Analytical & Numerical Analysis of Ship/FPSO Side Structures Subjected to Extreme Loading with Emphasis of Ice Actions

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Marine Technology
Submission date: June 2014
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Norwegian University of Science and Technology
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Abstract

IACS has implemented a unified requirement (UR) for polar going ships. This thesis work consists of a well understanding of the backgrounds of IACS UR, the way of applying those rules to the structure and the comparison of different requirements among different polar classes indicated in IACS. Average ice load, design ice load patch dimensions are calculated for different ship size. This thesis includes a better perception about plastic collapse mechanism method which is the main principle of IACS framing requirements.

A DNV class FPSO had been chosen to apply the IACS requirements and it has brought a comparative view between IACS with a non IACS class ship. Two different simplified collapse mechanism models have been developed for a single longitudinal frame of the FPSO concerned. Moreover using Abaqus, a non-linear finite element analysis has been performed for a large part of side plating of that FPSO. Then, twice elastic slope method is used to establish limit load from analysis result. By observing limit loads and combining with them with IACS UR, an argument has been drawn regarding validity of this FPSO according to IACS Polar Class.
Scope of work

The DNV management team has identified Arctic Operation and Technology as one of the main strategic focus areas. Transport and exploitation of resources in the Northern areas are increasingly focused upon. The corresponding climatic conditions represent a challenge both to the operation and design of ships in these waters. The presence of sea ice is the main factor hindering operations in the Arctic. Sea ice is a complex material and induces high pressures when being in contact with ships or structures. In order to understand the nature of the associated forces, the ice physics and ice mechanics have to be studied.

The intention of this work is to obtain a basic understanding of the physics involved in ship ice interaction and to be updated on current activities related to the topics.

The Thesis work shall address the following topics:

1. Review of IACS Polar Class (UR I1) requirements from PC1 to PC 2/3/4/5

2. Compare the different requirements for structural design for each ice class. Discuss the differences between the various classes with respect strength. How are these differences implemented in the rules and what is the most crucial parameters that impose these steps in the rules. Compare the different methods for estimation of ice pressure for each ice class

3. Comment on the above mentioned theory study with respect to the validity of using these methods for the design of a moored Arctic FSPO/driller

4. Determine the required plate thickness and stiffener dimensions for a range of stiffener spacing and length.

5. Perform nonlinear finite element analysis of a single frame subjected to ice patch loading. Compare the results with the models underlying the IACS polar code.

6. To the extent that local buckling occurs in the web plate of the web frame, propose additional secondary stiffening and verify their effect by performing NLFEA.
7. Perform analysis of a large part of the ship side, containing stiffeners, web frames and stringers. Discuss in particular how boundary conditions have been modeled. Perform NLFEA and identify primary collapse mechanisms. Compare the results with simplified capacity models. On the basis of the simulations assess limit loads when fracture in the plating is likely to take place. The distribution of pressure loads is to be determined in agreement with the supervisor.

8. To the extent time permits perform modeling and analysis of a bow panel. Compare the results with simplified methods.

9. Conclusions and recommendations for further work
Preface

This thesis has been done for the partial fulfilment of the requirements for Master of Science degree program at the department of Marine Technology, Norwegian University of Science and Technology (NTNU), Trondheim, Norway.

This thesis is accomplished in spring 2014. In the time frame of thesis, the analysis for the bow section had to be omitted and work of verifying the IACS rules for moored FPSO had been limited to only basic concepts in consultation with my supervisor Professor Jørgen Amdhal.

I would like to express my gratitude to my honorable supervisor Professor Jørgen Amdhal for his advice, guidance and continuous support through this thesis.

It is a pleasure to thank Martin Storheim and Katerina kim for helping me on Abaqus. I like to offer my regards and blessings to my friend Oystein Helland, Mohammad Irfan Uddin and other friends for sharing their thoughts regarding my projects.

Trondheim, 10th of June 2014

Md Habibullah Bahar
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<td>American Bureau of Shipping</td>
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<tr>
<td>$Af$</td>
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<td>$Co$</td>
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<td>$CF_c$</td>
<td>Crushing class factor</td>
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<tr>
<td>$D_{ship}$</td>
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<td>$KT$</td>
<td>kilo ton</td>
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<td>$E_{crush}$</td>
<td>Ice crushing energy</td>
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<td>FPSO</td>
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<td>$Fn$</td>
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<td>$hw$</td>
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Introduction

Transportation and exploitation of resources are increasing in the Northern area day by day. The climate of arctic area is the major challenging factor. The ships which are trading in arctic area, has to face the presence of ice. Ice is a complex material and creates high pressure during contact with ship and structures. So, well understanding the ice load on structure is the main factor to take into account for designing a ship for arctic area.

To mitigate this challenge International Association of Classification Societies combining with other classification societies has formed a Unified Requirements (UR). Understanding the principles, methods used and the way of derivation of the formulations described in IACS UR, 2011 [1] are the main inspirations of this thesis work. IACS requirements differ with 7 different polar class; PC1 to PC7 (Table 1) according to ship owner trading purpose and operational window. Ice load, framing requirements vary among these seven polar classes.

To get a comparative assessment, a FPSO has been chosen under DNV class, named ‘White Rose Field Husky Oil FPSO’. Method behind DNV polar class requirements is different than IACS. DNV used elastic method [2] to derive their formulas but IACS has used plastic method. Plastic method allows large deflection and post ultimate resistance range which utilize the overloading concept which is common fact nowadays. Plastic methods are normally applied where the load are extreme and not cyclic in nature which is so much in line with ice load nature. Ice load nature is different for a moored structure and that’s why it is also a concern to verify the IACS UR for that situation.

Finite Element Method is a popular numerical technique for engineering analysis. Adding non-linear behaviour to this method is a good choice when we need ultimate strength of structure which can buckle as well. In this work geometrical and material non-linearity has been considered. Abaqus is a powerful tool to perform non-linear finite element analysis and reliable to take as a real analysis value. So IACS requirements comparison with Abaqus results can give a satisfactory assessment for our regarding structure.
1. Review of IACS Polar Class Requirements

An international committee including representatives from many classification societies and polar nations developed requirements concerning polar class in the form of a Unified Requirement, International Association of Classification Society (IACS) standard. IACS standards are applicable to steel made ships which are desired to navigate in ice-surrounded polar waters, except ice breakers [1]. IACS unified requirements differs when the ice condition varies. Ice formation is complex and it is the main challenge to estimate the ice load perfectly. Daley shows the approach to determine the ice load in his paper [3] for IACS and the rules are based on single frame loading. Framing requirements are described in the paper of Daley and Kendrick [4], are based on plastic collapse mechanism work-energy principle. The different feature, backgrounds behind ice load calculation and framing requirements including some comparison with other classification societies are described below:

1.1. Polar Classes

Designing of a ship for operating in polar area, it is must to know about the ice condition in that route, duration of ice extent, operation window for that ship etc. Considering these issues IACS unified rules are classified into 7 polar classes. These Polar classes are the notation for making differences among the requirements of polar ships with respect to strength and operational window. Ships that comply with the IACS UR can be considered for a Polar class notation as listed in Table 1

<table>
<thead>
<tr>
<th>Polar class</th>
<th>Ice Description (Based on WMO Sea Ice Nomenclature)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PC 1</td>
<td>Year-round operation in all Polar waters</td>
</tr>
<tr>
<td>PC 2</td>
<td>Year-round operation in moderate multi-year ice conditions</td>
</tr>
<tr>
<td>PC 3</td>
<td>Year-round operation in second-year ice which may include multiyear ice inclusions.</td>
</tr>
<tr>
<td>PC 4</td>
<td>Year-round operation in thick first-year ice which may include old ice inclusions</td>
</tr>
</tbody>
</table>
PC 5 | Year-round operation in medium first-year ice which may include old ice inclusions
---|---
PC 6 | Summer/autumn operation in medium first-year ice which may include old ice inclusions
PC 7 | Summer/autumn operation in thin first-year ice which may include old ice inclusions

Owner selects an appropriate polar class and this selection keep that ship in balance with strength to ice condition keeping the economic consideration in mind.

