appendix E). The data sheet describes the flow around the flow characteristics at a pressure drop of 5bar. From the technical specifications and graphics, the nominal flow at a pressure drop of 5bar is 180l/min if the valve is fully opened. From this fact and the orifice equation, the maximum discharge area was determined to be $125\, mm^2$. To determine the discharge area in the deadband area the data sheet gave the following plot shown in fig 2.4.

![Figure 2.4: Flow in control valve in mid position. Pressure drop at 5bar.](image)

At 5Bar pressure drop, the nominal flow between A-T and B-T is 3l/min in the mid position. With this flow and pressure specification the discharge area for these ports deadband zone (±2%) was determined. The area was calculated to be $2.1\, mm^2$.

$$Q = A_d C_D \sqrt{\frac{2}{\rho} \Delta p} \quad C_D = 0.7 \quad \rho = 850\, kg/m^3 \quad \Delta p = 5\, bar$$

Hence, the following areas were found:

$$Q = 180l/min \rightarrow A_{d,max} = 124.9\, mm^2 \quad Q = 3l/min \rightarrow A_{d,min} = 2.1\, mm^2$$
CHAPTER 2. SIMULATION MODEL

Below the deadband zone it was assumed that the area was ramped to zero over the next 20% (fig 2.5). This was assumed since it was not possible to extract this information from the data sheet. Because of that assumption and the previously determined areas, the following properties for the simulated valve was obtained (fig 2.5).

![Figure 2.5: Valve port properties](image)

The figure show the flow characteristics around the deadband. The deadband corresponds to the deadband given in fig 2.4 and the deadband flow to tank (A-T and B-T) is 3l/min.
2.3 Proportional Directional Valve, PVG 32

2.3.1 Use and functionality

The lower guiding arm uses the proportional valve PVG 32, which is an electrical actuated valve. This valve is also pressure-compensated to keep a pressure drop of 7 bar over the valve. The use of constant pressure drop give a flow rate proportional to the control signal, and is due to this easier to control.

Figure 2.6: Electrical actuated PVG[2]
2.3.2 LS pressure characteristics

A common problem when closing into the LS pressure, is flow loss (fig 2.7).

![Figure 2.7: Oil flow characteristic at LS pressure limiting](image)

This flow loss is actually caused by the LS pressure setting and a reduced pressure drop over the PVG. As the pressure approach the LS pressure the relief valve(2) will slowly open up about 60bars below crack pressure. This will create a small flow through the relief valve(2) and the orifice(1). This flow will create a pressure loss and the measured pressure sent to the pressure compensator will then be lower than the actual pressure at the output port(3). The controller will therefore "assume" that the pressure drop over the control valve is correct while it actually is below. As the pressure is increased the flow and pressure drop over the spool is reduced. When the pressure reaches the LS pressure the relief valve has fully opened and the flow through the PVG has reached zero.

![Figure 2.8: PVG hydraulic sheet](image)


2.3.3 Simulation model

The PVG has the same functionality as the 4/3 servo valve (2.2), only this valve has different deadband and opening areas. The deadband was set to 0.8mm due to the specifications for a linear PVG. The maximum discharge area and the discharge area in neutral was determined due to the flow curves for a $100l/min$ spool (curve E in fig 2.9a and 2.9b) and the orifice equation,

$$Q = A_d C_D \sqrt{\frac{2}{\rho} \Delta p}$$

$$C_D = 0.7 \quad \rho = 850 kg/m^3$$

This give,

$$Q = 100l/min, \quad \Delta p = 7bar \quad \rightarrow \quad A_{d,\text{max}} = 58.7mm^2$$

$$Q = 60l/min, \quad \Delta p = 205bar \quad \rightarrow \quad A_{d,\text{min}} = 6.5mm^2$$

Figure 2.9: PVG characteristics [2]

The spool response was set to a second order transfer with a frequency of 30rad/sec and damping ratio of 0.8. These values is based on earlier test results [5] by Morten Kollerup Bak.
The parameters needed to simulate the valve is now obtained. The simulation model of the valve has three main parts (fig 2.10). Firstly the 4/3 valve functionality with the right spool travel, deadband, and discharge areas (table 2.2). Secondly is the response block which contains the second order transfer function. And the third main part is the pressure compensator. In this case the compensator is simulated as a function coupled to a ideal pressure source. The function is dependent on the output pressure of the PVG and controls the ideal source to keep a pressure 7bar above the output. When the output pressure passes the LS-pressure minus 60bar the function make the pressure drop linearly drop to zero as the output pressure goes towards the LS-pressure, corresponding to fig 2.7. To avoid singularity the function is coupled to a response block and to avoid that this would affect the model the response frequency was set very high (\( \omega = 1000 \text{rad/sec} \)).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Max spool travel</td>
<td>±7mm</td>
</tr>
<tr>
<td>Deadband</td>
<td>±0.8mm</td>
</tr>
<tr>
<td>Neutral discharge area to tank</td>
<td>6.5mm²</td>
</tr>
<tr>
<td>Maximum discharge area</td>
<td>58.7mm²</td>
</tr>
<tr>
<td>Response frequency</td>
<td>30 rad/sec</td>
</tr>
<tr>
<td>Response damping ratio</td>
<td>0.8</td>
</tr>
</tbody>
</table>

Table 2.2: PVG settings in simulated model
The LS pressure settings on the lga is given from the drawing sheets. The LS pressure used is shown in table 2.3.

<table>
<thead>
<tr>
<th>Output</th>
<th>Trolley Travel</th>
<th>Jib Tilt</th>
<th>Telescope</th>
<th>Slewing</th>
</tr>
</thead>
<tbody>
<tr>
<td>Port</td>
<td>A</td>
<td>B</td>
<td>A</td>
<td>B</td>
</tr>
<tr>
<td>LS [bar]</td>
<td>207</td>
<td>207</td>
<td>190</td>
<td>190</td>
</tr>
<tr>
<td>Q [l/min]</td>
<td>78</td>
<td>78</td>
<td>80</td>
<td>49</td>
</tr>
<tr>
<td>v [mm/s]</td>
<td>600</td>
<td>600</td>
<td>110</td>
<td>110</td>
</tr>
<tr>
<td>Descr.</td>
<td>FWD</td>
<td>AFT</td>
<td>EXTEND</td>
<td>RETRACT</td>
</tr>
</tbody>
</table>

Table 2.3: Data from drawing sheet, see appendix C

Figure 2.10: Simulink model of PVG 32
CHAPTER 2. SIMULATION MODEL

2.4 Motion control valve

2.4.1 General use and functioning

Motion control valves is used over every motor in the hydraulic system. The valve is primarily used for increased stability during load lowering (negative load). The valve also equalize the difference in acceleration and deceleration for the same spool position \((u\) and \(-u\)), and therefore make the system easier to control. The check valves between \(p_t\) and \(p_{v1}, p_{v2}\) (fig 2.14) will prevent cavities in the oil. That the mcv equalizes the difference in acceleration and deceleration, and prevent cavities are shown in the following example/test. The test contains a constant pressure source, \(p_p = 260\text{bar}\) (fig 2.13). The flow from the pressure source goes through an orifice with a variable discharge area. The area is ramped up and down as shown in fig 2.11, giving an increase and decrease in flow through the system. The rest of the system consists of a motor subjected to a constant force in opposite direction of the velocity (could for instance illustrate a coulomb friction force), and an orifice to tank. The system is simulated with and without over center valve.

![Figure 2.11: Test setup](image)

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The results highlighted the functionality of the motion control valve. It gave a stable and more even deceleration compared to the test with no implemented motion control valve (fig 2.11). In the system with no mcv, the pressure falls below 0bar. This is a sign of cavitation, which can cause instability due to low oil stiffness. On the system which has a motion control valve the cavitation is gone and the pressure settles at 0bar (fig 2.13).

![Figure 2.12: Velocity with and without mcv](image)

Figure 2.12: Velocity with and without mcv

![Figure 2.13: Pressures on each side of overcenter valve](image)

Figure 2.13: Pressures on each side of overcenter valve
CHAPTER 2. SIMULATION MODEL

The vertical pipe handler crane has many different motion control valves, but for this specific simulation model, those in table 2.4 and 2.5 are needed.

<table>
<thead>
<tr>
<th>Type</th>
<th>Place</th>
<th>Pilot ratio</th>
<th>Crack pressure</th>
</tr>
</thead>
<tbody>
<tr>
<td>VAA-B-SICN-ST-VF250</td>
<td>Bridge travel</td>
<td>2.8</td>
<td>230bar/230bar</td>
</tr>
<tr>
<td>VAA-B-SICN-ST-VF250</td>
<td>Trolley travel</td>
<td>2.8</td>
<td>260bar/260bar</td>
</tr>
<tr>
<td>VAA-B-SICN-ST-VF250</td>
<td>Slewing</td>
<td>2.8</td>
<td>270bar/270bar</td>
</tr>
</tbody>
</table>

Table 2.4: Overcenter valves, Bridge crane, [6]

<table>
<thead>
<tr>
<th>Type</th>
<th>Place</th>
<th>Pilot ratio</th>
<th>Crack pressure</th>
</tr>
</thead>
<tbody>
<tr>
<td>VAA-B-SICN-ST-VF050</td>
<td>Trolley travel</td>
<td>9.1</td>
<td>200bar/200bar</td>
</tr>
<tr>
<td>VAA-B-SICN-ST-VF150</td>
<td>Slewing</td>
<td>3</td>
<td>200bar/200bar</td>
</tr>
<tr>
<td>VBSO-DE-CC</td>
<td>Jib tilt</td>
<td>3.2</td>
<td>100bar/230bar</td>
</tr>
<tr>
<td>VBSO-DE-CC</td>
<td>Telescope</td>
<td>3.2</td>
<td>100bar/140bar</td>
</tr>
</tbody>
</table>

Table 2.5: Overcenter valves, LGA, [6]

The VAA-B-SICN-ST valves has the same functionality principle but with different sizes (VF050, VF150, VF250). Each size has its own flow-pressure characteristics, and therefore need individual adjustment. In the next sections the functionality of the VAA-B-SICN-ST valves and VBSO-DE-CC valves will be explained as well as the modeling and individual adjustments.
2.4.2 Motion Control Valve VAA-B-SICN-ST

Valve information

The valve provides a static and dynamic motion control by regulating the flow and pressure in and out of the hydraulic motor at ports C1 and C2. If the valve is placed close to the motor it will also stop runaway in case of hose failure. The check valves allow free flow into the motor and prevent reverse movement and the pilot assisted relief valves control the movement when pilot pressure is applied. The system of check valves at the end of each relief valve allows cross line relief (after crossing the pressure relief valve, the flow continuous either line one or line two, dependent on where the pressure is the lowest). Through port C3 (brake release port) a shuttle valve directs the highest pressure from V2 and V1 to the spring actuated brake for brake releasing. In this way the brake will always be on as long as maximum system pressure is bellow the needed brake release pressure.[6]

![Figure 2.14: Cross-section and hydraulic chart of motion control valve VAA-B-SICN-ST](image)

Figure 2.14: Cross-section and hydraulic chart of motion control valve VAA-B-SICN-ST [6]
CHAPTER 2. SIMULATION MODEL

The pressure relief valve opening

To calculate the spool position a static equilibrium is assumed. Hence, the valve opening is given by the pressure forces and the spring stiffness.

From fig 2.14 the static equilibrium state of the yellow spool was derived. The cross section in fig 2.14 show the valves between V2 and C2. By looking at the pressure in each chamber the figure 2.15 was drawn. The figure show the two parts of the spool and the pressures working on it. The pressures are pushing on different areas and the areas are shown in cross section A and B (fig 2.15). Since the spool has two parts it is necessary to have an equilibrium equation that depends on whether they are in contact or not. Hence the force \( N \),

\[
\sum F = 0 \rightarrow N_2 A_r = p_1 A_r \alpha - p_t A_r \alpha + (p_{cr2} - k_{p2} \cdot u_2) A_r \quad (2.3)
\]

\[
\sum p = \frac{\sum F}{A_r} = 0 \rightarrow N_2 = p_1 \cdot \alpha - p_t \cdot \alpha + p_{cr2} - k_{p2} \cdot u_2 \quad (2.4)
\]

where the pressures corresponds to the pressures subjected to the left spool piece (fig 2.15) and \( \alpha \) is the pilot ratio. The \( p_{cr2} \) and \( k_{p2} \) is crack pressure and spring stiffness relative to the ring area \( A_r \). While \( N \) i larger than zero the two pieces are in contact and the forces on the left piece will try to open the valve (push the right spool to the right).

![Diagram](https://via.placeholder.com/150)

**Figure 2.15: Pressure loads**

The equilibrium forces on the right spool determines the discharge area for the flow from C2 to V2. An equilibrium equal or less than zero means that the spool
is pushed to the position zero. Dependent on the spring stiffness and the pressures the static position of the spool is determined.

Equilibrium for the pressure relief valve between V2 and C2 is,

While $N_2 < 0$

$$\sum F = p_1(A_1 - A_r) + p_4 \cdot A_r - (p_{cr1} + k_1 \cdot u_2) \cdot A_r - p_t \cdot A_1 \quad (2.5)$$
$$\sum p = p_{eq} = -p_t + p_4 - (p_{cr1} + k_{p1} \cdot u_2) \quad (2.6)$$

Static solution, hence $p_{eq} = 0$ gives:

$$u_2 = \frac{p_4 - p_t - p_{cr1}}{k_{p1}}, \quad 0 \leq u_2 \leq 1 \quad (2.7)$$

While $N_2 > 0$

$$\sum F = p_1 \alpha A_r + (p_{cr2} - k_2 \cdot u_2)A_r - p_2 \alpha A_r + p_t(A_1 - A_r) + p_4A_r - (p_{cr1} + k_1 \cdot u_2)A_1 - p_tA_3$$
$$\sum p = p_{eq} = \frac{\sum F}{A_r} \quad (2.8)$$
$$p_{eq} = p_1 \alpha + p_{cr2} - k_{p2} \cdot u_2 - p_2 \alpha + p_t\frac{A_1}{A_r} - 1 + p_4 - (p_{cr1} + k_{p1} \cdot u_2) - p_t\frac{A_1}{A_r} \quad (2.9)$$
$$p_{eq} = p_1 \alpha + p_{cr2} - k_{p2} \cdot u_2 - p_t(\alpha + 1) + p_4 - p_{cr1} - k_{p1} \cdot u_2 \quad (2.10)$$

Static solution, hence $p_{eq} = 0$ gives:

$$u_2 = \frac{p_1 \cdot \alpha + p_{cr2} - p_t(\alpha + 1) + p_4 - p_{cr1}}{k_{p1} + k_{p2}}, \quad 0 \leq u_2 \leq 1 \quad (2.11)$$

The equation 2.11 give the opening position of the relief valve between port C2 and V2, given by the pressures and the spring stiffness. The static equilibrium for the pressure relief valve between V1 and C1 is identical, except $p_1 \rightarrow p_2$, and $p_4 \rightarrow p_3$. 

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Static equilibrium for the pressure relief valve between V1 and C1,

While \( N_1 < 0 \)

\[
u_1 = \frac{p_3 - p_t - p_{cr1}}{k_{p1}}, \quad 0 \leq u_1 \leq 1
\]

(2.12)

While \( N_1 > 0 \)

\[
u_1 = \frac{p_2 \cdot \alpha + p_{cr2} - p_t (\alpha + 1) + p_3 - p_{cr1}}{k_{p1} + k_{p2}}, \quad 0 \leq u_1 \leq 1
\]

(2.13)

where \( u_1 \) is the position of the spool in line 1 (between C1 and V1), \( p_t \) is the pressure in the end of the relief valves, \( p_{cr} \) and \( k_p \) is the crack pressure and spring stiffness due to the springs.

\( A_r \) : Ring pressure area, which is related crack pressure  
\( p_{cr1} \) : Crack pressure, spring 1, [Pa]  
\( k_{p1} \) : Stiffness spring 1, Pascal per unit displacement of \( u \), [Pa/unit]  
\( p_{cr2} \) : Crack pressure, adjustable, spring 2, [Pa]  
\( k_{p2} \) : Stiffness spring 2, Pascal per unit displacement of \( u \), [Pa/unit]  
\( \alpha \) : Pilot pressure ratio  
\( p_1 \) : Pressure at V1, see fig 2.14, [Pa]  
\( p_2 \) : Pressure at V2, see fig 2.14, [Pa]  
\( p_3 \) : Pressure at C1, see fig 2.14, [Pa]  
\( p_4 \) : Pressure at C2, see fig 2.14, [Pa]  
\( p_t \) : Pressure between relief and check valve, see fig 2.14, [Pa]  
\( u_i \) : Spool position for line 1 or 2 \( (i = 1 \) or \( i = 1) \). Saturates at zero and one

Table 2.6: Variable table
Simulink model

The motion control valve (fig 2.16) is simulated with two orifices with variable discharge area. One for each relief valve and four check valves (all from Simscape library in MATLAB). The variable discharge areas were calculated through the pressure/force equilibrium equations (eq:2.10 and 2.13). When this equilibrium is equal or less than zero, the valve is closed.

Assumed that the discharge area increase linearly with the spool position, the variable discharge area was calculated based on the pressures pressure equilibrium defining \( u \) (eq.2.13) and \( A_{d,max} \), hence,

\[
\begin{align*}
    a_1 &= u_1 \cdot A_{d,max} \\
    a_2 &= u_2 \cdot A_{d,max}
\end{align*}
\]  

(2.14)  
(2.15)

where \( a_1 \) and \( a_2 \) are the discharge areas for pressure relief valve 1 and 2 and corresponds to the \( a_1 \) and \( a_2 \) in fig 2.16, and \( u_1 \) and \( u_2 \) are calculated through equation 2.13 and 2.11. The spring stiffness for the springs on each side of the relief valve determines when the valve is fully open \( (u = 1, \text{ see eq 2.11 and 2.7}) \), and are therefore important parameters. The spring stiffness parameter is not given in the datasheets and will be determined with some valve testing in section 3.4.2.
CHAPTER 2. SIMULATION MODEL

The simulink model structure contains mainly 3 parts (fig 2.17). Firstly the equilibrium equation determine the static position of the spool. Second part is the dynamic response of the spool inserted as a transfer function. The third and last part is the hydraulic model with orifices and check valves.