We can get an idea how IACS polar classes differ with other classification societies with respect to nominal ice thickness (Figure 1-1) [5]

![Figure 1-1: Comparison of ice classes by nominal ice thickness](image)

From ice thickness comparison IACS classes are different from every class. The higher class limit is same with Canadian arctic shipping regulations, Russian
Register and ABS. The lightest class PC 7 of IACS is in between ICE-05 and ICE-10 of DNV class. The highest polar class of DNV, Polar 30 is equivalent to IACS PC4.

1.2. Upper and Lower Ice waterlines

The upper ice waterline (UIWL) is the maximum draughts fore, amidships and aft. The lower ice waterline is the minimum draughts fore, amidships and aft. The lower ice waterline is determined in ballast condition so that propeller submerges.

1.3. Hull Areas

The hull of polar class ships is divided into areas according to the expected load act upon them.

There are four regions:

- Bow
- Bow intermediate
- Mid-body
- Stern
- Bottom
- Lower
- Ice belt regions

This can be illustrated as following figure.

![Figure 1-2: Hull area extent](image)
Hull area is divided into many portions as the requirements vary on hull area as the ice load is not same in all areas. The bow area faces the highest forces and lowers for other portions. A typical pressure variation is shown below as hull area described in Figure 1-2.

![Pressure variance as Hull Area variation](image)

**Figure 1-3:** Pressure variance as Hull Area variation [6]

### 1.4. Design Ice Load

Ice load is established based on a design scenario and it is a glancing collision with an ice edge (Figure 1-4). This scenario is linked to the ice load with a ratio. Ice load equations are based on energy based collision model and this model assumes a ‘Popov’ type of collision in which ice indentation is introduced by a pressure area relationship. The following derivation process is based on as described in ‘Annex’ of paper of (Daley 2000) [3].

The following are considered for solving the ice load equation:

- Ice thickness
- Ice strength (crushing pressures)
- Hull form
- Ship size
- Ship speed
In this glancing scenario, it is assumed that a ship is in her design speed strikes an angular ice edge and she penetrates the ice and rebounds away. Then ice force is determined by equating the normal kinetic energy and ice crushing energy over penetration depth,

\[ \frac{1}{2} M_e V_n^2 = \int_0^{\delta_n} F_n(\delta) \cdot d\delta \]  

(1-1)

Where,
- \( \delta \) = normal ice penetration
- \( F_n \) = normal force
- \( M_e \) = effective mass = \( M_{\text{ship}} / C_0 \)
- \( V_n \) = normal velocity = \( V_{\text{ship}} \cdot l \)
- \( l \) = direction cosine
Using the ice penetration geometry (Figure 1-5) combining with pressure-area relationship, ice crushing normal force has been calculated. The maximum ice crushing force cannot be higher than the force to fail the ice in bending (Figure 1-6). Limit force for bending is defined by the combination of angles, ice strength and thickness (see equation 1-8).

![Diagram showing force versus contact area with ice, flexural strength of ice, and ice crushing force.]

Figure 1-6: Ice crush till flexural strength of ice

The nominal contact area from Figure 1-5,

\[ A = \frac{W}{2} H \]  

(1-2)

Where,

\[ W = \frac{2\delta \tan \left( \frac{\phi}{2} \right)}{\cos \beta''} \]  

(1-3)

\[ H = \frac{\delta}{\sin \beta' \cos \beta''} \]  

(1-4)

Now, average pressure is determined by pressure area relationship,

\[ P = P_0 A^{ex} \]  

(1-5)

Where, \( P_0 \) is a class dependent ice pressure at 1 m\(^2\) [MPa].
Then after some calculation we get the normal ice load, (details calculation in Appendix of the paper of Daley [3])

\[ F_n = (3 + 2 \cdot \text{ex}) \frac{2^{3x+2}}{3^{2x+2}} \cdot \frac{P_0}{3^{2x+2}} \cdot \left( \frac{\tan(\phi/2)}{\sin \beta \cdot \cos^2 \beta'} \right)^{1+\text{ex}} \cdot \left( \frac{1}{2} \cdot \Delta_n \cdot V_n^2 \right)^{2 \cdot 3x+2} \]  

(1-6)

Where, \( \Delta_n = \frac{\Delta_{\text{ship}}}{C_0} \)

Here in this equation, ex connects the force solution with the pressure-area relationship. Only the ice pressure at 1 m² \( P_0 \) is a class dependent parameter. Other variables are the hull angles (Figure 1-7) and ship displacement. So the force is dependent on ship bow shape and ship size.

Equation (1-6) can be simplified by following equation by taking \( \text{ex}=-0.1 \), \( \phi=150 \) deg and collecting the all the angle term into \( fa \) by following,

\[ F_n = fa \cdot P_0^{0.36} \cdot \Delta_{\text{ship}}^{0.64} \cdot V_{\text{ship}}^{1.28} \]  

(1-7)

Where, shape coefficient \( fa \) is,

\[
fa = \min \left\{ \begin{array}{l}
0.097 - 0.68 \left( \frac{x}{L} - 0.15 \right)^2 \frac{\alpha}{\sqrt{\beta'}} \ldots crushing \_ failure \\
1.2 CF_F \frac{\sin \beta' \cdot CF_C \cdot \Delta_{\text{ship}}^{0.64}}{\sin \beta' \cdot CF_C \cdot \Delta_{\text{ship}}^{0.64}} \ldots Flexural \_ failure \\
0.60 \ldots \ldots \ldots \ldots \ldots Limiting \_ failure
\end{array} \right. 
\]  

(1-8)
Where,

\[ x = \text{distance from forward perpendicular to the station under consideration} \]

\[ \text{CF}_f = \text{Flexural Class factor} = \sigma_f h_{\text{ice}}^2 \]

\[ \text{CF}_c = \text{Crushing class factor} = P_0^{0.36} \cdot V_{\text{ship}}^{1.28} \]

\[ h_{\text{ice}} = \text{ice thickness [m] [class dependent]} \]

\[ \sigma_f = \text{ice flexural strength [Mpa] [class dependent]} \]

\[ \beta' = \text{normal (true) frame angle} \]

In equation (1-8) \( fa \) has been considered for different failure mode of ice (Figure 1-8) and the minimum value has to be considered to calculate the ice load. By introducing flexural failure, the crushing load is now limited up to flexural failure. Crushing failure load cannot be higher than the flexural failure load. For crushing failure \( fa \) measured at several locations at the bow area to find the dimensioning load. The maximum value of \( fa \) is bound to be within 0.6 for avoiding extreme value. Finally, the minimum value has to be taken.

![Figure 1-8: Ice Failure Mode [7]](image)

After introducing the class factors, the load equation (1-7) be simplified to,

\[ F_n = fa \cdot CF_c \cdot A_{\text{ship}}^{0.64} \]

\[ (1-9) \]

1.5. **Design Load Patch**

From the equation (1-5), it can be said that ice force has a relation with nominal contact area between ship and ice. This contact area (nominal-overlapped) then simplified from triangular to an equivalent area rectangular patch which is called design load patch and the average pressure is distributed.
uniformly over the area patch. Then this ice load patch is reduced to be conservative by taking account the ice edge spalling effect (Figure 1-11).