Figure 2.17: Simulink model structure
Tuning motion control valve parameters

To obtain good model for the overcenter valve it is important to have the right parameter values. Some of these values is obtained through some simulations and comparisons to specifications from the data sheet[6]. These are the parameter values that belong to the check valves and the maximum opening area of the relief valves. The values that cannot be evaluated this way are the crack pressures, the spring stiffness and the spool response. These parameters looked into in chapter 3. The test simulation was executed with a simple model (fig 2.18). The model was built to determine the parameters based on some flow curves taken from the data specification sheet[6]. The data sheet gave flow curves through V1/V2 to C1/C2, and C1/C2 to V1/V2 when the spool was fully opened. With this data the maximum discharge areas for check valves and pressure relief valves could be obtained, as well as some crack pressures and areas for the check valves.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_{m,prv}$</td>
<td>Maximum discharge area in the pressure relief valve</td>
</tr>
<tr>
<td>$p_{cr1}$</td>
<td>Crack pressure, check valve 1</td>
</tr>
<tr>
<td>$A_{m,cv1}$</td>
<td>Maximum passage area, check valve 1</td>
</tr>
<tr>
<td>$p_{max,cv1}$</td>
<td>Maximum opening pressure, check valve 1</td>
</tr>
<tr>
<td>$p_{cr2}$</td>
<td>Crack pressure, check valve 2</td>
</tr>
<tr>
<td>$A_{m,cv2}$</td>
<td>Maximum passage area, check valve 2</td>
</tr>
<tr>
<td>$p_{max,cv2}$</td>
<td>Maximum opening pressure, check valve 2</td>
</tr>
</tbody>
</table>

Table 2.7: The parameters determined through the test
To perform this test, a model was built in Simulink. The connection between V and C only have a check valve, referred to as check valve 1, and the other direction (from C to V) was simulated with an orifice in series with a check valve, referred to as check valve 2 (2.18). The orifice illustrates a fully opened pressure relief valve.

![Figure 2.18: Model for testing of motion control valve parameters](image)

The simulation was executed by connecting an ideal flow source to each test model (fig 2.18). The flow was ramped to 200 l/min. The results were compared to readings from the actual curves in the data sheet.

To determine these parameters (table 2.7) a certain approach was used. This approach is explained below step by step. Each step has a number which refers to the numbers in fig 2.19 (except step 5 which refers to point 3).

1. Determine the maximum discharge area in "check valve 1" by giving the valve a pressure drop of the last given value in the data sheet. Use the same pressure drop and tune in the discharge area to get the correct flow. The flow and area are in this case linearly dependent.

2. Adjust your crack pressure to fit the given reading at flow equal zero.

3. Move the breakpoint by adjusting the maximum opening pressure. Check valve 1 is now fully determined.

4. Set the maximum discharge area in check valve 2 equal the check valve 1. Then determine the maximum discharge area in the pressure relief valve,
by the same procedure as in point 1. Because of the check valve coupled in series the flow and area is no longer linearly dependent.

5. Set the crack pressure to 0.1bar, and start with the fine tuning your plot by changing the maximum opening pressure as in point 3.

![Figure 2.19: Step by step procedure description](image)

The approach led to pressure-flow curves that was comparable with the datasheet curves. The red dots in fig 2.19 corresponds to readings from data sheets and the simulation results are marked with black and blue lines. The parameter optimization approach is performed for the three different sizes used on the bridge crane (VAA-B-SICN-ST-VF-50, -150, and -250). The curves (fig 2.19) show a remarkable similarity with the values read from the data sheet.
Figure 2.20: Simulation results compared with readings for the mcv [1]
CHAPTER 2. SIMULATION MODEL

As a result of this optimization approach these parameters were found (table 2.8), where $A_{m,prv}$ is the maximum discharge area of the pressure relief valve,

<table>
<thead>
<tr>
<th></th>
<th>VAA-B-SICN-ST-VF050</th>
<th>VAA-B-SICN-ST-VF150</th>
<th>VAA-B-SICN-ST-VF250</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_{m,prv}$</td>
<td>15mm$^2$</td>
<td>39mm$^2$</td>
<td>72.1mm$^2$</td>
</tr>
<tr>
<td>$p_{cr1}$</td>
<td>1bar</td>
<td>1bar</td>
<td>0.5bar</td>
</tr>
<tr>
<td>$A_{m,cv1}$</td>
<td>20.5mm$^2$</td>
<td>90.9mm$^2$</td>
<td>151.5mm$^2$</td>
</tr>
<tr>
<td>$p_{max,cv1}$</td>
<td>4.2bar</td>
<td>3bar</td>
<td>2bar</td>
</tr>
<tr>
<td>$p_{cr2}$</td>
<td>0.1bar</td>
<td>0.1bar</td>
<td>0.1bar</td>
</tr>
<tr>
<td>$A_{m,cv2}$</td>
<td>20.5mm$^2$</td>
<td>90.9mm$^2$</td>
<td>151.5mm$^2$</td>
</tr>
<tr>
<td>$p_{max,cv2}$</td>
<td>5bar</td>
<td>1.9bar</td>
<td>2.5bar</td>
</tr>
</tbody>
</table>

Table 2.8: Best parameter results for VAA-B-SICN-ST valves

$p_{cr1}$, $p_{max,cv1}$ and $A_{m,cv1}$ are the crack pressure, pressure at maximum opening and maximum discharge area for check valve 1. The similar names are used for check valve 2.

The simulation model of this mcv is now fully determined except for the spool response and spring stiffness. These parameters are found by physical testing of the valves. A physical test of the VAA-B-SICN-ST-VF-250 is executed in chapter 3.

<table>
<thead>
<tr>
<th></th>
<th>VAA-B-SICN-ST-VF250</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k_p$</td>
<td>495bar/unit*</td>
</tr>
<tr>
<td>$k_p$</td>
<td>400bar/unit*</td>
</tr>
<tr>
<td>$\omega$</td>
<td>12Hz</td>
</tr>
<tr>
<td>$\zeta$</td>
<td>1.0</td>
</tr>
</tbody>
</table>

Table 2.9: Results from experimental test in chapter 3

*The spring stiffness is not determined for each spring, but for the sum of both. Since the two parts of the spool always were connected in the performed test, it was impossible to separate them, hence $k_p = k_{p1} + k_{p2} = 895bar/unit$. The spool response is set as a second order transfer function containing the $\omega$ and $\zeta$ as frequency and damping ratio.
2.4.3 VBSO overcenter valve

Use and functionality

The valve provides control of load by regulating the flow in and out of the actuator through port C1 and C2. This valve module includes two sections, each one composed by a check and a relief valve with balanced piston. The piston has a pilot pressure assisted from the opposite line. The check valves allow free flow into the actuator, and holds against reversed movement. With pilot pressure applied at the line across, the pressure setting of the relief is reduced in proportion to the stated ratio until opening. Relief operates the valve opening independent of back-pressure, but is always subjected to the piloted pressure from V1 or V2. [6]

Figure 2.21: VBSO [6]
CHAPTER 2. SIMULATION MODEL

Determine the pressure relief valve opening

To determine the valve opening, \( u \), the pressure equilibrium was obtained. The pressure equilibrium was determined based on the spool areas and the related pressures.

\[ \sum F = 0 \rightarrow N_2 = \alpha A_r \cdot (p_{v1} - p_{v2}) \]  

where \( \alpha \) is the pilot ratio and \( p_{v1} \) and \( p_{v2} \) are the pressures in port V1 and V2 (fig 2.21). Positive \( N \) will cause contact between mid piston and relief valve 2 (the one between V2 and C2) and a negative N will cause contact between mid piston and relief valve 1.

Figure 2.22: Pressures and forces acting on the spool
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Static equilibrium for the pressure relief valve between V2 and C2 (line 2):

While \( N < 0 \) (no contact)

\[
\sum F = p_{c2}(A_1 - A_r) + p_{c2} \cdot A_r - p_{v2}A_1 - (p_{cr2} + k_{p2} \cdot u_2) \cdot A_r
\]

(2.17)

Divide by the ring area

\[
\frac{\sum F}{A_r} = p_{eq} = -p_{v2} + p_{c2} - p_{cr2} - k_{p2} \cdot u_2
\]

(2.18)

Static equilibrium, \( p_{eq} = 0 \), hence

\[
u_2 = \frac{-p_{v2} + p_{c2} - p_{cr2}}{k_{p2}}
\]

(2.19)

where \( u_2 \) is the relief valve opening position in line 2 \((0 < u_2 < 1)\), \( p_{cr2} \) is the crack pressure setting for line 2, and \( k_{p2} \) is the spring stiffness for the spring acting on the relief valve 2.

While \( N > 0 \) (contact)

\[
\sum F = \alpha A_r(p_{v1} - p_{v2}) + p_{c2}(A_1 - A_r) + p_{c2}A_r - p_{v2}A_1 - A_r(p_{cr2} + k_{p2}u_2)
\]

\[
\sum p = p_{eq} = \sum \frac{F}{A_r}
\]

\[
p_{eq} = \alpha(p_{v1} - p_{v2}) - p_{v2} + p_{c2} - (p_{cr2} + k_{p2}u_2)
\]

(2.20)

Static equilibrium, \( p_{eq} = 0 \), hence

\[
p_{eq} = 0 \rightarrow u_2 = \frac{\alpha p_{v1} - p_{v2}(\alpha + 1) - p_{cr2} + p_{c2}}{k_{p2}}
\]

(2.21)
CHAPTER 2. SIMULATION MODEL

Same static analysis was done for the pressure relief valve in line 1 (between V1 and C1):

While $N > 0$ (no contact)

$$u_1 = \frac{-p_{v1} + p_{c1} - p_{cr1}}{k_{p1}}$$  \hspace{1cm} (2.22)

While $N < 0$ (contact)

$$u_1 = \frac{\alpha p_{v2} - p_{v1}(\alpha + 1) - p_{cr1} + p_{c1}}{k_{p1}}$$ \hspace{1cm} (2.23)
CHAPTER 2. SIMULATION MODEL

Simulink model

The VBSO valve has two relief valves and two check valves (fig 2.23). The simulink model is structured the same way with one check valve in parallel with each relief valve. The relief valves are simulated as orifices with variable discharge areas. The areas \(a_1\) and \(a_2\) are determined through the spool position, \(u\), and the maximum discharge area, \(A_{d,\text{max}}\). The discharge areas are assumed to increase linearly with the sled position. Hence,

\[
\begin{align*}
    a_1 &= A_{d,\text{max}} \cdot u_1 \\
    a_2 &= A_{d,\text{max}} \cdot u_2
\end{align*}
\]

(2.24)  
(2.25)

where \(u_1\) and \(u_2\) are given by equation 2.21 and 2.19.

Figure 2.23: Flow chart and simulink structure

The discharge area is calculated through the equation 2.21 and 2.19. These functions are calculated through this block diagram in simulink in fig 2.24. It is also added a response block to represent the spool response.
Figure 2.24: Simulink block diagram of the calculation of the discharge area, $a_1$

**Tuning discharge areas**

Maximum discharge areas for these valve were found by the same procedure as in section 2.4.2. A pressure drop over the pressure relief valve was ramped from 0 to 26 bar, while the valve was fully opened. At 26 bar the flow across the relief valve should be 140 l/min (app. H). The area was determined by setting the area to fit the final value at $Q = 140$ l/min and $\Delta p = 26$ bar. On the directional valve the pressure drop was ramped from 0 to 7 bar. At 7 bar pressure drop the flow should be 140 l/min. The check valve tuning was found in three steps. Firstly the 7 bar at 140 l/min determined the discharge area when the check valve is fully open. Secondly the crack pressure was set to 0.5 bar according to the data sheet (app. H), which determined the starting offset at $Q = 0$. The third setting was the pressure needed to fully open the check valve. The results were plotted and compared to the values obtained from the data specification sheet (marked with red dots in fig 2.25).
CHAPTER 2. SIMULATION MODEL

Figure 2.25: Simulated overcenter valve response, compared with readings from datasheet [H]

The curves gave a satisfying match with the obtained parameters (table 2.25).

Table 2.10: Best parameter results for the VBSO-DE-CC valve

<table>
<thead>
<tr>
<th>Description</th>
<th>VBSO-DE-CC-05.42.05-10-04-35</th>
</tr>
</thead>
<tbody>
<tr>
<td>( A_{m,prv} ) Max area, relief valve</td>
<td>43mm(^2)</td>
</tr>
<tr>
<td>( p_{cr,cv} ) Crack pr., check valve</td>
<td>0.5bar</td>
</tr>
<tr>
<td>( A_{m,cv} ) Max area, check valve</td>
<td>82mm(^2)</td>
</tr>
<tr>
<td>( p_{max,cv} ) Max opening pr., check valve</td>
<td>2.2bar</td>
</tr>
</tbody>
</table>

The remaining parameters to be considered are the frequency and damping ratio in the response block (fig 2.24), and the spring stiffness of the spring acting on the spool. These parameters are set to some temporary values to be able to use the model (table 2.11). To get a more accurate model these parameters should be determined through some experimental testing of the valve.
CHAPTER 2. SIMULATION MODEL

<table>
<thead>
<tr>
<th>Response frequency</th>
<th>$\omega$</th>
<th>30 Hz</th>
</tr>
</thead>
<tbody>
<tr>
<td>Response damping ratio</td>
<td>$\zeta$</td>
<td>1</td>
</tr>
<tr>
<td>Spring stiffness*</td>
<td>$k_p$</td>
<td>900 bar/unit</td>
</tr>
</tbody>
</table>

Table 2.11: Temporary variables.

Where bar is the force divided by the ring area, $A_r$, and one unit represent the spool movement from 0 to 1.

2.5 Hydraulic motors

The hydraulic motors are simulated with both leakage flow and friction (mechanical efficiency). The hydraulic motors used on the bridge crane and lower guiding arm are produced by Parker Hannifin and are of the F12 and F11 series (table 2.13. The volumetric efficiency is caused by leakage flow inside the motor and is simulated as a small orifice with the area, $A_{lm}$ (fig 2.27). This makes the motor leakage dependent of the inlet- and back- pressure. The model also contains two drain orifices, $A_{ld}$. These orifices are very small and their mission is to prevent static pressure in the system.

![Simulated motor, flowchart](image)

Figure 2.26: Simulated motor, flowchart

It is assumed that the volumetric efficiency for these is more or less the same[7]. The volumetric efficiency show a low efficiency at low velocities and a efficiency about 95% at high velocities (fig 2.27).
To tune in the leakage orifices, a small test was executed for each motor displacement (19, 30, 60). In this test the pressure drop over the motor was set to 210 bar due to fig 2.27, and then curve fitted with readings from fig 2.27. To perform a curve fitting the expression for the volumetric efficiency was needed. This was found by measuring the inlet flow and output shaft velocity. The inlet flow was used to calculate the theoretical velocity, and a velocity sensor on the output shaft gave the angular velocity. The volumetric efficiency was then calculated through this formula,

$$\eta_{vM} = \frac{Q_{tM}}{Q_M} = \frac{\omega \cdot D_M}{Q_M \cdot 2\pi}$$

where \(\omega\) is the output velocity, \(D_M\) is the motor displacement, \(Q_M\) is the inlet flow, and \(Q_{tM}\) is the theoretical flow demand.

- \(\eta_{vM}\): Volumetric efficiency
- \(Q_{tM}\): Theoretical flow demand of the motor, \([m^3/s]\)
- \(Q_M\): Actual flow demand of the motor, \([m^3/s]\)
- \(D_M\): Stroke displacement, \([m^3/rev]\)

Table 2.12: Variables in eq 2.26
The curve fitting gave the following results (fig 2.28).

![Figure 2.28: Comparing simulated volumetric efficiency with readouts.](image)

Given that the readings is quite rough and that the efficiency graph (from datasheet) is given with an accuracy of $\pm 2\%$\cite{7}, it is assumed that the result is more than accurate enough for this simulation model of the motor. The mechanical efficiency (friction) is implemented as a moment subjected to the outputshaft, this is explained in section 2.6. The obtained orifice values are shown in table 2.13.