Figure 1-9: Nominal and design rectangular load patches [3]

Then we get the simplified design load patch with height $b$ and width $w$ as shown in Figure 1-10.

Figure 1-10: Ice load patch configuration [3]
Figure 1-11: Ice Failure including crashing and spalling [7]

So as described in Figure 1-9, the area of the nominal load patch using area pressure relationship will be (combining with equation 1-5)

$$A_{nom} = H_{nom} \cdot W_{nom} = \left( \frac{F_n}{P_0} \right) \frac{1}{1+ex}$$

(1-10)

Introducing aspect ratio,

$$AR = \frac{W_{nom}}{H_{nom}}$$

(1-11)

Using equation 1-3, 1-4 and assuming $\phi = 150$ deg.

$$AR = 2\tan(\phi/2)\sin \beta' = 7.46\sin \beta'$$

(1-12)

Using equation 1-3, 1-4, 1-10 the equation be,

$$H_{nom} = \left( \frac{F_n}{P_0 \cdot AR^{1+ex}} \right)^{\frac{1}{2+2ex}}$$

(1-13)

$$W_{nom} = \left( \frac{F_n}{P_0 \cdot AR^{1+ex}} \right)^{\frac{1}{2+2ex}} \cdot AR$$

(1-14)

Then to be conservative taking the ice spalling effect into account the load area described in equation 9 has been reduced, but the force will be same and pressure will rise. So the dimension of design load patch,

$$w = W_{nom}^{\text{wex}} = W_{nom}^{0.7} = F_n^{0.389} P_0^{-0.389} AR^{0.35}$$

(1-15)

$$b = \frac{w}{AR} = F_n^{0.389} P_0^{-0.389} AR^{-0.65}$$

(1-16)

In equation 12, frame angle $\beta'$ should not be less than 10 degree so that AR will be minimum 1.3 in bow region and for non-other than bow AR is fixed 3.6. [1]
Then the line load and pressure can be obtained as below:

\[ Q = \frac{F_n}{w} = F_n^{0.61} \frac{CF_D}{AR^{0.35}} \]  \hspace{1cm} (1-17)

\[ P = \frac{Q}{b} = F_n^{0.22} CF_D^2 AR^{0.3} \]  \hspace{1cm} (1-18)

The maximum value of F, Q and P occurs in different location of bow. So for determining the peak values of F, Q and P, calculation is done at many points at bow with an increment of at least L/20 or minimum 5 points. From every set the largest value of each parameter has chosen to be conservative. Finally largest value set is chosen for obtaining a single design load patch.

1.6. **Peak Pressure Factor (PPF)**

Having a complex structure of ice in real, the ice loads are quite peaked within the load patch. So, a set of peak pressure factors are used in design formula. The average pressure can be formulated within design load patch

\[ P_{avg} = \frac{F}{b \cdot w} \text{[MPa]} \]  \hspace{1cm} (1-19)

Within a higher area, concentrated pressure is more common in load patch and for smaller area; pressure will be higher for local. So to account the concentrated pressure for big area and localized pressure for smaller area PPF is used. PPF is illustrated below,

![Figure 1-12: Peak Pressure Factor to design individual elements [3]](image)

As the formula given in IACS polar class framing requirements, the following facts are important by giving PPF some minimum value for different framing system.
For plating member, stiffener spacing is limited to 600mm for transversely framed and 583mm for longitudinally framed structure.

For stringers, web frames PPF value is 1 if the web frame spacing is half of the ice load patch width.

So after the total description of ice load derivation, design loads are developed in several stages.

Firstly, the total load is minimum than the crushing and flexural limiting load for the design ice.

Secondly, the load patch is idealized.

Thirdly, load distribution within the idealized load patch is modified to account for local loading peaks.

1.7. IACS Structural Requirements

A polar class ship has to face random ice loading with a possibility of extreme load magnitude. To satisfy this demand, when designing a polar class ship, possibility of overloading must be considered. The IACS Unified Requirements has followed simplified plastic collapse mechanisms as design criteria for the structural members. It is called simplified because it is assumed the material is perfectly plastic and the collapse mechanism contains shear-bending moment hinge that means membrane and strain hardening effects are neglected but in real both of these are so obvious.

1.7.1. Membrane effect

In ship hull construction, plate fittings are continuous and the plate gets membrane force from adjacent plates. When we consider membrane effect, the capacity of a plate increases with respect to lateral deflection, as shown in Figure 1-13. Even when a member get enough lateral support, for plate support is from adjacent plate, shear failure not be critical (Amdhal, 2004) [8]. Daley has shown his derivation regarding the IACS UR neglecting the membrane effect. So Daley's derivation should give lower value than the real.
1.7.2. Energy Method

In IACS unified requirement the derivation of plastic framing requirements for polar ships is based on the shear plastic collapse mechanisms using work-energy principles \[11\].

Before applying energy method, right response mechanism (collapse mechanism) has to be chosen which has minimum capacity \[9\] \[2\], as this will be closest to the capacity that the structure actually provides. Even then choosing the minimum this is the upper bound to capacity. The chosen mechanism is valid for the regarding boundary condition and the material is assumed ideally plastic.

1.7.3. Collapse Mechanism

To understand the collapse mechanism, as explained by Tore H. Soreide \[9\] and Amdhal \[2\], the plastic mechanism for a clamped frame subjected to a uniform load develops through the following step:

First step: Increasing the load $q$ steadily from zero upto yield occurs. This yield load is denoted as $q_y$, and the elastic moment $M_y$. So the bending moment at this stage,
\( M_y = \frac{q_x l^2}{12} \) \hspace{1cm} (1-20)

**Second step:** Then load increase until \( q_1 \), so that ends reach maximum moment \( M_p \) i.e. be fully plastic and plastic hinge form at two ends.

\[ M_p = \frac{q_1 l^2}{12} \] \hspace{1cm} (1-21)

And moment at middle which is not plastic yet,

\[ M_{p1} = \frac{q_1 l^2}{24} \] \hspace{1cm} (1-22)

**Third step:** After reaching the maximum moment at end, it cannot take any moment more. So beam act as simply supported beam. In this condition, further load \( q_2 \) applied upto reach maximum moment \( M_{p2} \) and the beam center turns into 3\textsuperscript{rd} plastic hinge. So the moment, considering as simply supported at middle,

\[ M_{p2} = \frac{q_2 l^2}{8} \] \hspace{1cm} (1-23)

So total moment at middle of the beam,

\[ M_p = M_{p1} + M_{p2} = \frac{q_1 l^2}{24} + \frac{q_2 l^2}{8} \] \hspace{1cm} (1-24)

Combining equation 1-21, and 1-24,

\[ M_p = \frac{q_2 l^2}{4} \] \hspace{1cm} (1-25)

Now, the total load so far to form 3 plastic hinge is,

\[ q_c = q_1 + q_2 \] \hspace{1cm} (1-26)

Combining equation, 1-22, 1-25 and 1-26, we get the collapse load,

\[ q_c = 16 \frac{M_p}{l^2} \] \hspace{1cm} (1-27)
Figure 1-14: Formation of 3-hinge collapse mechanism for uniformly loaded beam

First step

\[ M_y = \frac{q_y l^2}{12} \]

Second step

\[ M_p = \frac{q_1 l^2}{12} \]

\[ M_p = \frac{q_y l^2}{24} \]

Third step

\[ M_p = \frac{q_y l^2}{8} \]

3-hinge collapse mechanism

\[ M_p = \frac{q_1 l^2}{24} + \frac{q_2 l^2}{8} \]

\[ M_p \]

\[ \theta \]

\[ w \]

\[ 2\theta \]

\[ \theta \]

\[ \text{Fixed support} \]

\[ \text{Free support} \]

\[ \text{Plastic hinge} \]
Load development and material behavior during formation of 3-hinge in Figure 1-14 is shown below:

![Graph showing load development and material behavior during formation of 3-hinge](image)

Figure 1-15: load development and material behavior during formation of 3-hinge

### 1.7.4. Moment and shear interaction

Daley has derived the framing requirements for IACS considering shear interaction i.e. shear stress in web section. When shear capacity increase then plastic moment capacity will decrease. Shear-moment interaction has been showed below:

![Graph showing Shear-Moment interaction](image)

Figure 1-16: Shear-Moment interaction [11]

Normally it is assumed that shear totally carried by the web. So for a flanged
frame, if web be fully plastic in shear even then frame will have the moment capacity as $M_0$. So practically frame has been designed in that way so that it could work in a combined way with significant moment and shear capacity. So at the ends reduced moment capacity, $M_{pr}$ has been used in Daley’s derivation. Shear-moment interaction can be expressed in following way [4]:

$$
\left( \frac{M}{M_{ult}} \right)^2 + \left( \frac{T}{\alpha T_{ult}} \right)^2 = 1
$$

(1-28)

Where,

$\alpha$=Section dependent, greater than or equal to one  
$M$= Bending moment  
$T$= shear capacity

1.7.5. Collapse mechanisms in IACS requirements

In the IACS Unified Requirements rules for framing requirements are based on energy principles so that the external energy is equal to internal energy. The following assumptions has taken into account,

- Rigid plastic material behavior  
- Ignores large deformation effects: membrane, strain hardening etc.

IACS has considered the following energy absorbing mechanisms, where the energy is assumed to be dissipated at the hinges.

1. Pure bending hinge  
   Considering a centrally patch loaded frame. Boundary condition of ends could be fixed-fixed or fixed-simply supported.

2. Combination of shear and bending hinge  
   When we consider a both clamped ends. In the fixed boundary condition shear force develop. Due to having shear stresses the plastic capacity will be reduced to $M_{pr}$.

3. Shear hinge  
   This hinge form when considering an asymmetrical patch load. The both ends can transfer the moment to the adjacent structure. Boundary condition is considered as fixed-fixed.
1.7.6. Centrally loaded patch

Cross sectional area of the attached plate normally be larger than the local frame so that it is assumed that plastic neutral axis is at the intersection point of the frame and the plate [11], shown in Figure 1-17.

![Figure 1-17: Simplified Plastic Modulus concept [11]](image)

Figure 1-18: Cross section dimensions as defined by IACS [1]
So that the plastic section modulus is,

\[ Z_p = A_f \left( \frac{t_f}{2} + h_w + \frac{t_p}{2} \right) + A_w \left( \frac{h_w}{2} + \frac{t_p}{2} \right) \]  
(1-29)

If the neutral axis situated above the intersection point and it is assumed the angle \( \phi_w = 90 \) then the neutral axis,

\[ Z_{na} = \frac{A_f + h_w t_w - t_p s}{2t_w} \]  
(1-30)

And the exact plastic section modulus will be,

\[ Z_{p,exact} = t_p s \left( Z_{na} + \frac{t_p}{2} \right) + \frac{(h_u - Z_{na})^2 + Z_{na}^2}{2} + A_f (h_c - Z_{na}) \]  
(1-31)

Figure 1-19: 3-hinge Collapse Mechanism for centrally patch loaded frame with fixed-fixed ends

Now, applying energy method for frame in Figure 1-19,

\[ W_e = \int_{-b/2}^{b/2} P.S.w(x)dx \]
\[ = 2 \int_{0}^{b/2} P.S.w(x)dx \]
\[ = 2P.S.\delta \int_{0}^{b/2} \left(1 - \frac{2}{L} x \right)dx \]
\[ = P.b.S.\delta \left(1 - \frac{b}{2L} \right) \]  
(1-32)
Internal work,

\[ W_i = \frac{4M_p}{L} \left( 1 + \frac{4M_{pr}}{L} \right) \]  \hspace{1cm} (1-33)

So, equating external and internal work we get,

\[ P.b.s \left( 1 - \frac{b}{2L} \right) = \frac{4M_p}{L} + \frac{4M_{pr}}{L} \]  \hspace{1cm} (1-34)

If we don't consider reduced plastic moment, then we get the capacity equation as follows,

\[ P = \frac{8M_p}{L.b.s \left( 1 - \frac{b}{2L} \right)} \]  \hspace{1cm} (1-35)

Where,

- \( P \) = the patch pressure
- \( S \) = frame spacing
- \( M_p = Z_p \sigma_y \)
- \( M_{pr} = Z_{pr} \sigma_y \)
- \( \sigma_y \) = yield stress

As derived by Daley [11] reduced section modulus,

\[ Z_{pr} = Z_p \left( 1 - k_w \left( 1 - \sqrt{1 - \frac{A_0}{A_w}} \right) \right) \]  \hspace{1cm} (1-36)

Where, minimum shear area, \( A_0 = \frac{1}{2} PbS \frac{\sqrt{3}}{\sigma_y} \) \hspace{1cm} (1-37)

\[ k_w = \frac{Z_w}{Z_p} \]  \hspace{1cm} (1-38)

When web will be fully effective in bending, \( Z_{pr} \) will be equal to \( Z_p \). So using equation 1-34, minimum section modulus,
\[ Z_0 = \frac{PbS}{8\sigma_y} \left(1 - \frac{b}{2L}\right)L \]  

So finally we get the capacity for 3-hinge collapse by using equation 1-34, 1-36, 1-37, 1-38

\[ P_{3h} = \frac{(2-k_w) + k_w \sqrt{1 - 48Z_{p\text{max}}(1-k_w)}}{12Z_{p\text{max}}k_w^2 + 1} \frac{4Z_p\sigma_y}{[SbL(1-b/2L)]} \]  

\[ Z_{p\text{max}} = \frac{1}{48(1-k_w)} A_w L \left(1 - \frac{b}{2L}\right) \]  

For the term under the root sign of equation (40) to stay positive, Zp must be less than Z_{p\text{max}}

\[ P_{3h} = \frac{2}{\sqrt{3}} \frac{A_w\sigma_y}{Sb} \]  

When Zp will be greater than Z_{p\text{max}} then shear failure will occur at frame first and the capacity will be limited to,
1.7.7. End load case (Asymmetric load)

From the Figure 1-20 the external work is found by integrating the external load over the deformation. So the external work is,

\[ W_e = \int_{c}^{b} P.S.\left[w(x)\right]dx \]

\[ = P.S.\left[\int_{c}^{a} \frac{x}{a} dx + \int_{a}^{b} \left(1 + \frac{x-a}{a-L}\right) dx\right] \]

\[ = P.S.\left[\frac{(a+c)(a-c)}{2a} + \frac{b+c-a}{L-a} \left(L - \frac{a+b+c}{2}\right)\right] \]

Find the location of c which will give the maximum external work.

\[ \frac{d}{dc} W_e = 0 \]

This gives, \[ c = a\left(1 - \frac{b}{L}\right) \]

Using equation 1-44, 1-46 we get the maximum external work for asymmetric loading condition,

\[ W_{e,\text{asym}} = PbS\left(1 - \frac{b}{L}\right) \]

For internal work, taking 4-shear hinges in shear panel and one bending hinges in the other end, the internal work for unit deflection will be,
\[ W_i = N + M_p \frac{1}{L-a} + m_p \left( \frac{2}{a} - \frac{1}{L-a} \right) \] (1-48)