<table>
<thead>
<tr>
<th>Place</th>
<th>Type</th>
<th>Leakage area, $A_{lm}$</th>
<th>Leakage area, $A_{ld}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bridge travel, BC</td>
<td>F12-030-MS-SV-S VOAC SAE B</td>
<td>0.13mm$^2$</td>
<td>0.0001mm$^2$</td>
</tr>
<tr>
<td>Trolley travel, BC</td>
<td>F12-030-MS-SV-S VOAC SAE B</td>
<td>0.13mm$^2$</td>
<td>0.0001mm$^2$</td>
</tr>
<tr>
<td>Slewing, BC</td>
<td>F12-060-MS-SH-S VOAC SAE C</td>
<td>0.263mm$^2$</td>
<td>0.0001mm$^2$</td>
</tr>
<tr>
<td>Trolley LGA</td>
<td>F11-019-MB-SH-S VOAC SAE B</td>
<td>0.083mm$^2$</td>
<td>0.0001mm$^2$</td>
</tr>
<tr>
<td>Slewing LGA</td>
<td>F12-030-MS-SV-S VOAC SAE B</td>
<td>0.13mm$^2$</td>
<td>0.0001mm$^2$</td>
</tr>
</tbody>
</table>

Table 2.13: Discharge areas, volumetric efficiency

The drain orifices were set to a almost negligible area of $10^{-4}mm^2$. The leakage orifice to tank is nonetheless included because it prevents static pressure in the system.
2.6 Effective friction

The applied friction force is added as a moment to the output shaft on the motors. This moment is calculated in a function block and depends on pressure loss over the motor, rotational velocity on output shaft, and motor displacement. The motor friction is simulated with the coulomb plus viscous friction model (fig 2.29), and is dependent on the output moment.

\[ F_M = (1 - \nu_{hm}) \cdot M_o = (1 - \nu_{hm}) \cdot \frac{\Delta p \cdot D_M}{2\pi} \]  

(2.27)

where \( F_M \) is the motor friction, \( \nu_{hm} \) is the hydromechanical efficiency, \( M_o \) is the output shaft moment, \( D_M \) is motor displacement, and \( \Delta p \) is the pressure loss through the motor. The hydromechanical efficiency is set to 0.9. Since there is no experimental data of the model the additional friction moment/force is set to be 10% of the created moment/force. This 10% could represent among other things, sliding friction, rack pinion friction and so on. How the friction moment model

![Diagram](image)

Figure 2.29: Coulomb + viscous friction model

(eq 2.27 and fig 2.29) acts dependent on velocity and moment is shown in fig 2.30.
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Figure 2.30: Plot verifies the direction of the friction moment

It may be that the actual friction also depends on the velocity, have hysteresis and stiction forces, but because friction is complex and experimental data is vital to get a good friction model it is chosen to use simple friction models. To examine how an increased friction will affect the design parameters of the model, it is in Chapter 4 looked at how an increased viscous friction dependent velocity (fig 2.31) will affect the system.

Figure 2.31: Viscous friction dependent on velocity
2.7 Effective mass moment of inertia, BC

The inertia is coupled directly to the motor output shaft. Because of this the effective mass moment of inertia (MMI) was calculated dependent on the masses acting and the shaft and gearing ratios. The mass moment of inertia for the gears and rotational shafts is considered negligible compared to the main parts, bridge, trolley, and guide mast. To keep a low complexity and a fast running simulation model the MMI was calculated dependent on the rotational motor shaft.

![Diagram](image)

Figure 2.32: Power transfer

To obtain the right gearing ratio it was important to determine how each part moved. As seen in fig 2.32, the trolley travel and bridge travel has a rack and pinion system, which make the gearing dependent on the pinion gear. On the slewing system the pinion on the motor shaft is coupled to a ring gear. Hence the gearing is dependent on both pinion radius and ring gear radius. In addition to this all of the motors have a gearbox.
The MMI for bridge and trolley travel was calculated with the formula,

$$J_m = \frac{(m + m_L) \cdot r^2}{n_g^2}$$ (2.28)

where $J_m$ is the MMI for the translational mass $(m + m_L)$, $m_L$ is the load mass (the pipe), $r$ is the pinion radius, and $n_g$ is the gearbox ratio. Because of the complex geometry of the guide mast, it was assumed that the guide mast was a cylindrical part with radius of 0.8 m and the additional load inertia was added as a point mass, with a distance $r_{tp} = 2100 mm$ from the slewing axis. This gave,

$$J_m = \frac{1}{2} \cdot m \cdot r_S^2 + \frac{m_L \cdot r_{tp}^2}{n_G^2}$$ (2.29)

where $m$ is guide mast mass, $r_S$ is the assumed radius, and $n_G$ is the gearing ratio between the rotating guide mast and motor shaft. Hence the $n_G$ is dependent on both gearbox ratio, and pinion and ring gear radius.

<table>
<thead>
<tr>
<th>Motor</th>
<th>Gearing ratio, $n_G$</th>
<th>Mass, $m$ [kg]</th>
<th>Radius, $r$ [m]</th>
<th>MMI, $J$ [kgm$^2$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bridge travel</td>
<td>39.0</td>
<td>22997</td>
<td>$r_{p,BT} = 75e - 3$</td>
<td>$J_{m,BT} = 0.085 + \frac{m_L \cdot r_{p,BT}^2}{n_G^2}$</td>
</tr>
<tr>
<td>Trolley travel</td>
<td>38.4</td>
<td>13006</td>
<td>$r_{p,TT} = 55e - 3$</td>
<td>$J_{m,TT} = 0.027 + \frac{m_L \cdot r_{p,TT}^2}{n_G^2}$</td>
</tr>
<tr>
<td>Slewing</td>
<td>$44.6 \cdot \frac{1200}{152}$</td>
<td>5741</td>
<td>$r_S = 0.8$</td>
<td>$J_{m,S} = 0.011 + \frac{m_L \cdot r_{tp}^2}{n_G^2}$</td>
</tr>
</tbody>
</table>

Table 2.14: MMI caused by moving mass presented on motor shaft. Masses and geometry values were obtained in component drawings.

The motor inertias was also added, and data was obtained from the motor specification sheets (app. I). Motor inertia for bridge travel (BT), trolley travel (TT) and slewing (S) were:

$$J_{m,BT} = 0.0034kgm^2 \quad J_{m,TT} = 0.0017kgm^2 \quad J_{m,S} = 0.005kgm^2$$
The inertias inserted in the model was the sum of these inertias,

\[ J_{BT} = J_{m,m_{BT}} + J_{m,BT} \quad J_{TT} = J_{m,m_{TT}} + J_{m,TT} \quad J_{S} = J_{m,m_{S}} + J_{m,S} \]

where \( J_{BT}, J_{TT}, J_{S} \) is the total MMI for BT, TT, and S.

Note that these are rough estimates of the inertias and that more accurate measurement could be found by using 3D cad models. However these estimates are believed to be accurate enough for this model.
2.8 Effective mass and mass moment of inertia, LGA

The LGA model consists of four actuators. Two cylinders and two motors. The cylinders perform the telescope extension and the jib tilt, and the motors perform trolley travel and slewing (fig 2.33). Since the system is modeled as a one dimensional system, there is a need for effective inertias and masses to replace the multibody dynamics. Most of these masses and inertias are dependent of the position and the velocity LGA. For example one can easily see that the slewing (rotating the LGA) inertia is dependent on the extension of the telescope. The key parameters to obtain the effective masses and inertias with are $\theta$, $J_A$, and $J_S$. The $\theta$ is the telescope angle, $J_A$ is the MMI around joint A and $J_S$ is the effective slewing inertia (fig 2.34).

Figure 2.33: Drawing of the LGA showing the functionalities implemented in the simulation model.
2.8.1 Geometry LGA

The geometry of the LGA is important to determine the local inertias and the
kinematics, which will give the inertias $J_A$, $J_S$ and the relationship between the
cylinder extension and $\theta_1$.

![Diagram showing geometry and location of center of mass. Global Z-axis and local ζ-axis works perpendicular to the paper plane pointing outwards.]

Figure 2.34: Geometry and location of center of mass. Global Z-axis and local ζ-axis works perpendicular to the paper plane pointing outwards.

$m_i, (\xi_i, \eta_i)$ : Mass and local mass center coordinates (referred to as $r_{mi}$).

$R_{mi}$ : Global coordinates to mass center, part $i$.

$r_{mi}$ : Local coordinates to mass center, part $i$, referred to fig 2.34.

$A_i$ : Transformation matrix from local to global vectors, part $i$.

$\theta_i$ : Angle between the global and the local coordinate system, $i$.

From the figure above one can see that the angle $\theta_1$ depends on the cylinder extraction $d_1$. Extracting the telescope will affect the inertia and mass center, and so on.
2.8.2 Obtain $\theta_1(d_1)$

To calculate the different inertias and effective masses, it is necessary to know the position of the LGA. This include the telescope angle, $\theta_1$, that is a function of the cylinder extension $d_1$ (fig 2.34) This relationship is given by the kinematics of the model. The basic equations are related to the ABC triangle (fig 2.34).

Local vector to joint C, and global vector to joint B:

$$\vec{r}_c = \begin{bmatrix} 2191 \\ 340 \end{bmatrix} \quad \vec{R}_B = \begin{bmatrix} -775 \\ 0 \end{bmatrix}$$

Transformation matrices (transforms from local to global coordinates):

$$A_i = \begin{bmatrix} \cos \theta_i & -\sin \theta_i \\ \sin \theta_i & \cos \theta_i \end{bmatrix} \quad B_i = \frac{\delta A_i}{\delta \theta_i} \begin{bmatrix} -\sin \theta_i & -\cos \theta_i \\ \cos \theta_i & -\sin \theta_i \end{bmatrix}$$

The relationship between distance, $d_1$, and angle $\theta_1$ according to Pythagoras:

$$0 = d_1^2 - \left( A_1 \begin{bmatrix} 2191 \\ 340 \end{bmatrix} - \begin{bmatrix} -775 \\ 0 \end{bmatrix} \right)^T \left( A_1 \begin{bmatrix} 2191 \\ 340 \end{bmatrix} - \begin{bmatrix} -775 \\ 0 \end{bmatrix} \right) \quad (2.30)$$

$$d_1 = \sqrt{(2191 \cos \theta_1 - 340 \sin \theta_1 + 775)^2 + (2191 \sin \theta_1 + 340 \cos \theta_1)^2} \quad (2.31)$$

The velocity relationship was found by time differentiation of eq 2.30.

$$0 = 2 \cdot d_1 \cdot \dot{d}_1 - 2 \cdot \left( A_1 \begin{bmatrix} 2191 \\ 340 \end{bmatrix} - \begin{bmatrix} -775 \\ 0 \end{bmatrix} \right)^T \left( \dot{\theta}_1 \cdot B_1 \begin{bmatrix} 2191 \\ 340 \end{bmatrix} \right) \quad (2.32)$$
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\[
\begin{align*}
C1 & \quad -263500 mm^2 \\
C2 & \quad -1698025 mm^2
\end{align*}
\]

Then solved for \( \dot{d}_1 \) and simplified.

\[
\dot{d}_1 = \frac{\dot{\theta}_1}{d_1} \left( (2191 \cos \theta_1 - 340 \sin \theta_1 + 775) \cdot (-2191 \sin \theta_1 - 340 \cos \theta_1) + \\
(2191 \sin \theta_1 + 340 \cos \theta_1) \cdot (2191 \cos \theta_1 - 340 \sin \theta_1) \right)
\]

\[
\rightarrow \quad \dot{d}_1 = \frac{\dot{\theta}_1}{d_1} \left( -263500 \cos \theta_1 - 1698025 \sin \theta_1 \right) \tag{2.33}
\]

Where \( \dot{\theta}_1 \) is the angular velocity (s\(^{-1}\)) of the main arm and \( \dot{d}_1 \) is the translational velocity of cylinder 1 in mm/s. The equations 2.31 and 2.33 show the connection between position and velocity of the cylinder and the rotation and angular velocity of the telescopic arm.

From equation 2.31 and 2.33 these expressions are solved for \( \theta_1 \) and \( \dot{\theta}_1 \):

\[
\theta_1 = f_1(d_1) \tag{2.34}
\]

Function \( f_1(d_1) \) is a very large expression and is shown in appendix D.

\[
\dot{\theta}_1 = \frac{\dot{d}_1 \cdot d_1}{(-263500 \cos \theta_1 - 1698025 \sin \theta_1)} \tag{2.35}
\]

The expressions for \( \theta_1 \) in eq 2.34 and 2.35 is now possible to implement in the simulation model, and are used to calculate the inertias \( J_A \) and \( J_S \).
2.8.3 Local mass moment of inertia

To calculate the total MMI for jib tilt (parallel to the Z axis) and slewing (parallel to the Y axis) it was necessary to calculate the MMI for each part. These local inertias is together with the parallel-axis theorem used to obtain the jib tilt MMI, $J_A$ and slewing MMI, $J_S$. The local MMI was calculated for the four moving parts (fig 2.35). The parts are simplified to be able to do some simple hand calculations. It is assumed that these rough hand calculations will be more than accurate enough for this simulation model, if necessary one could obtain the exact inertias with use of data from cad-models.

![Figure 2.35: Mass centers](image)

Figure 2.35: Mass centers
PART 1, MAIN ARM

The main arm is modeled as a beam with a square cross-section, with height, \( S_1 \) and length, \( L_1 \).

\[
m_1 = 401.3 kg \\
S_1 = 0.300 m \\
L_1 = 3.0 m
\]

\[ \vec{r}_{m1} = [1.5 m \ 0.05 m \ 0 m] \]

The local MMI around the mass center,

\[
J_{1,\xi} = \frac{7}{24} m_1 S_1^2 + \frac{m_1 L_1}{12} \\
J_{1,\eta} = \frac{7}{24} m_1 S_1^2 + \frac{m_1 L_1}{12} \\
J_{1,\zeta} = \frac{m_1 S_1^2}{3}
\]

where \( J_{1,\xi} \), \( J_{1,\eta} \) and \( J_{1,\zeta} \) are the local MMI around the mass center.
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Part 2, Telescopic arm

The telescopic arm is also modeled as if it was cylindrical:

\[
\begin{align*}
  m_2 &= 265.2 \text{kg} \\
  S_2 &= 0.250 \text{m} \\
  L_2 &= 3.13 \text{m}
\end{align*}
\]

\[
\begin{align*}
  \vec{r}_{m2} &= [1565 \text{m} \quad 0.075 \text{m} \quad 0 \text{m}] \\
  R_2 &= 0.250 \text{m}
\end{align*}
\]

Where \( R_2 \) is the cylinder radius, \( L_2 \) is the length, and \( \vec{r}_{m2} \) is the mass center location with local coordinates.

\[
\begin{align*}
  J_{2,\xi} &= \frac{7}{24} m_2 S_2^2 + \frac{m_2 L_2}{12} \\
  J_{2,\eta} &= \frac{7}{24} m_2 S_2^2 + \frac{m_2 L_2}{12} \\
  J_{2,\zeta} &= \frac{m_2 S_2^2}{3}
\end{align*}
\]

where \( J_{2,\xi}, J_{2,\eta} \) and \( J_{2,\zeta} \) are the local MMI around the mass center.
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Part 3, Gripper head

The gripper head was modeled as a solid box (fig 2.37). The gripper head was also assumed to always be horizontally ($\theta_3 = 0$).

![Figure 2.37: Box](image)

\[ a = 1.26m \quad b = 0.40m \quad c = 0.43m \quad m_3 = 175.2kg \]

\[ J_{3,\zeta} = \frac{m_3(a^2 + c^2)}{12} \]  
\[ J_{3,\eta} = \frac{m_3(a^2 + b^2)}{12} \]  

Part 4, Baseplate

When slewing, the baseplate is also rotating. The baseplate is assumed to be a disk with an inner and outer diameter, yielding:

\[ J_{4,Y} = J_{4,S} = \frac{m_4(R^2 + r^2)}{2} \quad R = 1.2m \quad r = 0.6m \quad m_4 = 362kg \]

where $R$ is the outer diameter, $r$ is the inner diameter, and $m_4$ is the baseplate weight.
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The local inertias are now established for the LGA with four parts. Inertias from cylinders and pistons are neglected.

2.8.4 Slewing MMI

To obtain the effective MMI for slewing the system is looked at as a two dimensional system (fig 2.38). The two interesting MMIs are the ones around the local \( \xi \) and \( \eta \) axis, because these will affect the global MMI parallel to the Y axis.

![Figure 2.38: The four parts of the LGA.](image)
Trough Nikravesh equation for 2-dimensional dynamics, the local MMIs are converted to global inertias.

\[ J_i = A_i J_i' A_i^T \]

\[ A_i = \begin{bmatrix} \cos \theta_i & -\sin \theta_i \\ \sin \theta_i & \cos \theta_i \end{bmatrix} \]

\[ J_i' = \begin{bmatrix} J_{i,\xi} & 0 \\ 0 & J_{i,\eta} \end{bmatrix} \]

(2.44)

\[ J = \begin{bmatrix} J_{i,X} \\ J_{i,Y} \end{bmatrix} \]

(2.45)

\[ J_{i,Y} = J_{\xi} \sin \theta_i^2 + J_{\eta} \cos \theta_i^2 \]

(2.46)

Where \( J_{i,Y} \) is the local MMI around an axis parallel to the global Y-axis. Using eq. 2.46 and the parallel-axis theorem give,

\[ J_{1,S} = m_1(e + \frac{L_1}{2}) \cos \theta_1 + J_{1,\xi} \sin \theta_1 + J_{1,\eta} \cos \theta_1 \]

(2.47)

\[ J_{2,S} = m_2(e + (d_2 - \frac{L_2}{2}) \cos \theta_1)^2 + J_{2,\xi} \sin \theta_1 + J_{2,\eta} \cos \theta_1 \]

(2.48)

\[ J_{3,S} = m_3(e + \frac{L_3}{2} + (d_2) \cos \theta_1)^2 + J_{3,\eta} \cos 0 \]

(2.49)

\[ J_{4,S} = J_{4,Y} \]

(2.50)

where \( e \) is the distance from joint A to the slewing axis (fig 2.38), \( d_2 \) is the telescope extension (fig 2.35), and \( J_{i,S} \) is the local MMI around mass center of part \( i \) (section 2.8.3).