Then equating the external and internal work and after some calculation (details in paper of Daley [11]) the shear capacity for this condition can be given by,

\[ P_s = \frac{\sigma_y}{bS(1-b/2L)} \left[ \frac{A_s}{\sqrt{3}} + \frac{Z_k}{L} \left( 1.1 + 5.75k_z^{0.7} \right) \right] \] (1-49)
2. Comparison of Polar Classes

IACS UR is classified into 7 polar classes PC1 to PC7. Among these polar classes the PC1 is the heaviest class with respect to strength which permits the structure to trade in year round ice condition and PC7 is the lightest. The requirements vary among these seven polar classes from many aspect of view. Comparison, differences, the different way of implementation of the requirement and the important parameters among these polar classes; all are discussed below:

2.1. Ice load

- For all polar class a glancing scenario on the bow area is considered as the design scenario.
- The parameters to define the ice load are
  - Average pressure\( (P_{avg})\)
  - Design load patch width\( (w)\) and breadth\( (b)\)
  - Total glancing impact force\( (F)\)
  - Line load\( (Q)\)
  - Shape co-efficient\( (f_a)\)
- The above mentioned parameters has to be calculated for the specific hull area as a function of bow shape for regarding polar class as shown below:

![Figure 2-1: Ice load parameter dependency on hull area](image-url)
Class dependent parameters define the glancing impact nature. Class factors are formulated as given discussed in earlier chapter.

- Crushing class factor: \( CF_c = P_0^{0.36}v_{ship}^{1.28} \)
- Flexural class factor: \( CF_F = \sigma_F h_{ice} \)
- Patch class factor: \( CF_D = P_0^{0.389} \)

These formulas are showing that, ship speed, ice flexural strength, nominal ice thickness all are constant class dependent. The values are given below:

<table>
<thead>
<tr>
<th>Polar Class</th>
<th>Crushing Failure Class Factor (CF_c)</th>
<th>Flexural Failure Class Factor (CF_f)</th>
<th>Load Patch Dimensions Class Factor (CF_D)</th>
<th>Displacement Class Factor (CF_DIS)</th>
<th>Longitudinal Strength Class Factor (CFL)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PC1</td>
<td>17.69</td>
<td>68.6</td>
<td>2.01</td>
<td>250</td>
<td>7.46</td>
</tr>
<tr>
<td>PC2</td>
<td>9.89</td>
<td>46.8</td>
<td>1.75</td>
<td>210</td>
<td>5.46</td>
</tr>
<tr>
<td>PC3</td>
<td>6.06</td>
<td>21.17</td>
<td>1.53</td>
<td>180</td>
<td>4.17</td>
</tr>
<tr>
<td>PC4</td>
<td>4.5</td>
<td>13.48</td>
<td>1.42</td>
<td>130</td>
<td>3.15</td>
</tr>
<tr>
<td>PC5</td>
<td>3.1</td>
<td>9</td>
<td>1.31</td>
<td>70</td>
<td>2.5</td>
</tr>
<tr>
<td>PC6</td>
<td>2.4</td>
<td>5.49</td>
<td>1.17</td>
<td>40</td>
<td>2.37</td>
</tr>
<tr>
<td>PC7</td>
<td>1.8</td>
<td>4.06</td>
<td>1.11</td>
<td>22</td>
<td>1.81</td>
</tr>
</tbody>
</table>
As it is seen from above figure, flexural class factor values vary so much compared to crushing factor. The dimension load patch factor is almost so close for all polar class. For better understanding let recall the force equation 1-9 and shape coefficient $fa$ again,

$$F_n = fa \cdot CF_c \cdot \Delta_{ship}^{0.64}$$

For higher polar class, flexural factor is so much high which permit crushing force to a substantial limit. That means the structure of higher polar class has been given better crushing ability. But the load patch dimension factor doesn’t change as the load changing. So that simplified design load patch dimension has been kept approximately close for all polar classes (see Figure 2-4).

- From force equation 1-9, it can be said that the ice force is dependent on ship size and bow angles. So ice force is dependent on ship shape i.e. ship’s displacement. Pressure and load dimension variance for different displacement has been shown below. The calculations have been done for ‘mid-body ice belt area’.
Comparison of Polar Classes

Figure 2-3: Pressure variance for different displacement

From above figure it can be said that ice load is obtained much higher for PC1 & PC2 compared to other class. And pressure variance is also higher for PC1 and PC2. Pressure variance is linear when displacement is more than 90 Kilo Ton for PC1 and PC2. For PC3-PC7 pressure variance is linear when ship displacement is more than 60 Kilo Ton.

Figure 2-4: Load Patch dimension variations

From the above two curves set, variation of dimensions is quite regular compared to the pressure variation. For a displacement, like 250 KT, where pressure is varying from 3 MPa to 19 MPa but load height is changing form 1.2 m to 1.8 m and width 4.4m to 6.3m only. As load area is not increasing as pressure increase, higher polar class is intended to face more local pressure than lower polar class. So local strengthening will be a requirement for higher polar class.
2.2. Framing Requirements

2.2.1. Shell plate requirements

As given in IACS req. 2011, the shell plate thickness (unit: mm) is

For transversely framed plating, \( t_{net} = 500s \left( \frac{AF \cdot PPF_p \cdot P_{avg}}{\sigma_y} \right)^{0.5} \frac{1}{1 + \frac{s}{2b}} \) \hspace{1cm} (2-1)

For longitudinally framed, when \( b \geq s \); \( t_{net} = 500s \left( \frac{AF \cdot PPF_p \cdot P_{avg}}{\sigma_y} \right)^{0.5} \frac{1}{1 + \frac{s}{2l}} \) \hspace{1cm} (2-2)

when \( b < s \); \( t_{net} = 500s \left( \frac{AF \cdot PPF_p \cdot P_{avg}}{\sigma_y} \right)^{0.5} \left( \frac{2b}{s} - \left( \frac{b}{s} \right)^2 \right)^{0.5} \frac{1}{1 + \frac{s}{2l}} \) \hspace{1cm} (2-3)

Where,

- \( s \) = transverse frame spacing in transversely-framed ships or longitudinal frame spacing in longitudinally-framed ships [m]
- \( AF \) = Hull Area Factor
- \( PPF_p \) = Peak Pressure Factor
- \( P_{avg} \) = average patch pressure [MPa]
- \( \sigma_y \) = minimum upper yield stress of the material [N/mm²]
- \( b \) = height of design load patch [m]
- \( l \) = distance between frame supports[m].

From the above equations, plate thickness is dependent on pressure which means dependent on ship displacement, and the frame arrangements.

For a specific framing arrangement, the plate thickness variation is proportional to \( P^{0.5} \). So the variations show the same trend as pressure variations as shown in Figure 2-5. These thicknesses are for frame spacing 600mm and span length 2.215 m for a longitudinally framed FPSO.
For a specific displacement thickness requirements change linearly with frame spacing. IACS rules limit the frame spacing to maximum 600 mm for plating members considering the peak pressure factor discussed earlier. From Figure 2-5 & Figure 2-6, plating thickness is much higher for PC and PC2 comparing to others as it was discussed earlier that for higher polar class local high pressure is much higher.