The MMI for slewing around the slewing axis (s-axis in fig 2.38):

\[ J_S = J_{1,S} + J_{2,S} + J_{3,S} + J_{4,S} \]

(2.51)

Where the \( J_S \) depends on the rotated parts (part 1, 2, 3, 4 see fig 2.38). To obtain the effective MMI subjected to the motor shaft, the gearing between the slewing axis and the motor shaft need to be considered (fig 2.39).
This geometry (fig 2.39) give,

\[ n_{\text{tot}} = n_g \cdot \frac{D_{\text{irg}}}{d_p} \]  \hfill (2.52)

where \( n_{\text{tot}} \) is the gearing ratio between motor axis and slewing axis, \( n_g \) is the gearbox ratio, \( D_{\text{irg}} \) is the pitch diameter of the internal ring gear, and \( d_p \) is the pitch diameter of the pinion gear connected to the motor. This give an effective MMI for slewing acting on the motor shaft,

\[ J_{\text{sm}} = \frac{J_S}{n_{\text{tot}}^2} + J_m + J_g \]  \hfill (2.53)

Where \( J_m \) is the MMI for the motor, \( J_g \) is the MMI for the gearbox, and \( n_{\text{tot}} \) and \( J_S \) correspond to the variables in equation 2.52 and 2.51.
2.8.5 Trolley travel MMI

The effective MMI for the trolley travel is given by the trolley mass and the gearing ratio. The gearing ratio is given by the gearbox ratio and the pitch diameter of the pinion gear (fig 2.40).

\[ J_{tt} = m_{tt} \frac{r_p^2}{n_g} + J_m + J_g \]  

(2.54)

where \( J_{tt} \) is the effective MMI, \( m_{tt} \) is the mass of the trolley included the mass of the LGA, \( r_p \) is the pitch radius, \( n_g \) is the gearing ratio of the gearbox, \( J_m \) is the MMI for the motor, and \( J_g \) is the MMI for the gearbox.
2.8.6 Effective mass

The effective mass of cylinder one is calculated from a kinematic energy consideration (eq 2.60). The formula is dependent on the angular velocity, translational velocity of the piston, and the MMI around joint A (joint A has a rotational degree of freedom around Z-axis, in fig 2.35). The MMI was obtained dependent on the gravitational center and local MMI for each part.

To calculate the MMI around the center of mass the center of mass coordinates are necessary. Center of mass (global coordinates):

\[
\begin{bmatrix}
X_G \\
Y_G
\end{bmatrix} = \frac{A_1 \vec{r}_m^1 + (\vec{R}_{cs2} + A_2 \vec{r}_m^2) \cdot m_2 + (\vec{R}_{cs3} + A_3 \vec{r}_m^3) \cdot m_3}{m_1 + m_2 + m_3} 
\]

(2.55)

\[
\vec{R}_G = \begin{bmatrix}
X_G \\
Y_G
\end{bmatrix}
\]

(2.56)

The \( \vec{R}_{csi} \) is the global coordinates for the local coordinate systems corresponding to part \( i \), and are respectively:

\[
\vec{R}_{cs1} = \begin{bmatrix}
0 \\
0
\end{bmatrix} \quad \vec{R}_{cs2} = A_1 \begin{bmatrix}
d_2 \\
-50
\end{bmatrix}^T \quad \vec{R}_{cs3} = \vec{R}_{c2}
\]

The parallel-axis theorem was used to calculate the MMI parallel to the Z-axis in the gravitational mass center of the guiding arm.

\[
J_{GZ} = J_{1,\zeta} + m_1 \cdot |\vec{R}_G - A_1 \cdot \vec{r}_m^1|^2 + \\
J_{2,\zeta} + m_2 \cdot |\vec{R}_G - (\vec{R}_{cs2} + A_2 \cdot \vec{r}_m^2)|^2 + \\
J_{3,\zeta} + m_3 \cdot |\vec{R}_G - (\vec{R}_{cs3} + A_3 \cdot \vec{r}_m^3)|^2
\]

(2.57)

where \( J_{i,\zeta} \) is the local MMI around the mass center for part \( i \) (see eq 2.38, 2.41, and 2.42), \( m_i \) is the mass of part \( i \), \( A_i \) is the transformation matrix for part \( i \), \( \vec{r}_m^i \) is the local vector from the local coordinate system to the local mass center in part \( i \) (fig 2.34), \( R_G \) is the global center of gravity vector, and \( R_{csi} \) is the global position of the local coordinate systems.
CHAPTER 2. SIMULATION MODEL

By using parallel-axis theorem the jib tilt inertia around point A ($J_A$) is derived

$$J_A = J_G + m_G \cdot r^2_G = J_G + m_G(X_G^2 + Y_G^2) \quad (2.58)$$

Through the equations to calculate $\theta_1$ and $\dot{\theta}_1$ and $J_A$ (eq: 2.31, 2.33, 2.58) the effective mass is calculated. The effective mass was calculated due to the equilibrium between rotational and translational kinetic energy.

$$E_{kin} = \frac{1}{2} m \dot{x}^2 = \frac{1}{2} J \dot{\theta}^2 \quad (2.59)$$

$$m = J \frac{\dot{\theta}^2}{\dot{x}^2} \quad (2.60)$$

Equation 2.60 give a this formula for the effective mass acting on cylinder 1.

$$m_{1,eff} = J_A \frac{\dot{\theta}_1^2}{d_1^2} \quad (2.61)$$

The formula gave a variable effective mass working on cylinder 1 (jib tilt cylinder) corresponding to figure 2.41.

![Figure 2.41: Effective mass dependent on cylinder positions](image)

Figure 2.41: Effective mass dependent on cylinder positions
CHAPTER 2. SIMULATION MODEL

The effective mass of cylinder 2 is simply the sum of \( m_2 \) and \( m_3 \), because the cylinder perform a pure translation of the body parts two and three.

\[
m_{2,\text{eff}} = m_2 + m_3
\]  
(2.62)

2.9 Effective force due to gravity

The effect of gravity on the BC is nonexistent since all motions occurs in the horizontal plane and is guided with rails. On the LGA the gravity will have a larger influence. Because the simulation model is one dimensional, only the dynamic forces due to accelerations of inertias and masses will be visible. To implement the static forces acting on the cylinders, the forces were calculated in a function block implemented in the simulation model controlling an ideal force acting on each cylinder. Forces due to centripetal acceleration, friction and weight of hydraulic cylinders are neglected. The forces counted for is the gravitational force acting on the telescope arm. The forces acting on the jib tilt cylinder (cylinder 1) is calculated due to moment equilibrium. The cylinder force \( F_{c1} \) then becomes,

\[
\sum M_A = 0 = X_G m_{\text{tot}} g - F_{c1} R_{cy} \cos \theta_2 + F_{c1} R_{cx} \sin \theta_2
\]  
(2.63)

\[
F_{c1} = \frac{X_G m_{\text{tot}} g}{R_{cy} \cos \theta_2 - R_{cx} \sin \theta_2}
\]  
(2.64)

where \( g \) is the gravitational acceleration (9.81 m/s\(^2\)), \( X_G \) is the global x-coordinate of the mass center (eq. 2.55), \( m_{\text{tot}} \) is the total weight of the moving masses on the LGA \( (m_1 + m_2 + m_4) \), \( \theta_1 \) is the telescope angle, \( \theta_2 \) is the jib tilt cylinder angle, and \( F_{c1} \) is the static force acting on cylinder one (fig 2.42).
Figure 2.42: Simplified model of the LGA to calculate cylinder forces

The static forces acting on the telescope cylinder (cylinder 2) are caused by the inner telescope arm \( m_2 \) and the gripper head \( m_3 \).

\[
F_{c2} = \sin \theta_1 \cdot (m_2 + m_3) \cdot g
\]  

(2.65)

Where \( m_2 \) and \( m_3 \) are the masses of the telescopic arm and the gripper head, and \( F_{c2} \) is the static force acting on cylinder two (inside the telescope arm).
2.10 Simulink model

2.10.1 Bridge Crane

The simulation model was assembled due to the corresponding drawing sheets (app. B). Orifices due to pipes and bendings are not implemented in the model.

To explain the initial positions of the bridge crane, the figure below is made. The tool point (TP) position in fig 2.43 is at point [0,0].

\[
x = 2100 \sin \alpha + b_{pos} \\
y = 2100 - 2100 \cos \alpha + t_{pos}
\]

where \( b_{pos} \) and \( t_{pos} \) is the bridge travel and trolley travel position given by the motor rotation angle in the model.
The simulink model consists of three main circuits (fig 2.44), bridge travel, trolley travel and slewing. Each circuit is very similar and consists of a directional servo valve, mentioned in section 2.2. All circuits are connected with a hydraulic motor, and in between of the motor and the directional valve it is placed a motion control valve. On the motor shafts there is connected a friction moment, and an inertia corresponding to the weight and gearing of the mechanical system.

Figure 2.44: Simulation model bridge crane
CHAPTER 2. SIMULATION MODEL

From the model it is possible to extract a lot of data, for instance pressures, spool positions, motor shaft moment, velocities, control signals, and flow consumption. To demonstrate this, the trolley travel is simulated (fig 2.45).

Figure 2.45: Simulated results for trolley travel
2.10.2 Lower guiding arm

The lower guiding arm is built due to the drawing sheets (app. C). The forces and variable inertias are calculated in the yellow function block (on the right side in fig 2.46).

Figure 2.46: Simulation model LGA
Chapter 3

Experimental Test

3.1 Test introduction

The modeling of the overcenter valves is important for the overall modeling of the bridge crane and the lower guiding arm. Therefore, experimental work was carried out to investigate validity of the modeling approach and for identify parameters. A test was performed on the VAA-B-SICN-ST-VF-250 overcenter valve from Bosch Rexroth Oil Control. This specific valve is used with all three hydraulic motors on the bridge crane. The test was conducted to determine spring stiffness, spool response and to validate the crack pressure setting of the valve.

Figure 3.1: Test rig assembly
3.2 Test rig and measure points

The test assembly was built up as shown in figure 3.2, seen below. Between the PVG and measure point \( p_1 \) and \( p_2 \) there is used pipes, and from the flow sensor and \( p_2 \) it is used tubes with a length of approximately 1m each. Measure point \( p_3 \) is connected with pipes.

![Test rig diagram](image)

**Figure 3.2: Test rig diagram.**

*PVG: Proportional directional valve. MCV: Motion control valve*

The measure points (MP) signal names are related to figure 3.2

<table>
<thead>
<tr>
<th>MP</th>
<th>Signal</th>
<th>Description</th>
<th>Type</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>( p_1 )</td>
<td>A-port pressure, control valve</td>
<td>State</td>
<td>Bar or MPa</td>
</tr>
<tr>
<td>2</td>
<td>( p_2 )</td>
<td>B-port pressure, control valve</td>
<td>State</td>
<td>Bar or MPa</td>
</tr>
<tr>
<td>3</td>
<td>( p_3 )</td>
<td>Pressure on &quot;load side&quot; of mcv</td>
<td>State</td>
<td>Bar or MPa</td>
</tr>
<tr>
<td>4</td>
<td>( Q )</td>
<td>Flow through port A, control valve</td>
<td>State</td>
<td>Bar or MPa</td>
</tr>
<tr>
<td>5</td>
<td>( u )</td>
<td>Command signal, PVG</td>
<td>Input</td>
<td>%</td>
</tr>
</tbody>
</table>

Table 3.1: Measure points
CHAPTER 3. EXPERIMENTAL TEST

3.3 Test Sequences

These three tests were executed with three different spring settings. The first one was with approximately the standard setting, the two others was plus and minus one turn on the spring adjustment screw.

Crack pressure test

To find the crack pressure for the specific setting, the PVG spool position was slowly ramped up manually. The test sequence was terminated when a visible flow was measured.

Multistep

To get some static measurements, the spool position was stepped up gradually to maximum travel.

Step response

In this sequence the PVG spool position was stepped from 0% up to 100%.

Figure 3.3: Flow route through the valve during test
CHAPTER 3. EXPERIMENTAL TEST

3.4 Result

3.4.1 Test sequence 1

In this sequence the goal was to determine the actual crack pressure setting for each of the three test settings. This crack pressure is important to later calculations of spool positions in section 3.4.2.

![Figure 3.4: Opening pressure. Setting 1, 2, 3.](image)

To calculate the crack pressure from these measurements, it was assumed that the spool position is equal zero when the flow increase becomes measurable. From eq 2.11 the following equation was derived. It assumes that spool positions is equal to zero \( u = 0 \), that both parts of the spool are connected \( N > 0 \), see fig.2.15) and that the pressure losses across the two check valves (fig.3.3) is equal \( (p_v - p_c) = p_{v1} - p_c \).

\[
\begin{align*}
  p_{cr} &= p_{v1} \cdot \alpha + p_{c2} - (p_{v2} + (p_{v1} - p_{c1})) \cdot (\alpha + 1) \\
  p_{cr} &= p_c \cdot (\alpha + 2) - p_{v1} - p_{v2} \cdot (\alpha + 1), \quad p_c = p_{c1} = p_{c2}
\end{align*}
\]

\( p_{cr} \) describe the total crack pressure including both springs \( (p_{cr} = p_{cr1} - p_{cr2}) \)
TABLE 3.2: Crack pressures, test settings and results

<table>
<thead>
<tr>
<th>Setting</th>
<th>$\alpha$</th>
<th>$p_1$</th>
<th>$p_{c1}$</th>
<th>$p_{c2}$</th>
<th>$p_c$</th>
<th>Set screw</th>
<th>Crack pr.,$p_{cr}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2.8</td>
<td>27.8bar</td>
<td>26.8bar</td>
<td>1.7bar</td>
<td>26.8bar</td>
<td>std. -1turn</td>
<td>95.4bar</td>
</tr>
<tr>
<td>2</td>
<td>2.8</td>
<td>42.2bar</td>
<td>41.2bar</td>
<td>1.7bar</td>
<td>41.6bar</td>
<td>std.</td>
<td>152.0bar</td>
</tr>
<tr>
<td>3</td>
<td>2.8</td>
<td>59.0bar</td>
<td>58.0bar</td>
<td>1.7bar</td>
<td>57.5bar</td>
<td>std. +1turn</td>
<td>211.5bar</td>
</tr>
</tbody>
</table>

These results (table 3.2) are manually readings from test result plots, and correspond to the average pressure from 0 to 0.5$l/min$. The pressure, $p_{c1}$, is calculated based on a pressure drop of 1bar over the flow sensor at $Q \approx 0$ (eq 3.4). The datasheet[8] say 2bar but this did not correspond with the measurements taken. From the results the assumption about the contact force $N$ being larger than zero is confirmed through eq2.4. The results corresponds quite well with the given specifications in the datasheet[6]. The standard setting should give a crack pressure of 150bar and 1 clockwise turn on the set screw should correspond to an increase in crack pressure of 62bar[6]. These test results gave a standard setting crack pressure of 152bar and an increase of approximately 58bar/turn. The fact that the crack pressure increases linearly with x turns on the adjustment screw indicates that the spring force is linear and that the spring constant is, indeed, constant. This assumption will be important in the next test sequence (sequence 2).
3.4.2 Test sequence 2

In this sequence the flow from the directional control valve is ramped up in steps. Each step moves the main spool of the directional control valve 8% of max travel. The steady state values from each step are logged and used to estimate the spring stiffness.

The first seven steps for each setting was manually read out:

\[
\begin{align*}
\text{SET}_1 &= \begin{pmatrix} p_1 & p_2 & p_3 & Q \end{pmatrix} = \begin{pmatrix} 33.4 & 1.7 & 31.2 & 12.5 \\ 39.3 & 2.3 & 36.0 & 24.6 \\ 44.1 & 4.2 & 39.6 & 36.3 \\ 48.6 & 6.0 & 42.8 & 47.7 \\ 53.3 & 7.9 & 46.2 & 59.6 \\ 58.0 & 9.6 & 49.2 & 70.5 \\ 62.2 & 11.3 & 51.8 & 80.8 \end{pmatrix} \\
\text{SET}_2 &= \begin{pmatrix} p_1 & p_2 & p_3 & Q \end{pmatrix} = \begin{pmatrix} 53.8 & 2.1 & 50.3 & 24.5 \\ 58.0 & 3.8 & 53.5 & 36.0 \\ 62.2 & 5.6 & 56.5 & 47.4 \\ 66.5 & 7.3 & 59.2 & 59.2 \\ 70.6 & 8.95 & 61.9 & 70.2 \\ 75.5 & 11.1 & 65.1 & 81.5 \\ 78.9 & 12.5 & 67.1 & 89.6 \end{pmatrix} \\
\text{SET}_3 &= \begin{pmatrix} p_1 & p_2 & p_3 & Q \end{pmatrix} = \begin{pmatrix} 65.8 & 1.7 & 63.5 & 12.8 \\ 70.8 & 2.4 & 67.4 & 24.6 \\ 74.9 & 4.2 & 70.4 & 35.6 \\ 78.8 & 5.8 & 73.1 & 46.6 \\ 83.3 & 7.6 & 76.0 & 57.9 \\ 87.1 & 9.1 & 78.3 & 68.8 \\ 89.4 & 9.8 & 79.5 & 75.5 \end{pmatrix}
\end{align*}
\]

Figure 3.5: Results from test sequence 2
CHAPTER 3. EXPERIMENTAL TEST

Fig 3.6 show the transmitter positions. Notice that the logged values are $p_1$, $p_2$ and $p_3$, and that they correspond to the $p_{v1}$, $p_{v2}$ and $p_c$ that are needed to identify the spring stiffness.

\[ p_{v1} = p_1 - \Delta p_f \quad p_{v2} = p_2 \quad p_c = p_3 \]

$\Delta p_f$: Pressure loss across the flow sensor.

The pressure loss across the flow sensor increases linearly with the flow according to the datasheet[8]:

\[ \Delta p_f = 2 \cdot 10^5 Pa + 24000 \cdot 10^5 \frac{Pa \cdot s}{m^3} \cdot Q \quad (3.3) \]

This formula did not match the measured data and a change of the formula was made:

\[ \Delta p_f = 1 \cdot 10^5 Pa + 30000 \cdot 10^5 \frac{Pa \cdot s}{m^3} \cdot Q \quad (3.4) \]
The next steps describe the spring stiffness calculation.

From the orifice equation we get:

\[ Q = A_d C_d \sqrt{\frac{\Delta p}{\rho}} \rightarrow A_d = \frac{Q \sqrt{\rho}}{C_d \sqrt{2 \Delta p}} \]  \hspace{1cm} (3.5)

The pressure loss over relief valve is:

\[ \Delta p = p_{c2} - p_t \]  \hspace{1cm} (3.6)

Assuming that \( p_t = p_{c2} + (p_{c1} - p_v) \) and \( p_c = p_{c1} = p_{c2} \)

\[ \Delta p = 2p_c - p_{c2} - p_v \]  \hspace{1cm} (3.7)

Combining eq3.5 and eq3.7, yields:

\[ A_d = \frac{Q \sqrt{\rho}}{C_d \sqrt{2(2p_c - p_{c2} - p_v)}} \] \hspace{1cm} (3.8)

The spool position is derived from \( A_d \):

\[ u = \frac{A_d}{A_{d,\text{max}}} \] \hspace{1cm} (3.9)

The spool position is also given by pressure equilibrium, see eq 2.11 (assumed \( p_t = p_{c2} + (p_{c1} - p_v) \) and \( p_c = p_{c1} = p_{c2} \)):

\[ u = \frac{p_c(\alpha + 2) - p_{cr} - p_{c2}(\alpha + 1) - p_v}{k_{p1} + k_{p2}} \] \hspace{1cm} (3.10)

Combining equations 3.8, 3.9 and 3.10, yields:

\[ k_p = k_{p1} + k_{p2} \] \hspace{1cm} (3.11)

\[ k_p = \frac{A_{d,\text{max}} C_d \sqrt{2\sqrt{2p_c - p_{c2} - p_v}}}{Q \sqrt{\rho}} \cdot (p_c(\alpha + 2) - p_{cr} - p_{c2}(\alpha + 1) - p_v) \] \hspace{1cm} (3.12)
Adopting the spring stiffness formula in equation 3.12, a highly non-constant spring stiffness was obtained (fig 3.7). The result show curves that are mainly dependent on flow and crack pressure setting. The irregularity in setting 1 is most likely caused by the low crack pressure setting. The minimum allowed crack pressure is set to 100bar [6]. Too low crack pressure setting could cause a gap between spring and spool. This mean that only one of the two springs is in contact with the spool. Hence it would cause a discontinuity in total spring stiffness.

From the crack pressure measurements it is known that the spring stiffness is approximately constant. Therefore, the results indicate that there is additional forces acting on the spool that is not yet taken into account. Since this force is complex and dependent of the orifice geometry, it is not possible to find an analytical expression. In stead a force function that ensures a constant spring stiffness has been introduced. Since all three settings have different slopes, it became necessary to make the new function dependent of the $p_{cr}$ setting. Another thing that was important was that the force should not affect the $p_{cr}$. Hence the force should be equal zero at low flow ($p_F(Q = 0) = 0$). The new force was added in to the existing pressure equilibrium as a positive force/pressure working on the ring pressure area, $A_r$ (fig 2.15).

Figure 3.7: Spring stiffness vs flow and pressure
CHAPTER 3. EXPERIMENTAL TEST

The force was added in the original pressure equilibrium:

\[
p_F(Q) = (1.66 \cdot 10^{-5} \cdot Q_{l/min}^4 - 3.0 \cdot 10^{-3} \cdot Q_{l/min}^3 + 0.071 \cdot Q_{l/min}^2 + 13.2 \cdot Q_{l/min}) \frac{Q \cdot z_1}{\sqrt{\Delta p}} \quad 180 \text{bar} < p_{cr}
\]

\[
p_F(Q) = (-1.9 \cdot 10^{-5} \cdot Q_{l/min}^4 + 5.2 \cdot 10^{-3} \cdot Q_{l/min}^3 - 0.55 \cdot Q_{l/min}^2 + 28.9 \cdot Q_{l/min}) \frac{Q \cdot z_1}{\sqrt{\Delta p}} \quad 120 \text{bar} > p_{cr} < 180 \text{bar}
\]

\[
p_F(Q) = (-4.4 \cdot 10^{-5} \cdot Q_{l/min}^4 + 0.011 \cdot Q_{l/min}^3 - 1 \cdot Q_{l/min}^2 + 40.5 \cdot Q_{l/min}) \frac{Q \cdot z_1}{\sqrt{\Delta p}} \quad p_{cr} < 120 \text{bar}
\]

The constants were manually tuned:

\[z_1 = 4.0847e + 5 \cdot 10^5 \quad \Delta p = p_c - p_t \quad Q_{l/min} = Q \cdot 60000\]

This \(p_F\) was added as a pressure in pressure equilibrium equation (eq 2.10)

\[p_{eq} = p_{c1} \alpha + p_{cr2} - k_{c2} \cdot u - p_t(\alpha + 1) + p_{c2} - p_{cr1} - k_{p1} \cdot u + p_F\]

Assumed:

\[p_{eq} = 0, \quad p_t = p_{c2} + (p_{c1} - p_{c1}), \quad \Delta p = p_{c2} - p_t, \quad p_c = p_{c1} = p_{c2}\]

\[\rightarrow u = \frac{p_c(\alpha + 2) - p_{cr} - p_{c2}(\alpha + 1) - p_{c1} + p_F}{k_{p1} + k_{p2}} \quad (3.13)\]

Combine equation 3.8, 3.9, 3.11.

\[k_p = \frac{C_d \sqrt{2} \sqrt{p_c \cdot p_{c2} - p_{c1}}}{Q \sqrt{\rho}} \cdot (p_c(\alpha + 2) - p_{cr} - p_{c2}(\alpha + 1) - p_{c1} + p_F) \quad (3.14)\]
Using equation 3.14 resulted in a more even spring stiffness (fig 3.8).

The spring stiffness settled around $895 \pm 15\text{bar/unit}$. As seen in fig 3.8 the highest accuracy was obtained between $20\text{l/min}$ and $100\text{l/min}$. This result confirms that the function are making the model more realistically.
CHAPTER 3. EXPERIMENTAL TEST

3.4.3 Test sequence 3

In this test the PVG was stepped from its neutral position to max opening and half opening. This test gave some pressure peaks before settling. These peaks are mainly caused by the spool response.

![Figure 3.9: Step response. 0% - 50%](image)

![Figure 3.10: Step response. 0% - 100%](image)
3.5 Comparing physical with simulated results

Figure 3.11: Simulink model of test assembly

To compare and validate the results a simulation model in simulink was built corresponding to the physical assembly. The pressure loss across the flow rate sensor was set due to eq 3.4. There is not implemented any pipes and fittings with losses except the gray block. This block has a variable orifice which is implemented to get the correct $p_{v2}$ pressure due to the experimental tests. A deviation of the $p_{v2}$ pressure will cause an offset error in $p_c$ and $p_{v1}$. This error will also lead to a different spool position and generate an even higher deviation in $p_{v1}$ and $p_c$. 
3.5.1 Crack pressure

The crack pressure is calculated based on $p_{v1}$, $p_{v2}$ and $p_c$.

$$p_{v1} = p_1 - \Delta p_f$$
$$p_{v2} = p_2$$
$$p_c = p_3$$

$\Delta p_f$: Pressure loss across the flow sensor.

The pressure loss across the flow sensor increases linearly with the flow (eq.3.4):

$$\Delta p_f = 1 \cdot 10^5 + 30000 \cdot 10^5 \cdot Q$$ \hspace{1cm} (3.15)

<table>
<thead>
<tr>
<th></th>
<th>Setting 1</th>
<th></th>
<th>Setting 2</th>
<th></th>
<th>Setting 3</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Exp.</td>
<td>Sim.</td>
<td>Exp.</td>
<td>Sim.</td>
<td>Exp.</td>
<td>Sim.</td>
</tr>
<tr>
<td>$p_1$ [bar]</td>
<td>27.8</td>
<td>28.1</td>
<td>42.2</td>
<td>42.8</td>
<td>59.0</td>
<td>58.6</td>
</tr>
<tr>
<td>$p_{v1}$ [bar]</td>
<td>26.8</td>
<td>27.1</td>
<td>41.2</td>
<td>41.7</td>
<td>58.0</td>
<td>57.7</td>
</tr>
<tr>
<td>$p_2$ [bar]</td>
<td>1.7</td>
<td>1.5</td>
<td>1.7</td>
<td>1.5</td>
<td>1.7</td>
<td>1.5</td>
</tr>
<tr>
<td>$p_3$ [bar]</td>
<td>26.8</td>
<td>26.6</td>
<td>41.6</td>
<td>41.2</td>
<td>57.5</td>
<td>57.2</td>
</tr>
<tr>
<td>$p_c$ [bar]</td>
<td>95.4</td>
<td>94.9</td>
<td>152.0</td>
<td>150.3</td>
<td>211.5</td>
<td>211.3</td>
</tr>
</tbody>
</table>

Table 3.3: Crack pressures from experimental test and simulation

The results are satisfying and the deviations in $p_c$ varies from 0.2 to 1.7bar. It can be seen that the $p_c$ function is very sensitive. In setting 2 the pressures $p_1$, $p_2$ and $p_3$ have a maximum deviation of only 0.6bar, but the $p_c$ fails with 1.7bar.
3.5.2 Spring stiffness

The same "multistep" procedure was done in simulink, and the corresponding values are inserted in table 3.4. The simulated values for pressure $p_1$, $p_2$, $p_3$, and flow $Q$ are compared to the experimental test data values.

<table>
<thead>
<tr>
<th></th>
<th>$p_1$ [bar]</th>
<th>$p_2$ [bar]</th>
<th>$p_3$ [bar]</th>
<th>$Q$ [l/min]</th>
</tr>
</thead>
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<tr>
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<td><strong>Set. 3</strong></td>
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<td>65.8</td>
<td>1.7</td>
<td>1.7</td>
</tr>
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<td>70.8</td>
<td>2.5</td>
<td>2.4</td>
</tr>
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<td>74.9</td>
<td>3.8</td>
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<td>5.8</td>
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<tr>
<td></td>
<td>84.5</td>
<td>89.4</td>
<td>10.1</td>
<td>9.8</td>
</tr>
</tbody>
</table>

Table 3.4: Multistep results
CHAPTER 3. EXPERIMENTAL TEST

The interesting value is the pressure drop over the pressure relief valve. The other pressure drops in the motion control valve is already confirmed (see section 2.4.2). The pressure drop over the pressure relief valve is determined by the spool position which again depends on the pressures acting on the spool. Hence the difference between the simulated results and the experimental results of the pressure drop over the main spool will indicate the accuracy of the simulated model (fig 3.12).

![Graph showing pressure drop error]

Figure 3.12: Difference (error) between the pressure drop across the spool \((p_3 - p_2)\) in the simulation model and the experimental test

The figure show a high accuracy around 50 l/min, with a pressure drop error less than 0.5 bar. As the flow approaches 100 l/min the error increases.
Figure 3.13: The flow force divided by the ring pressure area, $A_r$, giving $p_F$

In figure 3.13 the additional flow force added as $p_F$ in the pressure equilibrium is shown. The results correspond with the pressure force added in the multistep test.
3.6 Spool response

The response test was executed by giving a stepped input signal to the PVG. The experiment was conducted with steps from 0-100% and 0-50%. Because this test did not have the ability to measure the spool position directly, the pressure between the two ports $p_{c1}$ and $p_{c2}$ was used, $(p_c)$. The response of this pressure will give a good indication of the correctness of the spool response.

![Figure 3.14](image1.png)

Figure 3.14: Response when the PVG spool is stepped from 0 to 100% opening.

![Figure 3.15](image2.png)

Figure 3.15: Response when the PVG spool is stepped from 0 to 50% opening.

From the results (fig 3.14 and 3.15) we see that most of the curves have a significant first peak. This peak appears because the fluid is pressurized before the
valve opens. Therefore, this peak will depend on the oil stiffness and/or volume of the pressure chamber $p_3$ (fig 3.11). Figure 3.16 show the effect of increasing the $p_3$ chamber volume. The next peak have a less steep slope and this slope represents the spool response. The spool response is tuned in such that the slopes of the second peak is quite similar (see left hand side plot in fig3.16).

![Figure 3.16: Response plot with a PVG spool step from 0-100%](image)

The results (fig 3.15 and 3.14) show a quite large deviation between the simulated and measured results of the highest crack pressure setting (setting 3, $p_{cr} = 211$ bar). For setting 1 the results are good, and for setting 2 there are similarities but less accurate than setting 1.

With the existing model parameters it was difficult define the best and most correct fit. The pressure response that is measured is not only dependent of the spool response but also the volume sizes surrounding the spool. Another aspect that is not taken into account in the simulation model is the spool friction. The spool friction may have some stick slip properties that could contribute to give a more accurate model of the response. The friction may also include some hystere-
sis effect caused by the sealing rings.

Aside from the frictional effects and other possible influences, the best fitted second order response (fig 3.14 and 3.15) was with a frequency about 50Hz, a damping ratio equal 1 and a volume in pressure chamber $p_3$ of 0.1 litre.
3.7 Sub-conclusions

The results are good according to data sheets and the model versus experiments.

The spring stiffness measurements clearly revealed the need for an extra steady state force acting on the spool. It was assumed that this was related to the flow force and it was possible to develop a flow force model that supported the idea of a linear spring. Because the fitted force is only accurate for the three tested crack pressure settings (95 bar, 152 bar and 211 bar) the model is only accurate for these settings. To keep the same accuracy for other crack pressure settings it is necessary to make new flow force curves, \( p_F \).

Some important assumptions were made in this simulink model:

- The bendings, tubes and pipes between \( p_2 \) and the mcv, mcv and \( p_3 \), and between the flow sensor and the mcv are ignored. This could cause some errors, especially at high flow rates.

- All simulation models uses an oil density of 850 kg/m\(^3\) and a bulk modulus of \( 8 \cdot 10^8 Pa \).

- The flow force curves is this case only valid up to 100 l/min. If the is increased any further the deviation may increase.
4.1 Intro

The subject of this chapter has mainly three objectives. Firstly to create a model and establish a suitable connection between the model and a possible optimization algorithm. Secondly which design parameters to optimize is evaluated. Finally an optimization routines with suitable cost functions and design parameters are executed. The results were used to create an insight of how these design parameters affect the performance.
4.2 Optimization model

To create a suitable model to connect with the algorithm some measures were needed to be carried out. This will involve shrinking and making the simulation model quick enough. By quick enough, it means that the model should be able to simulate the given sequence within such period of time that the time on the optimization routine is kept within reasonable limits. Since the vertical pipe handling system is very complex and has many components, it was necessary to shrink the model.

The pipe handler consists of two main part, the bridge crane and the lower guiding arm. Since a model for the overcenter valve used in the bridge crane was verified (chap. 3), it was beneficial to use parts of the bridge crane. The bridge travel drive line was chosen. This drive line consists of a hydraulic part with servo valve, overcenter valve, two motors, and a mechanical part with inertia and friction (fig 4.1).
The model (fig 4.1) was modeled in Matlab Simulink as a time domain model. Using Matlab made it convenient to apply the optimization routine. By implementing the optimization routine in scripts and commands, the model could easily be executed using existing commands in the Matlab program.
CHAPTER 4. OPTIMIZATION OF VPHS

Another parameter which also have a large influence on the time consume is the simulated time. The velocity reference for this drive line last for 13 seconds. This was shrunk to a simulation time of 3 seconds. To stay conservative the velocity was ramped four times faster than the original reference to a velocity of $400\text{mm/s}$ (fig 4.2).

![Figure 4.2: Original and new velocity reference](image)

4.3 Design variables

The components that are focused on is mainly the over center valve, the directional servo valve and the controller.

From these components some specific parameters were chosen (table 4.1).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k_v$</td>
<td>Feed forward velocity gain</td>
</tr>
<tr>
<td>$k_p$</td>
<td>Position error proportional gain</td>
</tr>
<tr>
<td>$k_i$</td>
<td>Position error integrator gain</td>
</tr>
<tr>
<td>$k_{vp}$</td>
<td>Velocity error proportional gain</td>
</tr>
<tr>
<td>$\omega_{pDV}$</td>
<td>Natural frequency of the proportional directional valve spool</td>
</tr>
<tr>
<td>$k_s$</td>
<td>Spring stiffness in motion control valve</td>
</tr>
<tr>
<td>$p$</td>
<td>Pilot ratio in motion control valve</td>
</tr>
</tbody>
</table>

Table 4.1: Design parameters
4.4 Design criteria

In this optimization it has been focused on positioning error and vibrations. To weight the position, the squared position and velocity error was time integrated. The integrated values were scaled such that they had about the same weight (eq 4.1).

\[ C_{pos} = 50 \cdot \int e_{pos}^2 dt + \int e_{vel}^2 dt \]  

(4.1)

To weight the presence of noise and vibrations, the pressure on the inlet side of the motor was evaluated. A second order high pass filter was used on the pressure data to be able to measure the high frequency vibrations (fig 4.3). The high frequent

![Figure 4.3: Second order high pass filter](image)

signal noise is let through and the smooth signals are neglected (fig 4.4)
CHAPTER 4. OPTIMIZATION OF VPHS

Figure 4.4: Example of a signal with and without the high pass filter.

The noise/vibration data were then integrated over time to obtain one scalar value (eq 4.2). This value represents the cost in terms of vibrations.

\[ C_{vib} = 3 \cdot 10^{-8} \cdot \int p_{\text{high}}^2 dt \]  

(4.2)

Where \( p_{\text{high}} \) is the high pass filtered inlet pressure data.
4.5 The complex optimization algorithm

The complex optimization algorithm is a numerical and heuristic method. The algorithm is based on a population consisting of \( n \) designs. The designs are randomly chosen from between the boundaries for the given variables. In each iteration the poorest design is identified, \( j \), and the centroid of the remaining design is computed, \( y^c \).\(^4\) The poorest design is the design that gives the highest cost due to the chosen cost function and centroid is calculated as a mean value of the randomly chosen parameter population.

\[
y^c = \frac{\sum_{i \neq j} y^i}{n-1} \tag{4.3}
\]

The worst design, \( j \), is then mirrored over the centroid.

\[
y^{j,\text{new}} = 1.3 \cdot (y^c - y^j) + y^c \tag{4.4}
\]

Figure 4.5: Population and centroid \(^4\)

Figure 4.6: Worst design mirrored over the centroid \(^4\)
If the newly mirrored design continues to be the worst design, the design parameters are moved toward the best design. How strongly it should be moved is dependent of how many times this design has been the worst in a row.

\[ y_{j,\text{new}} = 0.5 \cdot |y^j + \epsilon \cdot y^c + (1 + \epsilon) \cdot y^k| \]  

(4.5)

\[ \epsilon = \frac{n_0}{n_0 + n_{\text{rep}} - 1} \]  

(4.6)

\( y^k \) = Best design  
\( y^j \) = Worst design  
\( y^c \) = Centroid design  
\( n_0 \) = Tuning parameter, normally 4 or 5  
\( n_{\text{rep}} \) = Number of iterations in a row where design \#j has been the worst
4.5.1 Optimization result

The optimization of the system is divided into three main sections. First the controller parameters are evaluated dependent on different load cases and friction sizes. Secondly the response of the servo valve, and thirdly the parameters in the motion control valve are evaluated.