2.2.2. Shear Area

Minimum shear area (equation 1-37) is modified in IACS req. 2011 [1] as given as below; for longitudinally ships,
Comparison of Polar Classes

\[ A_L = \frac{100^2 \cdot AF \cdot PPF_s \cdot P_{avg} \cdot 0.5 \cdot b_1 \cdot a}{0.577 \cdot \sigma_y} \] [cm²] \hspace{1cm} (2-4)

Where,

PPFs = Peak Pressure Factor
b1 = ko · b2 [m]
k0 = 1 - 0.3 / b'
b' = b / s
b2 = b · (1 - 0.25 · b') [m], if b' < 2
= s [m], if b' ≥ 2
a = longitudinal design span [m]

Calculating the minimum shear area required for frame spacing of 600mm, span length of 2.215 m and ship displacement 186.12 KT

From above figure, there is a huge difference between lightest and heaviest polar class. For polar class PC1 and PC2 need heavy longitudinal frame to protect shear failure which could be achieved by giving higher web height.
3. IACS UR for a moored Arctic FPSO

The failure modes of an ice sheet are mainly compression failure i.e. crushing and flexure failure i.e. buckling, bending etc. For trading in polar waters, the main challenge is to crush or bend the ice while the ship moves. The structure must have the strength to resist the ice bending force. But for a moored FPSO, it is different. The force is from drifting ice and it bends itself to the FPSO. So a moored FPSO has to be strength enough to resist the drifting ice pressure.

The normal ice load is expressed as equation (1-9)

\[ F_n = f_a \cdot C_F \cdot \Delta_{ship}^{0.64} \]

For a moored FPSO, the vessel velocity which is class dependent is not related to this case. The other factors such as the ice thickness, strength of ice data for a polar class are predetermined. These data can be found from the environmental data for a specific area. So as discussed earlier, the main parameter that can be changed is hull shape or more specifically bow shape.

Another challenge is to keep the FPSO face to the opposite of the ice drift (Figure 3-1). In addition the ice drift direction changes always because of wind and current. So the designing of an effective mooring system is necessary and make it sure that its ice vaning capacity is at its best. Ice vaning is the capability of the FPSO to keep the bow direction always towards to drift direction.

![Figure 3-1: Ice vaning: Ice drifts and ship direction [12]](image)
A moored ship scenario is quite different than a moving one. For a moving FPSO, in the energy balancing equation (1), normal kinetic energy includes the mass of ship but in this case it will be drifting ice sheet mass. So the kinetic energy equation will be for ice sheet. The mooring system and FPSO itself has to be strength enough to resist the kinetic energy of ice sheet. The wedge based (Figure 1-5) collision which determines the nominal contact area, $A = \frac{WH}{2}$ should also be different for moored condition which will make the ice load calculation different.
4. Assessment of a FPSO

Floating production, storage and offloading (FPSO) unit is familiar in the offshore oil and gas industry. This thesis work was motivated by a FPSO named ‘white Rose Field Husky Oil FPSO’ which was built under DNV class. She had been built to operate in White Rose oil field, 350km off the coast of Newfoundland and operated by Husky Energy; build by Samsung heavy industries co. ltd. [13].

This FPSO was interesting to choose because DNV class framing requirements calculation method is different to IACS. So by assessing this FPSO, we will get a comparative assessment with IACS requirements.

In this thesis work I worked with a larger part of the ship side. As IACS hull area definition (Figure 1-2), the main focus is on mid-body ice belt area.

Principle particulars are given in below table (source-provided by supervisor):

<table>
<thead>
<tr>
<th>Table 3: Principle particulars of the FPSO</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ship length O.A.</td>
</tr>
<tr>
<td>Length LBP</td>
</tr>
<tr>
<td>Breadth</td>
</tr>
<tr>
<td>Depth</td>
</tr>
<tr>
<td>Block coefficient(assumed)</td>
</tr>
<tr>
<td>Displacement</td>
</tr>
<tr>
<td>Frame Spacing</td>
</tr>
</tbody>
</table>

Now this side structure contains (Figure 6-1) side plating, longitudinal frames, normal web frame, heavy web frame, heavy stringers and stiffeners attached to web and stringer. The dimensions and material properties are given below:
Table 4: Side Structure Dimension details

<table>
<thead>
<tr>
<th>Component</th>
<th>Dimension/Thickness(mm)</th>
<th>Material Property(Yield)(MPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Side plate</td>
<td>23</td>
<td>315</td>
</tr>
<tr>
<td>Side Longitudinal</td>
<td>250x12+75x12</td>
<td>315</td>
</tr>
<tr>
<td>Ordinary web</td>
<td>850x15</td>
<td>250</td>
</tr>
<tr>
<td>Ordinary web stiffener</td>
<td>200x15</td>
<td>250</td>
</tr>
<tr>
<td>Stringer web</td>
<td>2200x14(1),13(2)</td>
<td>315</td>
</tr>
<tr>
<td>Stringer web</td>
<td>2200x13</td>
<td>315</td>
</tr>
<tr>
<td>Stiffener-Web</td>
<td>150x12</td>
<td>250</td>
</tr>
<tr>
<td>Stiffener-stringer</td>
<td>200x12</td>
<td>250</td>
</tr>
</tbody>
</table>

We don't know the exact polar class of this FPSO. So that as in IACS, all the calculations will be done for seven polar classes which include the calculation of ice load, framing requirements (Table 5). Using equation 1-15 to 1-18

Table 5: IACS calculated values for 186.12 KT displacements FPSO

<table>
<thead>
<tr>
<th>Polar class</th>
<th>Avg. Pressure(MPa)</th>
<th>Load Patch dimension</th>
<th>Plate thickness required (mm)</th>
<th>Min. Shear area required (cm²)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>b(mm)</td>
<td>w(mm)</td>
<td></td>
</tr>
<tr>
<td>PC1</td>
<td>18.62816</td>
<td>1.641016</td>
<td>5.907657</td>
<td>72.22067</td>
</tr>
<tr>
<td>PC2</td>
<td>12.42501</td>
<td>1.502393</td>
<td>5.408614</td>
<td>57.96707</td>
</tr>
<tr>
<td>PC3</td>
<td>8.527931</td>
<td>1.419833</td>
<td>5.1114</td>
<td>45.3787</td>
</tr>
<tr>
<td>PC4</td>
<td>6.868485</td>
<td>1.358058</td>
<td>4.889009</td>
<td>40.24341</td>
</tr>
<tr>
<td>PC5</td>
<td>5.326514</td>
<td>1.248378</td>
<td>4.49416</td>
<td>34.46314</td>
</tr>
<tr>
<td>PC6</td>
<td>3.963362</td>
<td>1.235606</td>
<td>4.448182</td>
<td>27.9617</td>
</tr>
<tr>
<td>PC7</td>
<td>3.301475</td>
<td>1.135341</td>
<td>4.087227</td>
<td>25.81568</td>
</tr>
</tbody>
</table>

Existing side plate thickness of this FPSO is 23mm. So it doesn’t match with even the lightest polar class of IACS. So, it will be checked later that it can carry the load of 3.3 MPa which is the lowest load calculated for this displacement or not.
• Shear area calculation

The longitudinal used in this FPSO are originally bulb profile. Then for simple dimension it’s converted to L profile of dimension given in Table 4. Dimension conversion is based on ‘RukkiProfiler’ standard shipbuilding profiles [14].

Actual shear area of the longitudinal frame is calculated for the web section of the frame considering corrosion factor of 2mm. So the shear area is 250 x (12-10)/100 = 25cm².

As a requirement of IACS, this shear area has to be greater than the shear area shown in Table 5. But it the actual shear area is approximately half of the required if we consider even the lightest polar class.