4.5.2 The controller

Initially the $K_v$ parameter was optimized. $K_v$ is the feed forward velocity gain (fig 4.7). This gain will be dependent on the specific load case. The load case in this model will be the friction force and the inertia. The inertia is based on a total weight of 23ton the additional maximum load capacity of the crane is 15ton. The $K_v$ parameter was optimized for 15tons added load 7.5tons and no load (0ton). The three load cases are referred to as 100% 50% and 0% of the maximum capacity.

![Figure 4.7: Block diagram of the controller](image)

The three load cases resulted in three different $K_v$, but with a linear spacing (fig 4.8). The three obtained parameters were 0.00025, 0.00026, 0.00027. The parameter tend to increase linear with the load (fig 4.8).
The optimization was performed on the other parameters in the controller ($K_p$, $K_i$, fig 4.7). The cost function used was only the $C_{pos}$ to see how good accuracy was possible. The result of this has a clear potential for improvement and resulted in a relatively high position and velocity reference error (fig fig:opt5). Because of this a controller modification was performed followed by a parameter optimization.
CHAPTER 4. OPTIMIZATION OF VPHS

![Modified controller diagram](image)

Figure 4.9: Modified controller

The modified (fig 4.9) has a proportional gain on the velocity, $K_{vp}$. The result of adding this parameter was fundamental and reduced the cost function, $C_{pos}$, with two-thirds of the original error.

$$K_v, K_p, K_i, K_{vp}, C_{pos}, \text{eq 4.1}, \text{Max pos error}$$

<table>
<thead>
<tr>
<th>Load</th>
<th>$K_v$</th>
<th>$K_p$</th>
<th>$K_i$</th>
<th>$K_{vp}$</th>
<th>$C_{pos}$, eq 4.1</th>
<th>Max pos error</th>
</tr>
</thead>
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<tr>
<td>0% load</td>
<td>0.00025</td>
<td>0.016</td>
<td>0</td>
<td>NA</td>
<td>1869</td>
<td>6.1mm</td>
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<tr>
<td></td>
<td>0.00025</td>
<td>0.0139</td>
<td>0.0048</td>
<td>0.000757</td>
<td>622</td>
<td>2.4mm</td>
</tr>
<tr>
<td>50% load</td>
<td>0.00026</td>
<td>0.0072</td>
<td>0</td>
<td>NA</td>
<td>3288</td>
<td>10.1mm</td>
</tr>
<tr>
<td></td>
<td>0.00026</td>
<td>0.0157</td>
<td>0.0085</td>
<td>0.000907</td>
<td>640</td>
<td>3.0mm</td>
</tr>
<tr>
<td>100% load</td>
<td>0.00027</td>
<td>0.0077</td>
<td>0.0026</td>
<td>NA</td>
<td>4674</td>
<td>12.2mm</td>
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<tr>
<td></td>
<td>0.00027</td>
<td>0.0186</td>
<td>0.0087</td>
<td>0.0020</td>
<td>672</td>
<td>3.3mm</td>
</tr>
</tbody>
</table>

Table 4.2: Optimized position parameters, for different load cases

A graphically comparison of the two optimized controllers is shown in figure 4.10. On the left the regular controller is used, and on the right the modified controller with a velocity error proportional gain is implemented. In the bottom of this figure there is two plots of the integrated error. These errors refers to the cost functions, equation 4.1 and 4.2. From these two plots one can easily see that the down side of using a proportional velocity error gain is an increase of high frequent noise in the oil (fig 4.11). The advantage is the improved accuracy which is revealed in the integrated position error (fig 4.10).
CHAPTER 4. OPTIMIZATION OF VPHS

Figure 4.10: Comparison of position and velocity error with (right side) and without (left side) a controller with proportional velocity error gain.

Figure 4.11: Comparison of the pressures with (right side) and without (left side) a controller with proportional velocity error gain.

By looking at the integrated position error one understand that the position are improving with the modified controller. To compare with the actual error and not the generated error by the defined cost function one can look at the figure 4.12. The figure show the maximum positioning error during the simulation period. The same parameters as in table 4.2 are use to generate the results.
To look at the effect of increased friction a viscous friction dependent on velocity was added. The friction is modeled as a rotational damper coupled to the output shaft of the motor. The results were compared with 4 different damper coefficients, $C_d$: $0 Nm/\text{rad/s}$, $0.01 Nm/\text{rad/s}$, $0.1 Nm/\text{rad/s}$, and $1 Nm/\text{rad/s}$. To get an image of the size of this friction the added friction moment is compared with the existing (fig 4.13).
Figure 4.13: Friction moment during the simulation. The results are simulated with the parameters from table 4.3

The parameter optimization was performed with a load case of 7500 kg and with the cost function dependent on position, $C_{pos}$ (eq 4.1).

<table>
<thead>
<tr>
<th>Case</th>
<th>$C_d$</th>
<th>$K_v$</th>
<th>$K_p$</th>
<th>$K_i$</th>
<th>$C_{vib}$, eq 4.2</th>
<th>$C_{pos}$, eq 4.1</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0</td>
<td>0.00026</td>
<td>0.0072</td>
<td>0</td>
<td>373</td>
<td>3288</td>
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<tr>
<td>2</td>
<td>0.01</td>
<td>0.000265</td>
<td>0.0083</td>
<td>0.0057</td>
<td>1097</td>
<td>2230</td>
</tr>
<tr>
<td>3</td>
<td>0.1</td>
<td>0.000309</td>
<td>0.0086</td>
<td>0.0153</td>
<td>659</td>
<td>2122</td>
</tr>
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<td>4</td>
<td>1</td>
<td>0.000820</td>
<td>0.0264</td>
<td>0</td>
<td>642</td>
<td>1946</td>
</tr>
</tbody>
</table>

Table 4.3: Optimized position parameters for different friction coefficients
4.5.3 The servo valve parameters

Because of the observed spool position error in the servo valve at high frequent changes in the spool position reference (fig 4.14), there is a reason to believe that the spool response frequency is affecting the position error.

The spool frequency response test was executed by simulate the system with a frequency increasing from $50 \text{rad/sec}$ to $200 \text{rad/sec}$. This was performed on the three different load cases (4.2) with a regular controller (no $K_{vp}$).

The test revealed that particularly at low load cases (0kg to 7500kg) an increased response frequency of the spool will improve the overall position error (4.15). For example one can see that for an increased spool frequency response from $50 \text{rad/sec}$ to $75 \text{rad/sec}$ the accuracy increases with 23% (Load: 7500kg fig 4.15b).
CHAPTER 4. OPTIMIZATION OF VPHS

(a) Cost function error

(b) Position error

Figure 4.15: Results of spool response test.
4.5.4 The motion control valve parameters

To finally explore the effect of changing the pilot ratio and the spring stiffness of the spring in the motion control valve, a test with base from case 3 in table 4.3 was executed. In this test an optimization of the parameters \( P \) and \( K_s \) was performed. The optimization routine was conducted with 3 different cost functions. The three functions were based on the two cost functions in equation 4.1 and 4.2.

\[
C_1 = C_{\text{pos}} \\
C_2 = C_{\text{vib}} \\
C_3 = C_{\text{pos}} + C_{\text{vib}}
\]

This resulted in three different combinations of \( P \) and \( K_s \) (fig 4.16. The result shows that it is particularly important to include the position error/cost in the cost function for the optimization algorithm. If one compare the results for the optimization with cost function \( C_1 \) versus the \( C_2 \), it is clearly shown that using a cost function only dependent of noise can be very misleading. The vibration cost function, \( C_{\text{vib}} \), is reduced to 198, but the position cost function is increased to over 10000. The \( C_{\text{vib}} \) is lowered to a minimum of 198 which is over 50% lower than for the cost function \( C_1 \). But since the position is out of bounds this result is not acceptable. What can be seen when the cost function \( C_3 \) is used is that both the \( C_{\text{vib}} \) and the \( C_{\text{pos}} \) is kept at a low level (table 4.4).
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If one compares the base design which is case 3 (table 4.3) with the new design, one can see that the original design had a $C_{vib} = 659$ and a $C_{pos} = 2122$, while the new design with cost function $C_3$ has $C_{vib} = 219$ and $C_{pos} = 2035$.

<table>
<thead>
<tr>
<th>Cost function</th>
<th>$P$</th>
<th>$K_s$</th>
<th>$C_{vib}$</th>
<th>$C_{pos}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>None</td>
<td>2.8</td>
<td>895</td>
<td>659</td>
<td>2122</td>
</tr>
<tr>
<td>$C_1$</td>
<td>3.0</td>
<td>868</td>
<td>322</td>
<td>1974</td>
</tr>
<tr>
<td>$C_2$</td>
<td>7.2</td>
<td>673</td>
<td>198</td>
<td>10353</td>
</tr>
<tr>
<td>$C_3$</td>
<td>3.4</td>
<td>855</td>
<td>219</td>
<td>2035</td>
</tr>
</tbody>
</table>

Table 4.4: Parameters obtained in optimization

Figure 4.16: Optimized design of pilot ratio and spring stiffness.
Note: the bars for the cost function, $C_{vib}$ continues to a cost of 10353 and 10551.
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You see from table 4.4 and figure 4.16 that both results with cost function $C_1$ and $C_2$ give an improved result in terms of high frequent vibrations (fig 4.17).

Figure 4.17: The effect of vibration reduction in the inlet pressure on the motor.
4.6 Sub-conclusions

Through this experiment it is shown that the accuracy (position error) is highly dependent on the controller parameters, and that the optimal controller parameters are dependent on the load case in form of inertia or friction. These discoveries points out a need for more a advanced controller. An alternative could be a controller with gain scheduling, where the gain is dependent on one or more observed variables. In this case the load could be this observed variable. If this is necessary or not is of coarse dependent on the necessity for high accuracy, or in other word the highest possible accuracy.

It was also shown that increasing the frequency response of the servo valve with 25% (from 52rad/sec to 75rad/sec) will increase the accuracy with about the same percentage. From this examination it was also revealed that increasing the frequency response above 100rad/sec would actually not improve the accuracy significantly. This means in a larger picture that it is not always benefitial to buy a more expensive and faster valve because it does not guarantee the system will increase its accuracy compared with the cost of upgrading the valve.

The regular controller of the existing system has a feed forward velocity reference and a PI controller acting on the position. A small modification of this controller revealed that adding a proportional velocity gain to the compensator can increase your accuracy with about 70%. It does assume that the velocity sensors has high resolution and is able to give a smooth signal to the controller. If this is possible it will be a very sheep and simple way to improve accuracy. A small downside of adding this term was a slight increase of noise in the system.

The parameter optimization of the motion control valve demonstrated that small adjustments in pilot ratio and spring stiffness will decrease the presence of noise and improve the accuracy slightly.
Conclusion

In this project a complete simulation model of the VPHS, containing the most important functionalities, has been developed. The complexity and simulation time is kept low by modeling the 3D machinery as several one dimensional sub systems. The components are built separately as modules and this makes it convenient to switch or change one single component without changing the complete model.

The motion control valves are identified as critical components and it is therefore important to use accurate models of these. To ensure an accurate model some experimental work was performed. This work revealed the importance of implementing flow forces to the model. The experimental work also verified the spool response, though with a low accuracy.

A model of the bridge travel drive line was customized for optimization purpose. Optimization with the so-called Complex algorithm and parameter variation was performed. This revealed opportunities and changes that could improve the accuracy of the pipe handler. The greatest opportunity for improvement lies in the controller. Implementing a velocity feedback and a proportional controller could increase the accuracy with roughly 70%. The current system only has a classical PI controller with a feedforward velocity gain. The optimization revealed that the optimal parameters change dependent on the load case. This implies that having
a classical controller with constant variables is not ideal in terms of accuracy. An alternative to the current constants could be to implement a gain scheduling. In this case the accuracy will improve without changing the controller states.

Parameter variation was performed on the response frequency of the directional servo valve. The current valve used on the bridge travel has a frequency of 8.3Hz. The parameter variation showed that an increase of the frequency will increase the accuracy until the frequency has reached 15Hz. Increasing the frequency above 16Hz gave negligible or small improvement in accuracy. For example, if the frequency response is increased from 8Hz to 12Hz the tool point accuracy increases with 23% and to 16Hz it increases with 35%, but from 8Hz to 20Hz the accuracy only increases with just 39% (data obtained from fig 4.15b load:7500kg). The figure 4.15b reveals that increasing the frequency above 16Hz has small impact on the toolpoint accuracy.

In this project the different components have been verified through experimental tests and/or with values and properties described in datasheets. The motion control valve VAA-B-SICN-ST-VF250, used in several operations on the bridge crane is verified through an experimental test. The experimental test was used to adapt and verify the simulation model. This resulted in a simulation model with high accuracy in terms crack pressure, spool opening and response. The different components were assembled to create the BC and LGA simulation model. With some experimental test results these models could be verified to obtain the desired accuracy. The models are proven to be used for optimization in terms of controller parameters, valve responses and motion control valve parameters.

The simulation model is modular. The different types of modules include motors, motion control valves, directional valves, inertias and friction forces. The advantage is that the different modules can be reused to create other systems containing the same components. In the future one could imagine that a library of accurate simulation sub models is established. Accurate simulation components give an opportunity to adjust controllers and components in a system to obtain the best possible result before physical testing. Since physical testing is a huge expense for the companies results from realistic simulation models are desired.
Bibliography


Experimental test

A.1 intro

To verify the simulation model, a full scale test is done. This is done on a test rigg in Kristiansand, with help from Morten Bak. First of all we had to choose measurement points that easily could be connected to the simulation model.

A.2 Measurement points

The vertical pipe handler system has already some measured signals that are used by the control system. These are signals like position and velocities of hydraulic cylinders and motors. These signals are relatively easy to observe, but to verify the model properly I need some additional measurepoints.

These additional points are in the hydraulic system and can be sorted in two categories:

1. Pressure on each side of the motors and cylinders.
   For example should one pressuretransmitter be placed between 6a and 6b, in fig A.1. This pressure is important to log, because it says how much force
that is subjected to the motor. In this way I could use the data to see how much force that disappear in friction and energy losses, by comparing to the real accelerations of the trolley.

2. Pressure on each port between motion control valve and the directional valve.

These pressures are important when tuning the parameters in the simulated motion control valve. These pressures are also useful when the oil stiffness is determined.
A.3 Test procedure

This document is a procedure for experimental testing of the VPHS. The testing is a quantitative test with the purpose to measure and record data describing system behaviour that can be used to validate design calculations and simulation models.

A.3.1 Test Setup

In order to properly validate design calculations or simulation models of the crane, it is necessary to obtain measured data from the actual crane when performing operations identical to the ones from the calculations or simulations. More specifically three types of signals must be measured:

1. Input variables: control signals to hydraulic valves, and external loads (could be wind, or rigg axelerations)

2. State variables: hydraulic pressure, state signals from hydraulic valves, positions of actuators and moving parts.

3. Output variables: positions/velocities of controlled machine components. As in this case these signals are often also included in the state variables and here they are the signals from the various rotary encoders and position sensors.
**APPENDIX A. EXPERIMENTAL TEST**

**Measure Points**

The measure points on the bridge crane are described in the table below and in the appendix B.