• Framing-structural stability

As stated in the IACS req. 2011, to avoid local buckling in the web frame, the web frame dimension has to satisfy the following limit values,

For flat bar,
\[
\frac{h_w}{t_{wn}} \leq \frac{282}{\sigma_y^{0.5}}
\]  
(4-1)

For bulb, tee and angle sections,
\[
\frac{h_w}{t_{wn}} \leq \frac{805}{\sigma_y^{0.5}}
\]  
(4-2)

Minimum net web thickness, \( t_{wn} = 2.63 \times 10^{-3} \cdot c_1 \sqrt{\sigma_y / (5.34 + 4(c_1/c_2)^3) } \)  
(4-3)

Where,
\( h_w \) = web height  
\( t_{wn} \) = net web thickness  
\( \sigma_y \) = minimum upper yield stress of the material [N/mm²]
\[ c_1 = hw - 0.8 \cdot h \ [\text{mm}] \]

hw = web height of stringer / web frame [mm]

h = height of framing member penetrating the member under consideration (Figure 4-1)

\[ c_2 = \text{spacing between supporting structure oriented perpendicular to the member under consideration} \ [\text{mm}] \) (see Figure 4-1)

Figure 4-1: Parameter Definition for Web Stiffening [1]

By applying these formulas, it is calculated that the net web thickness requirement is 39mm. Web height to thickness ratio also doesn’t satisfy the limit equation for flat bar.

So we will get local buckling on web frame. This will be analyzed later on Abaqus analysis.
5. Non-linear finite element analysis of a single frame

IACS requirements are based on single frame loading. So, single frame analysis should be so precise so that it can represent the entire grillage structure properly. Here a longitudinal frame is intended to analyze analytically and numerically. Within a full span (4.43m) longitudinal, ends are supported with transverse heavy web frame and in middle there is an ordinary web frame (Figure 5-1). Before starting the analysis, it was a question that should we take the full span or half span of 2.23m. If we take, the half span then it would be same as Daley’s asymmetric load case (loading description, see chapter 5.5, Figure 5-9). But there is problem with support, because the strength of web frame and ordinary web frame is not equal. Then it was decided to take full span and keep the ordinary frame at middle. So this formation is representing symmetric loading condition. So the analytical model and loading configuration will be based on symmetric loading condition as Daley. From the large part a single longitudinal has been chosen from the ice loaded area as shown figure below:

Figure 5-1: Single Frame selection

This longitudinal frame is in mid-body ice belt area (Figure 1-2). Abaqus analysis and analytical formulation procedure are as follows:
5.1. Non-Linear Finite Element Analysis

In linear analysis the displacement is assumed to be small and the material behavior is elastic and linear i.e. follow hooks law. But for realistic analysis and the case like accidental or overloading, non-linearity of geometry and material should consider. A non-linear analysis permits large deformation and consider plastic behavior of material. Then the load-displacement relation differs from linear hooks law stress-strain relation. Non-linear behavior of a typical structure is shown below,

![Figure 5-2: Non-linear behavior of a thin plate/shell [15]](image)

For the analysis of ultimate strength or collapse non-linear analysis has to be implemented as it allows large deformation.

Finite element analysis is based 3 principles,

- Equilibrium
- Kinematic compatibility
- Stress-strain relationship

When a structure is allowed for large deformation, unstable behavior of load-displacement curve is frequently observed.
There are many ways to solve this kind of behavior such as arc-length technique. In Abaqus modified Riks method is used to solve such case.

5.2. Finite element model

J. Abraham in his master thesis [17] found that, solid element give higher capacity than shell element so taking shell element will be a conservative selection. Getting idea from this, shell element has been used in my thesis. Abaqus documentation [16] also recommends to use shell element when thickness of the plate, members is significantly lesser than the other dimensions; less than 1/10. Other dimension refers a typical global structural dimension not the element dimensions. Global dimensions are like distance between supports, stiffeners, radius of curvature etc. In Abaqus, it is assumed that the plane perpendicular to the shell mid-surface remain perpendicular after displacement.

5.3. Material Property

Nonlinear model is considered for the structure. The non-linearity is utilized by using the hooks law up to yield stress and then plasticity which permit large deformations. Allowing larger deformations and applying plasticity indicate non-linearity of geometry and material. The following materials property has been taken into account. To relate with IACS rules, in analysis two pure plastic material property has been applied as shown in Figure 5-4 with the standard
Non-linear finite element analysis of a single frame

steel property; Young Modulus=210,000 MPa and Poison’s ration=0.3

![Stress-Strain Curve](image)

Figure 5-4: Elastic-Purly plastic material behavior

5.4. Boundary Condition

A single longitudinal frame is considered, supported with heavy web frame at the end and one ordinary web frame at the middle (Figure 5-1). The end of the longitudinal is assumed to be welded at the web frame. Before applying the boundary conditions the following facts will be considered:

- Adjacent structure
- Symmetricity
- Supporting structure strength
- Possible translation and rotation ability

Firstly, it was tried to use the following structure to analyze,
It is easy to think, to assume the longitudinal end fixed as having the heavy web support. But it was difficult to set what should be the boundary condition at ordinary web position. This cannot be neither fixed as it is not same strong as the web frame nor free in $y$-direction. If at ordinary web frame position $U_y$ is free, then this frame will not have any effect as the load direction is towards positive $y$-direction (see Appendix, Figure A-4).

Then, it would be a solution to take the full ordinary web length between Longitudinal Stringer as following image.
As the A: A end is supported by heavy web frame and B: B end is by stringer end; this ends has been kept fixed. The plate is the short part of whole side plating. In the transverse direction (x-direction) both long edge is symmetric. So in x-direction the shell plate has to be restricted to deform due to keep the adjacent plating effect. So this plate edges (red highlighted two edges in Figure 5-7) has been given symmetric boundary condition. $U_x=U_Ry=U_Rz=0$.

![Figure 5-7: Boundary Condition for single Longitudinal Frame](image)

For setting the final boundary condition, the deformation nature in whole grillage part had been observed. From the figure below, longitudinal end (red circled) has been kept fixed analytically, but actually we get deformation in whole grillage analysis.
5.5. Load

This longitudinal frame is intended to analyze according to IACS PC7 loading configuration. The ice load and the ice load patch dimension are for PC7 as presented in Table 5. Applied pressure 3.3 MPa, Load patch width is 4.08m and the height is 1.13m. So the load is applied over the frame spacing (600mm).

Figure 5-8: Displacement pattern in whole grillage part at 1.5MPa load

Figure 5-9: Loading of Single longitudinal frame.
5.6. Analytical Formulas

To form a simplified collapse mechanism I have tried different mechanism model. The different models are discussed below:

- **1st Model:**

First of all the mechanism is just assumed as the normal 3 hinge model as derived in chapter 1.7.6 that maximum deformation occur at middle for symmetric center load. The addition with that model (Figure 1-19) is a normal web frame has been added of length 1.5L. (Longitudinal length, L=4.43m and span length between stringer 6.6m=1.5L). Pure bending hinge is assumed where \( M_L \) for longitudinal and \( M_W \) for Ordinary web frame. Shear reduction is not considered.

\[
W_e = \int_{-w/2}^{w/2} P.s.w(x)dx
\]

External work,

\[
= P.w.s.\delta \left( 1 - \frac{b}{2L} \right) \quad (5-1)
\]
Non-linear finite element analysis of a single frame

Internal work,

\[ W_i = (4M_L + 2.68M_w) \frac{2\delta}{L} \]  \hspace{1cm} (5-2)

Equating 5-1, 5-2 we get the capacity,

\[ P_i = \frac{8M_L + 5.37M_w}{LwS\left(1 - \frac{w}{2L}\right)} \]  \hspace{1cm} (5-3)