<table>
<thead>
<tr>
<th>MP</th>
<th>Signal</th>
<th>Description</th>
<th>Type</th>
<th>Unit</th>
<th>Measure Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>pS</td>
<td>Supply pressure</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>pA_BTM</td>
<td>A-port pressure, bridge travel motor</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>pB_BTM</td>
<td>B-port pressure, bridge travel motor</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>pA_BTC</td>
<td>A-port pressure, bridge travel control valve</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>pB_BTC</td>
<td>B-port pressure, bridge travel control valve</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>pA_TTM</td>
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<tr>
<td>7</td>
<td>pB_TTM</td>
<td>B-port pressure, trolley travel motor</td>
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<tr>
<td>8</td>
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<tr>
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<tr>
<td>10</td>
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<td>State</td>
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<td>Bar or MPa</td>
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<tr>
<td>14a</td>
<td>s_BTM</td>
<td>Position, bridge travel motor</td>
<td>State</td>
<td>rad</td>
<td></td>
</tr>
<tr>
<td>14b</td>
<td>v_BTM</td>
<td>Velocity, bridge travel motor</td>
<td>State</td>
<td>rad/sec</td>
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</tr>
<tr>
<td>15a</td>
<td>u_BTV</td>
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<td>Input</td>
<td>%</td>
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<tr>
<td>15b</td>
<td>s_BTV</td>
<td>Position, bridge travel control valve</td>
<td>State</td>
<td>%</td>
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<tr>
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<td>State</td>
<td>rad</td>
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<td>v_TTM</td>
<td>Velocity, trolley travel motor</td>
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<td>rad/sec</td>
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<td>u_TTV</td>
<td>Command signal, bridge travel control valve</td>
<td>Input</td>
<td>%</td>
<td></td>
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<tr>
<td>17b</td>
<td>s_TTV</td>
<td>Position, bridge travel control valve</td>
<td>State</td>
<td>%</td>
<td></td>
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<tr>
<td>18a</td>
<td>s_SM</td>
<td>Position, slewing motor</td>
<td>State</td>
<td>rad</td>
<td></td>
</tr>
<tr>
<td>18b</td>
<td>v_SM</td>
<td>Velocity, slewing motor</td>
<td>State</td>
<td>rad/sec</td>
<td></td>
</tr>
<tr>
<td>19a</td>
<td>u_SV</td>
<td>Command signal, slewing control valve</td>
<td>Input</td>
<td>%</td>
<td></td>
</tr>
<tr>
<td>19b</td>
<td>s_SV</td>
<td>Position, slewing control valve</td>
<td>State</td>
<td>%</td>
<td></td>
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Table A.1: Measure points, bridge crane
APPENDIX A. EXPERIMENTAL TEST

For the lower guiding arm the logged states are:

<table>
<thead>
<tr>
<th>MP</th>
<th>Signal</th>
<th>Description</th>
<th>Type</th>
<th>Unit</th>
<th>Mes. Unit</th>
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<td>Bar or MPa</td>
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<tr>
<td>21</td>
<td>pA_LBTM</td>
<td>A-port pressure, bridge travel motor LGA</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
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<tr>
<td>22</td>
<td>pB_LBTM</td>
<td>B-port pressure, bridge travel motor LGA</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
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<tr>
<td>23</td>
<td>pA_LBTC</td>
<td>A-port pressure, bridge travel control valve LGA</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
</tr>
<tr>
<td>24</td>
<td>pB_LBTC</td>
<td>B-port pressure, bridge travel control valve LGA</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
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<tr>
<td>25</td>
<td>pA_LSM</td>
<td>A-port pressure, slewing motor LGA</td>
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<tr>
<td>26</td>
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<td></td>
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<tr>
<td>27</td>
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<td>Bar or MPa</td>
<td></td>
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<tr>
<td>28</td>
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<td></td>
</tr>
<tr>
<td>29</td>
<td>pA_LJTC</td>
<td>A-port pressure, jib tilt cylinder LGA</td>
<td>State</td>
<td>Bar or MPa</td>
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<tr>
<td>30</td>
<td>pB_LJTC</td>
<td>B-port pressure, jib tilt cylinder LGA</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
</tr>
<tr>
<td>31</td>
<td>pA_LTC</td>
<td>A-port pressure, telescope control valve LGA</td>
<td>State</td>
<td>Bar or MPa</td>
<td></td>
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<tr>
<td>32</td>
<td>pB_LTC</td>
<td>B-port pressure, telescope control valve LGA</td>
<td>State</td>
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<td></td>
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<tr>
<td>33</td>
<td>pR_JTC</td>
<td>Rod-side pressure, jib tilt cylinder LGA</td>
<td>State</td>
<td>Bar or MPa</td>
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</tr>
<tr>
<td>34</td>
<td>pP_JTC</td>
<td>Piston-side pressure, jib tilt cylinder LGA</td>
<td>State</td>
<td>Bar or MPa</td>
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<tr>
<td>35</td>
<td>pR_TC</td>
<td>Rod-side pressure, telescope cylinder LGA</td>
<td>Input</td>
<td>Bar or MPa</td>
<td></td>
</tr>
<tr>
<td>36</td>
<td>pP_TC</td>
<td>Piston-side pressure, telescope cylinder LGA</td>
<td>Input</td>
<td>Bar or MPa</td>
<td></td>
</tr>
<tr>
<td>37</td>
<td>v_LBTM</td>
<td>Position, bridge travel motor LGA</td>
<td>State</td>
<td>rad</td>
<td></td>
</tr>
<tr>
<td>38</td>
<td>u_LBTV</td>
<td>Command signal, bridge travel control valve</td>
<td>Input</td>
<td>%</td>
<td></td>
</tr>
<tr>
<td>39</td>
<td>v_LSM</td>
<td>Velocity, slewing motor LGA</td>
<td>State</td>
<td>rad/sec</td>
<td></td>
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<tr>
<td>40</td>
<td>u_LJTV</td>
<td>Position, slewing motor</td>
<td>State</td>
<td>rad</td>
<td></td>
</tr>
<tr>
<td>41</td>
<td>u_LTV</td>
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<td>Input</td>
<td>%</td>
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</tr>
<tr>
<td>42</td>
<td>u_LSV</td>
<td>Command signal, slewing control valve</td>
<td>Input</td>
<td>%</td>
<td></td>
</tr>
<tr>
<td>43</td>
<td>s_JTC</td>
<td>Position, jib tilt cylinder</td>
<td>State</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td>44</td>
<td>s_TC</td>
<td>Position, telescope cylinder</td>
<td>State</td>
<td>m</td>
<td></td>
</tr>
</tbody>
</table>

Table A.2: Measure points, lower guiding arm
This test was canceled by aker 21.02.2012. The test will probably be completed at a later stage.
Measurement points, Bridge crane
Measurement points, Lower guiding arm
Functions, $\theta_1$ and $\theta_3$

From equation 2.31 and 2.33 this expression is solved for $\theta_1$, $f_1(d_1)$:

$$\theta_1 = -\log\left(d_1^2 \cdot \left(\frac{2191}{761992555} - \frac{34 \cdot i}{761992555}\right)\right) + \sqrt{\left(\frac{87247290729882095616}{14515816346885700625} + \frac{d_1^4 \cdot \left(\frac{4684881}{14515816346885700625} - \frac{297976 \cdot i}{51690222243972}\right)}{2}\right)^2 - 5549254869553217536 \cdot i} \cdot \frac{1}{2} - \frac{6043551423 + 187568004 \cdot i}{761992555} \cdot i \tag{D.1}$$

Expression for $\theta_3$, $f_3(d_3)$:

$$\theta_3 = -\log\left(d_3^2 \cdot \left(\frac{47i}{29407824} + \frac{193}{73519560} + \frac{21153577395728}{3127966263075} + \frac{9071i}{3473}\right) + \left(\frac{270256285129680}{798302426i} + \frac{200189840836800}{152822419}\right) + \frac{d_3^2 \cdot \left(-\frac{16891017820605}{221000979621824i} \cdot 0.5 + \frac{6255932526150}{16985158} - \frac{2068141i}{1837989}\right)}{2} \cdot i \cdot \frac{1}{2} - \frac{9189945}{1837989} \cdot i \right) \tag{D.2}$$
APPENDIX D. FUNCTIONS, $\theta_1$ AND $\theta_3$
Valve, Technical data
Servo solenoid valves with positive overlap and on-board electronics

Type 4WRLE 10...35, symbols E./W.

Nominal size 10, 16, 25, 35
Unit series 3X
Maximum working pressure P, A, B 350 bar, T 250 bar
Nominal flow rate 50...1,100 l/min ($\Delta p$, 10 bar)

### Overview of contents

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</tr>
</thead>
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<td>5 and 6</td>
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<td>11 to 15</td>
</tr>
<tr>
<td>Unit dimensions</td>
<td>16 to 19</td>
</tr>
<tr>
<td>Mounting hole configurations</td>
<td>20 and 21</td>
</tr>
</tbody>
</table>

### Features

- Pilot operated servo solenoid valves NG10 to NG35 with positive overlap, see symbols E./W. and characteristic curves
- Pilot valve NG6, with control piston and sleeve in servo quality
- Actuated on one side, 4/4 fail-safe position when switched off
- Control solenoid with integral position feedback and on-board valve electronics (OBE), calibrated at the factory
- Main stage with approx. 20% overlap and position feedback
- Electronically compensated, calibrated overlap, see characteristic curve range ±0.5 V
- Spool with linear travel, with anti-rotation element
- Flow characteristic
  - S = Progressive
  - NG16 and 25 with load tap C1/C2
- Suitable for electrohydraulic controllers in production systems with more demanding requirements
- Subplates as per catalog section, NG10 RE 45055, NG16 RE 45057, NG25 RE 45059 and NG32 RE 45060 (order separately)
- Plug-in connectors to DIN 43563-AM6, see catalog section RE 08008 (order separately)

### Variants on request

- For standard applications
- Special symbols and characteristic curves with/without intermediate plates
Ordering data and scope of delivery

With on-board trigger electronics = E

Nominal size 10 = 10
Nominal size 16 = 16
Nominal size 25 = 25
Nominal size 35

Symbols = E, E1

With symbol E1, E1(Z), E4, W1(Z), W4:
P → A: q₁, B → T: q₂/2
P → B: q₂/2, A → T: q₁

Further information in plain text
M = NBR seals, suitable for mineral oils (HL, HLP) to DIN 51524

Interface for trigger electronics
A1 = Setpoint input ±10 V

Electrical connection
K0 = without plug-in connector, with plug to DIN 43663-AM6
Order plug-in connector separately

Control oil supply “x”, control oil outlet “y”
No code = “x” = external, “y” = external
E = “x” = internal, “y” = external
ET = “x” = internal, “y” = internal
T = “x” = external, “y” = internal

Voltage supply of trigger electronics
G24 = +24 V DC

H = Highflow version (on request)
3X = Unit series 30 to 39
J = Overlap compensation signal
S = See characteristic curve range: ±0.5 V

Flow characteristic
Progressive

Nominal flow rate at 10 bar valve pressure difference
10 = 50 or 85 l/min
16 = 180 l/min
25 = 350 or 430 l/min
35 = 1,100 l/min

With load tap C1/C2

1) NG35 is a high flow version of the NG32, ports P, A, B and T have Ø50 mm in the main stage.
Contrary to the standard, ports P, A, B and T may be drilled to max. Ø48 mm in the control block.
These valves therefore provide higher flow rates q₁: q₂.
### Preferred types (available at short notice)

<table>
<thead>
<tr>
<th>Type 4WRLE</th>
<th>Material No.</th>
</tr>
</thead>
<tbody>
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<td>E, E1, E4, W, W1, W4</td>
<td>NG10</td>
</tr>
<tr>
<td>4WRLE10E–80SJ–3X/G24KO/A1M</td>
<td>0 811 404 700</td>
</tr>
<tr>
<td>4WRLE10E–80SJ–3X/G24ETKO/A1M</td>
<td>0 811 404 713</td>
</tr>
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<td>4WRLE10E4–80SJ–3X/G24KO/A1M</td>
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<td>4WRLE10W–50SJ–3X/G24ETKO/A1M</td>
<td>0 811 404 704</td>
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<td>4WRLE16W4–180SJ–3X/G24ETKO/A1M</td>
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<tr>
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<td>4WRLE16W4–180SJ–3X/G24ETKO/A1M</td>
<td>0 811 404 328</td>
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<table>
<thead>
<tr>
<th>Type 4WRLE</th>
<th>Material No.</th>
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<tbody>
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<td>E (Z), E1 (Z), E4, W (Z), W1 (Z), W4</td>
<td>NG16</td>
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<td>4WRLE25EZ–350SJ–3X/G24KO/A1M</td>
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</tr>
<tr>
<td>4WRLE25EZ–350SJ–3X/G24TKO/A1M</td>
<td>0 811 404 466</td>
</tr>
<tr>
<td>4WRLE25EZ–350SJ–3X/G24ETKO/A1M</td>
<td>0 811 404 481</td>
</tr>
<tr>
<td>4WRLE25E1Z–350SJ–3X/G24KO/A1M</td>
<td>0 811 404 455</td>
</tr>
<tr>
<td>4WRLE25E4–350SJ–3X/G24KO/A1M</td>
<td>0 811 404 459</td>
</tr>
<tr>
<td>4WRLE25WZ–350SJ–3X/G24KO/A1M</td>
<td>0 811 404 456</td>
</tr>
<tr>
<td>4WRLE25W1Z–350SJ–3X/G24ETKO/A1M</td>
<td>0 811 404 476</td>
</tr>
<tr>
<td>4WRLE25W1Z–350SJ–3X/G24KO/A1M</td>
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</tr>
<tr>
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<td>0 811 404 471</td>
</tr>
<tr>
<td>4WRLE25W4–350SJ–3X/G24KO/A1M</td>
<td>0 811 404 472</td>
</tr>
<tr>
<td>W</td>
<td>NG35</td>
</tr>
<tr>
<td>4WRLE35W–1100SJ–3X/G24KO/A1M</td>
<td>0 811 404 504</td>
</tr>
</tbody>
</table>

### Function, sectional diagram

**Servo solenoid valve 4WRLE 10...35**

![Diagram of the servo solenoid valve 4WRLE 10...35](image)

- **Main stage**
- **Position transducer**
- **Pilot valve**

See page 4
## Accessories, not included in scope of delivery

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Fastening screws</td>
<td>NG10</td>
<td>4 x M6 x 40, DIN 912-10.9</td>
</tr>
<tr>
<td></td>
<td>NG16</td>
<td>2 x M6 x 45, DIN 912-10.9</td>
</tr>
<tr>
<td></td>
<td></td>
<td>4 x M10 x 50, DIN 912-10.9</td>
</tr>
<tr>
<td></td>
<td>NG25</td>
<td>6 x M12 x 60, DIN 912-10.9</td>
</tr>
<tr>
<td></td>
<td>NG35</td>
<td>6 x M20 x 90, DIN 912-10.9</td>
</tr>
<tr>
<td>Plug-in connectors 6P+PE, see also RE 06008</td>
<td>KS</td>
<td>1834482022</td>
</tr>
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<td></td>
<td>KS</td>
<td>1834482026</td>
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<td></td>
<td>MS</td>
<td>1834482023</td>
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<tr>
<td></td>
<td>KS 90°*</td>
<td>1834484252</td>
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</table>

## Testing and service equipment

- Test box type VT-PE.TB3, see RE 30065
- Test adapter 6P+PE type VT-PA-2, see RE 30068

## Control oil supply

### NG16

#### Symbol in detail

- **Pilot valve**
- **Main valve**

#### Conversion

The pilot valve can be supplied with oil both via ports X and Y (external) and from the main flow ducts P and T.

In the basic version, the valve is equipped with the plugs (1) and (2), i.e. X and Y are external.

For valve versions with X and/or Y as internal, see ordering overview or carry out the conversion (see diagram above).

When the control oil supply or outlet is changed, the part number must also be changed.

### NG10, 25, 35

#### Plug

1. NG10...25 1 813 464 007 SW 3
2. NG35 1 813 464 001 SW 4

#### Type ...-3X ...

- **A**
- **B**
- **P**
- **T**
- **Y**

#### Type ...-3X ... E ...

#### Type ...-3X ... ET ...

#### Type ...-3X ... T ...

**No code**

- **E** = "x" = internal, "y" = external
- **ET** = "x" = internal, "y" = internal
- **T** = "x" = external, "y" = internal
Symbols in mid position “E”.. or “W”..

Spool valves with overlap
With symbol “E”, leakage oil in the two work chambers A and B of the control piston results in a build-up of pressure in A or B, which then causes a connecting cylinder to drift out of position. In many cases, the “W” symbol is a better solution. With a setpoint of “0”, the control piston moves into the overlapped mid position.
In this mid position, pressure is then relieved from ports A and B with small openings to T.
This also supports the function of external check valves.

Flow in mid position
“leakage pressure relief”

\[ Q = f(\Delta s) \]
\[ 0 \ldots \pm 25 \% \]

\[ Q_s = Q_{\text{nom}} \cdot \sqrt{\frac{\Delta P}{5 \text{ bar}}} \]
Load tap C1/C2

To compensate for fluctuations in the load or supply pressure, proportional valves are combined with pressure compensators. The load is tapped through a shuttle valve for the NG10 and 35, and through two additional ports C1 and C2 for NG16 and 25 ("4WRL" and "4WRL" only).

The pressure compensator therefore always receives the correct pressure signal even in the event of negative load. When using pressure compensators, external control oil supply should always be selected.

Asymmetrical valve spool $Q_A : Q_B = 2:1$

The two throttle cross-sections of proportional directional control valves are usually symmetrical. In order to adapt to differential cylinders with different with asymmetrical metering notches are available. A comparison of the flow rates can be found in the product range overview "Preferred types, characteristic curves".

Valve spools in a differential circuit

In order to produce differential circuits, valve spools with an additional "4th position" are available (see diagram). It is sufficient to install a check valve in the consumer lines. In addition, a symbol (spool) with internal B-P connection is employed for certain “branch-oriented solutions”. However, we recommend that you consult the BRH Application Center with regard to these special symbols. As a rule, a simulation or knowledge of this type of system is required.
## Technical data

### General
- **Construction**: Spool type valve, pilot operated
- **Actuation**: Servo solenoid valve NG6, with position controller for pilot valve and main stage
- **Type of mounting**: Subplate, mounting hole configuration NG10...35 (ISO 4401-...)
- **Installation position**: Optional
- **Ambient temperature range**: °C: -20...+50
- **Weight**: kg: NG10 8.7, NG16 10.6, NG25 18.4, NG35 81
- **Vibration resistance, test condition**: max. 25 g, shaken in 3 dimensions (24 h)

### Hydraulic (measured with HLP 46, \(\rho_{oill} = 40^\circ\text{C}\pm5^\circ\text{C}\))
- **Pressure fluid**: Hydraulic oil to DIN 51524...535, other fluids after prior consultation
- **Viscosity range**: recommended mm²/s: 20...100
  - max. permitted mm²/s: 10...800
- **Pressure fluid temperature range**: °C: -20...+70
- **Maximum permissible degree of contamination of pressure fluid**: Class 18/16/13
- **Purity class to ISO 4406 (c)**: See symbol

### Nominal flow at \(\Delta p = 5\) bar per notch

<table>
<thead>
<tr>
<th></th>
<th>NG10</th>
<th>NG16</th>
<th>NG25</th>
<th>NG35</th>
</tr>
</thead>
<tbody>
<tr>
<td>l/min</td>
<td>50, 80</td>
<td>180</td>
<td>350</td>
<td>1,100</td>
</tr>
</tbody>
</table>

### Max. working pressure in P, A, B

<table>
<thead>
<tr>
<th></th>
<th>max. in X (ext.)</th>
<th>280</th>
</tr>
</thead>
<tbody>
<tr>
<td>bar</td>
<td>max. in P (X = int.)</td>
<td>280</td>
</tr>
<tr>
<td></td>
<td>max. in T (Y = ext.)</td>
<td>250</td>
</tr>
<tr>
<td></td>
<td>max. in T (Y = int.)</td>
<td>250</td>
</tr>
<tr>
<td></td>
<td>max. in Y (ext.)</td>
<td>250</td>
</tr>
<tr>
<td></td>
<td>Min. control oil pressure of “pilot stage”</td>
<td>8</td>
</tr>
</tbody>
</table>

### Static/Dynamic
- **Overlap in mid position**: \(\approx 18...22\%\) of spool stroke, electrically adjustable for \(U_{oill} \pm 0.5\) V
- **Spool stroke, main stage ± mm**: 4 \(\pm 7\) \(\pm 10\) \(\pm 12.5\)
- **Control oil volume of main stage 100% cm³**: 1.1 \(\pm 4.3\) \(\pm 11.3\) \(\pm 41.5\)
- **Control oil requirement 0...100%, l/min x = 100 bar**: 2.2 \(\pm 4.7\) \(\pm 11.7\) \(\pm 15.6\)
- **Hysteresis %**: < 0.1, scarcely measurable
- **Manufacturing tolerance %**: <±5 \(Q_{max}\)
- **Response time for 0...100%, ms x = 100 bar**: <40 \(\pm 80\) \(\pm 80\) \(\pm 130\)
- **Response time for 0...100%, ms x = 10 bar**: <150 \(\pm 250\) \(\pm 250\) \(\pm 500\)
- **Switch-off behavior**: After electrical shut-off (pilot valve in “fail-safe”) Main stage moves to spring-centered mid position (Sb “E/W..”)
- **Thermal drift %**: <1 % at \(\Delta T = 40^\circ\text{C}\)
- **Calibration**: At factory ±1 %, see flow curve

### Conformity
- CE EN 61000-6-2
- CE EN 61000-6-3

---

1) The purity classes stated for the components must be complied with in hydraulic systems. Effective filtration prevents problems and also extends the service life of components. For a selection of filters, see catalog sections RE 50070, RE 50076 and RE 50061.

2) Flow rate at a different \(\Delta p\): \(q_r = q_{om} \cdot \sqrt{\frac{\Delta p}{5}}\)
### Technical data

**Electric pilot valve NG6**, valve with on-board electronics

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cyclic duration factor</td>
<td>100</td>
</tr>
<tr>
<td>Degree of protection</td>
<td>IP 65 to DIN 40050 and IEC 14434/5</td>
</tr>
<tr>
<td>Connection</td>
<td>Plug-in connector 6P+PE, DIN 43563</td>
</tr>
<tr>
<td>Power supply</td>
<td>24 V DC</td>
</tr>
<tr>
<td>Terminal A:</td>
<td>min. 21 V DC/max. 40 V DC</td>
</tr>
<tr>
<td>Terminal B:</td>
<td>0 V</td>
</tr>
<tr>
<td>Ripple max. 2 V DC</td>
<td></td>
</tr>
<tr>
<td>Power consumption</td>
<td>Solenoid 45 mm = 40 VA max.</td>
</tr>
<tr>
<td>External fuse</td>
<td>2.5 A</td>
</tr>
<tr>
<td>Input, “Standard” version</td>
<td>Difference amplifier, $R_c = 100$ kΩ</td>
</tr>
<tr>
<td>Terminal D: $U_E$</td>
<td>0 ... ±10 V</td>
</tr>
<tr>
<td>Terminal E:</td>
<td>0 V</td>
</tr>
<tr>
<td>Max. differential input voltage at 0 V</td>
<td>$D \rightarrow B \quad E \rightarrow B \quad$ max. 18 V DC</td>
</tr>
<tr>
<td>Test signal, “Standard” version</td>
<td>LVDT</td>
</tr>
<tr>
<td>Terminal F: $U_{\text{Test}}$</td>
<td>0 ... ±10 V</td>
</tr>
<tr>
<td>Terminal C:</td>
<td>Reference 0 V</td>
</tr>
<tr>
<td>Protective conductor and screen</td>
<td>See pin assignment (installation conforms to CE)</td>
</tr>
<tr>
<td>Recommended cable</td>
<td>See pin assignment</td>
</tr>
<tr>
<td></td>
<td>up to 20 m: $7 \times 0.75$ mm²</td>
</tr>
<tr>
<td></td>
<td>up to 40 m: $7 \times 1$ mm²</td>
</tr>
<tr>
<td>Calibration</td>
<td>Overlap and P~A at +8 V, calibrated at the factory, see valve characteristic curve</td>
</tr>
</tbody>
</table>

### Important

Pilot operated servo solenoid valves with positive overlap perform their function in open or closed-loop-controlled axes and have approx. 20% overlap when switched off. This condition does not constitute an active, safe basic position. For this reason, many applications require the use of “external check valves” or certain sandwich-mounted valves, which must be taken into account during the On/Off switching sequence.
Further testing of the complex algorithm

F.1 Intro

To learn about the complex method and how sensitive it is to the input parameter like population, and boundary conditions, some experimental testing was done. This test was based on the step response of the control directional valve (see section 2.2). This system was chosen because it had few variables and the best solution was relatively easy to find. For each parameter setting the algorithm run hundred times and logged each error value. The error in this case is the deviation between the smallest possible error and the error in each optimization routine.
APPENDIX F. FURTHER TESTING OF THE COMPLEX ALGORITHM

F.2 Results

The run is ran a hundred times and x number of solutions are divided into two groups:

Gr.1: \( ERROR < E_{\text{best}} \pm 0.4\% \)

Gr.2: \( E_{\text{best}} \pm 0.4\% < ERROR < E_{\text{best}} \pm 2.0\% \)

Error value:

\[
E_v = \sum \varepsilon^2 
\]

\[
ERROR = E_v - E_{\text{best}} 
\]

Error function in algorithm:

\[
Err = E_v \cdot K 
\]

\( E_{\text{best}} \): Best/lowest possible error.

\( E_v \): Error value, obtained in each run.

\( ERROR \): Calculated error deviation.

\( Err \): Cost function used in the algorithm.
APPENDIX F. FURTHER TESTING OF THE COMPLEX ALGORITHM

The table below show 17 different test parameter settings. Each parameter design is ran 100 times with the complex algorithm.

<table>
<thead>
<tr>
<th>Test no.</th>
<th>C</th>
<th>K</th>
<th>B</th>
<th>x</th>
<th>y</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3</td>
<td>1</td>
<td>±60%</td>
<td>2</td>
<td>98</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>10</td>
<td>±60%</td>
<td>32</td>
<td>68</td>
</tr>
<tr>
<td>3</td>
<td>3</td>
<td>50</td>
<td>±60%</td>
<td>80</td>
<td>20</td>
</tr>
<tr>
<td>4</td>
<td>3</td>
<td>100</td>
<td>±60%</td>
<td>89</td>
<td>11</td>
</tr>
<tr>
<td>5</td>
<td>3</td>
<td>1000</td>
<td>±60%</td>
<td>96</td>
<td>4</td>
</tr>
<tr>
<td>6</td>
<td>5</td>
<td>10</td>
<td>±60%</td>
<td>70</td>
<td>30</td>
</tr>
<tr>
<td>7</td>
<td>5</td>
<td>50</td>
<td>±40%</td>
<td>99</td>
<td>1</td>
</tr>
<tr>
<td>8</td>
<td>5</td>
<td>50</td>
<td>±60%</td>
<td>99</td>
<td>1</td>
</tr>
<tr>
<td>9</td>
<td>5</td>
<td>50</td>
<td>±80%</td>
<td>100</td>
<td>0</td>
</tr>
<tr>
<td>10</td>
<td>5</td>
<td>50</td>
<td>±100%</td>
<td>100</td>
<td>0</td>
</tr>
<tr>
<td>11</td>
<td>5</td>
<td>50</td>
<td>±280%</td>
<td>85</td>
<td>15</td>
</tr>
<tr>
<td>12</td>
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<td>13</td>
<td>10</td>
<td>50</td>
<td>±280%</td>
<td>91</td>
<td>9</td>
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<tr>
<td>14</td>
<td>15</td>
<td>50</td>
<td>±280%</td>
<td>48</td>
<td>52</td>
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<tr>
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<td>17</td>
<td>30</td>
<td>50</td>
<td>±280%</td>
<td>0</td>
<td>97</td>
</tr>
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</table>

Table F.1: Experimental data

C: Population
K: Error gain
B: Boundary condition for the parameters, $\zeta$ and $\omega$. Upper and lower symmetric boundary compared to the best values, $\zeta = 0.90$ and $\omega = 52.5$.

x: Number of solutions with a deviation less than 0.4% of the best possible error, $0.807 \cdot 10^{-3}$.
y: Number of solutions with a deviation less than 2% and higher than 0.4%
F.3 Effect of changing the error gain

The error function is given by the equation F.3. By freezing the parameters B and C I tested the effect of changing K.

![Chart showing the effect of changing parameter K. C = 3, B = ±60%](image)

Figure F.1: Effect of changing the parameter K. $C = 3, B = \pm 60\%$
APPENDIX F. FURTHER TESTING OF THE COMPLEX ALGORITHM

F.4 Effect of changing the population

To see the effect of the population parameter, C, I set the error gain to 50 and boundaries to 250%.

The figure F.2 show that a to high population will increase the error. A population of 30 will in this case lead to no results within 0.4%. This result is valid for this test and this test only, and it could be possible that the best population will change dependent on the size of the parameter boundaries. This indication is verified by comparing test result number 3 and 8, see table F.1.
F.5  Effect of changing the boundaries

From this I conclude that the result is not very sensitive to the boundary conditions, as long as they embrace the optimal parameter size. The figure (F.3) show that our result will get a bit less optimal with high bandwidth on the boundary settings. A high bandwidth can be compensated with a larger population (see F.4). A consequence of increasing bandwidth and population is a significant increase in simulation time. I also notice a small but escalated error deviation when the boundaries are very low. This abnormal result is not significant and is ignored.
Appendix G

Simulink model of valve

\[ \zeta = 0.90 \]
\[ \omega = 52.5 \]
\[ A_{btv} = 1.25e-4 \]
\[ A_n = 2.08e-006 \]
Figure G.1: Simulink model of directional control valve
VBSO over center valve
BILANCIAMENTO, DOPPIO EFFETTO, VERSIONE "CC"
DUAL PILOT ASSISTED, "CC" TYPE OVERCENTRE

VBSO-DE-CC

05.42.05- X - Y - Z

DATI TECNICI / TECHNICAL DATA

Pressione max.
Max. pressure 350 bar

Portata max. vedi diagramma
Flow see performance graph

Taratura della valvola: almeno 1.3 volte superiore alla pressione indotta dal carico
Pressure setting: at least 1.3 times the load induced pressure

40 155 50 62.5 10 107 34 175 65 10 70 10 38 90 10.5 3/4 2.15
35 125 36 54.5 10 86 29.5 145 65 8 54 8 33 70 8.5 M22 1.45
35 125 36 54.5 10 80 32.5 145 65 8 54 8 33 70 8.5 1/2 1.45

S L6 L5 L4 L3 L2 L1 L I H4 H3 H2 H1 H F

X RAPPORTO DI PILOTAGGIO
PILOT RATIO

02 8.2 : 1
10 3.2 : 1

Y ATTACCHI / PORT SIZE

V1-V2-C1-C2

Z MOLLE / SPRINGS

Campo taratura
min - max bar
Adj. press. range bar

Incremento press.
bar / giro vite
Press. increase
bar / turn

Taratura standard
bar (Q = 5 l/min)
Std. setting bar
(made at = 5 l/min)

Cod. ordinazione
Ordering code

Colore
Colour

20 60-210 54 200 03.51.01.075 verde green
35 100-350 95 350 03.51.01.059 giallo yellow

03 G 1/2
04 G 3/4
89 M22x1.5

Marzo 99
Hydraulic Motor F12 series
## Specifications

<table>
<thead>
<tr>
<th>Frame size</th>
<th>30</th>
<th>40</th>
<th>60</th>
<th>80</th>
<th>110</th>
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<tbody>
<tr>
<td><strong>Displacement</strong> [cm³/rev]</td>
<td>30</td>
<td>40</td>
<td>59.8</td>
<td>80.4</td>
<td>110.1</td>
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<td>[cu. in./rev]</td>
<td>1.83</td>
<td>2.44</td>
<td>3.65</td>
<td>4.90</td>
<td>6.72</td>
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<td><strong>Motor operating speed</strong> [rpm]</td>
<td></td>
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<tr>
<td>max intermittent</td>
<td>7100</td>
<td>6400</td>
<td>5600</td>
<td>5200</td>
<td>4700</td>
</tr>
<tr>
<td>max continuous</td>
<td>5600</td>
<td>5000</td>
<td>4300</td>
<td>4000</td>
<td>3600</td>
</tr>
<tr>
<td>min continuous</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>50</td>
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<td><strong>Max pump selfpriming speed</strong> [rpm]</td>
<td>2850</td>
<td>2650</td>
<td>2350</td>
<td>2350</td>
<td>2200</td>
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<tr>
<td><strong>Torque (theor.) at 100 bar</strong> [Nm]</td>
<td>47.6</td>
<td>63.5</td>
<td>94.9</td>
<td>127.6</td>
<td>174.8</td>
</tr>
<tr>
<td>[In-lb]</td>
<td>29</td>
<td>38.7</td>
<td>58.1</td>
<td>77.5</td>
<td>106.6</td>
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<td><strong>Motor input flow</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>max intermittent [l/min]</td>
<td>213</td>
<td>256</td>
<td>335</td>
<td>418</td>
<td>517</td>
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<tr>
<td>[gpm]</td>
<td>56.3</td>
<td>67.6</td>
<td>88.5</td>
<td>110.4</td>
<td>136.6</td>
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<td>max continuous [l/min]</td>
<td>168</td>
<td>200</td>
<td>257</td>
<td>322</td>
<td>396</td>
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<tr>
<td>[gpm]</td>
<td>44.4</td>
<td>52.8</td>
<td>67.9</td>
<td>85.1</td>
<td>104.6</td>
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<tr>
<td><strong>Output power</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>max intermittent [kW]</td>
<td>110</td>
<td>130</td>
<td>175</td>
<td>220</td>
<td>270</td>
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<tr>
<td>[HP]</td>
<td>150</td>
<td>177</td>
<td>238</td>
<td>300</td>
<td>361</td>
</tr>
<tr>
<td>max continuous [kW]</td>
<td>70</td>
<td>85</td>
<td>110</td>
<td>153</td>
<td>165</td>
</tr>
<tr>
<td>[HP]</td>
<td>95</td>
<td>115</td>
<td>150</td>
<td>184</td>
<td>221</td>
</tr>
<tr>
<td><strong>Operating pressure</strong></td>
<td></td>
<td></td>
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</tr>
<tr>
<td>max intermittent [bar]</td>
<td>480</td>
<td>480</td>
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<td>480</td>
<td>480</td>
</tr>
<tr>
<td>[psi]</td>
<td>7000</td>
<td>7000</td>
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</tr>
<tr>
<td>max continuous [bar]</td>
<td>420</td>
<td>420</td>
<td>420</td>
<td>420</td>
<td>420</td>
</tr>
<tr>
<td>[psi]</td>
<td>6000</td>
<td>6000</td>
<td>6000</td>
<td>6000</td>
<td>6000</td>
</tr>
<tr>
<td><strong>Max case pressure at 1500 rpm</strong> [bar]</td>
<td>14</td>
<td>12</td>
<td>12</td>
<td>10</td>
<td>9.5</td>
</tr>
<tr>
<td>[psi]</td>
<td>200</td>
<td>175</td>
<td>175</td>
<td>145</td>
<td>140</td>
</tr>
<tr>
<td><strong>Main circuit temperature, max.</strong> [°C]</td>
<td>80</td>
<td>80</td>
<td>80</td>
<td>80</td>
<td>80</td>
</tr>
<tr>
<td>[°F]</td>
<td>176</td>
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</tr>
<tr>
<td>min. [°C]</td>
<td>-40</td>
<td>-40</td>
<td>-40</td>
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<tr>
<td><strong>Fluid viscosity, max.</strong> [mm²/s]</td>
<td>1000</td>
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<tr>
<td>[SUS]</td>
<td>5000</td>
<td>5000</td>
<td>5000</td>
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<td>5000</td>
</tr>
<tr>
<td>min. [mm²/s]</td>
<td>8</td>
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</tr>
<tr>
<td>[SUS]</td>
<td>58</td>
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<td>58</td>
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</tr>
<tr>
<td><strong>Fluid contamination level</strong></td>
<td>18/13</td>
<td>18/13</td>
<td>18/13</td>
<td>18/13</td>
<td>18/13</td>
</tr>
<tr>
<td>(ISO code 4406)</td>
<td></td>
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</tr>
<tr>
<td><strong>Mass moment of inertia</strong> (x10⁻³) [kg m²]</td>
<td>1.7</td>
<td>2.9</td>
<td>5</td>
<td>8.4</td>
<td>11.2</td>
</tr>
<tr>
<td>[ft lb s²]</td>
<td>1.3</td>
<td>2.1</td>
<td>3.7</td>
<td>6.2</td>
<td>8.2</td>
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<tr>
<td><strong>Weight</strong> [kg]</td>
<td>12</td>
<td>16.5</td>
<td>21</td>
<td>26</td>
<td>36</td>
</tr>
<tr>
<td>[lb]</td>
<td>26</td>
<td>36</td>
<td>46</td>
<td>57</td>
<td>79</td>
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