- 2\textsuperscript{nd} Collapse Model

![Diagram showing 2\textsuperscript{nd} Collapse Mechanism for single longitudinal frame]

Figure 5-11: 2\textsuperscript{nd} Collapse Mechanism for single longitudinal frame

Then after having an observation from the deformation pattern from the whole grillage (Figure 5-8), it is seen that the maximum deformation is not occurring at mid-point. Maximum deformation is in between the fixed support and the ordinary frame. The position of hinge A (Figure 5-11) is assumed that the maximum deformation happens at the end of the load. So then applying energy principle,
Non-linear finite element analysis of a single frame

External work:

\[ W_e = 2Ps \left[ \int_{0}^{b/2} w_{OA}(x)dx + \int_{b/2}^{L/2} w_{AB}(x)dx \right] \] (5-4)

\[ w_{OA} = \delta \left( \frac{L}{L+w} + \frac{2x}{w} \left( 1 - \frac{L}{L+w} \right) \right) \] (5-5)

\[ w_{AB} = \delta \left( 1 + \frac{2x-w}{w-2L} \right) \] (5-6)

So, external work

\[ W_e = \delta \frac{Ps}{L+w} \left( wL + \frac{w^2}{2} + \frac{(L-w)^2}{2(w-2L)} \right) \] (5-7)

Taking \( L=4.43m, w=4.08 \), and length of web=6.6m we get the angles as shown in Figure 5-11, External Work is,

\[ W_e = M_L (2 \times 1.34\theta + 2 \times 2.34\theta) + M_w (4 \times 0.67\theta) \]

\[ = (7.36M_L + 2.68M_w) - \delta L \frac{2}{L+w} \] (5-8)

So the capacity using an ordinary web frame at mid-point of the longitudinal frame be,

\[ P = \frac{2(7.36M_L + 2.68M_w)}{\delta L \left( \frac{b^2}{2} + \frac{(L-w)^2}{2(w-2L)} \right)} \] (5-9)
5.7. Analytical Results

Now, the capacity of the longitudinal will be calculated for different cases which were derived earlier.

**Case 1:** without any support at middle i.e. without taking consideration the ordinary web frame,

1a: All the hinges are pure bending hinge that mean no reduction due to shear as equation

\[
P = \frac{8M_p}{Lb_s\left(1 - \frac{b}{2L}\right)}
\]

(1-35) capacity is 0.323 MPa

1b: Considering shear reduction as Daley derived, equation (40) capacity is 0.27 MPa.

**Case 2:** With the ordinary frame at middle,

2a: As 1st collapse mechanism, equation

\[
P = \frac{8M_L + 5.37M_w}{LwS\left(1 - \frac{w}{2L}\right)}
\]

(5-3), capacity is 2.15 MPa.

2b: As 2nd collapse mechanism, equation

\[
P = \frac{2\left(7.36M_L + 2.68M_w\right)}{wL + \frac{b^2}{2} + \frac{(L - w)^2}{2(L - 2L)}}
\]

(5-9), it is 2.13 MPa.

So I have taken the minimum capacity 2.13 as collapse mechanism principle.

5.8. Abaqus Results

A single longitudinal frame without having any support in middle (case 1, chapter 5.7) span of 4.43m, loading with 4.08m ice load patch, analysis has been done to check the Daley’s 3-hinge collapse mechanism derivation as equation (1-40)
Non-linear finite element analysis of a single frame

So it is observed that Daley’s 3-hinge capacity of 0.27MPa allowing deformation of 19mm. The limit load according to this plot will be estimated by twice elastic slope method later.

Figure 5-12: Pressure vs. Deformation plot single longitudinal with span of 4.43m (case1)

Figure 5-13: Pressure vs. Deformation plot for individual longitudinal at centre.

The above plot is for the mid-point (Figure 5-14, location D) of the longitudinal. Up to 1.1 MPa (point A) it shows elastic behavior with a deflection of 12 m. From the above plot we can see this longitudinal has the
Non-linear finite element analysis of a single frame

capacity of 1.4 MPa (Point B in Figure 5-13) allowing deformation of 50mm at mid-point of the longitudinal. But from Figure 5-14, the maximum deflection of 81mm is occurring at location E. So it can be said that the 2\textsuperscript{nd} collapse mechanism can't present the actual collapse nature. The collapse load founded using 2\textsuperscript{nd} model is 2.13MPa, which is so much to allow.

![Figure 5-14: Deformation of longitudinal at 1.4 MPa load](image)

But normally it is expected that the analytical value should be higher than real value. Because for analytical calculation it was assumed that all hinges are pure bending moment hinge but at the longitudinal end moment will be reduced due to shear created, has been shown in Figure 5-15 and the capacity will be lower. So the assumption behind the analytical model formed and the position of hinge should be modified. Deformation contour plot for different load will be found at Appendix.

![Figure 5-15: Shear Stress in 1.4MPa.](image)
6. Analysis of a large part of the ship side

The large part has been taken the large part is modeled by considering a grillage of 1/2-1-1/2 span (Figure 6-1) in both longitudinal and transverse direction. The half span in both directions has been taken so that we can get a better effect from adjacent structure.

![Side Structure Abaqus model](image)

Figure 6-1: Side Structure Abaqus model

The letters A, B, C, D indicated in above figure will be used in further work to denote different location in structure.
6.1. Boundary conditions

Selecting boundary condition for this large part is a difficult issue which will represent that structure has a well connection with adjacent structure. Before applying boundary condition it is necessary to know the hierarchy of load transfer. The load transfer from ice load to this regarding large side part is shown below:

![Load transfer hierarchy diagram]

Another factor to consider is the strength of adjacent structure. For this case stringers and transverse web frames are the heaviest part compared to other members.

Two alternative boundary conditions have been applied to the end of web and stringers.

- **BC 1:** All the stringers and web ends are fixed
- **BC 2:** All the stringers end fixed. Main web and ordinary web ends are symmetric; $U_y=U_{Rx}=U_{Rz}=0$

For both alternative, same boundary condition have been applied for the plate edges, (see Figure 6-1)

- For longitudinal($x$-direction) edge: $U_y=U_{Rx}=U_{Rz}=0$
- For transverse($y$-direction) edge: $U_x=U_{Ry}=U_{Rz}=0$
Boundary condition is shown simply below for longitudinal direction plate edge:

![Diagram](image)

**Figure 6-3: Boundary condition for plate edge in longitudinal direction**

Symmetric boundary condition creates the support given by adjacent structure. From the figure above, adjacent plating in y-direction will restrict to deform this plate edge. So in that direction displacement (Uy) has been kept zero. The adjacent plate will also restrict this edge to rotate about x-axis (URx) and z-axis (URz).

### 6.2. Loading

As stated before, this model is intended to assess under IACS polar class 7, the load and the load patch dimensions are applied as calculated in Table 5.

<table>
<thead>
<tr>
<th>Ice Load(MPa)</th>
<th>Patch height(m)</th>
<th>Patch width(m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PC7</td>
<td>3.301475</td>
<td>1.135341</td>
</tr>
</tbody>
</table>
The load patch height has covered two longitudinals. The load is applied symmetrically in both directions. The load is applied to positive z-direction.

### 6.3. Meshing Technique

This part is meshed with Abaqus predefined automatic mesh technique where I’ve set the average mesh size and element type as shell quad element. Abaqus did the rest of the meshing work automatic. That’s why there was no control on meshing specially for critical location and therefore very coarse and un-uniform mesh has been found for this structure (see Figure 6-5, Figure 6-6). The loading area is also not uniformly meshed.
6.4. Abaqus analysis result

The whole grillage part has been analyzed with many alternatives like, different boundary condition (BC1 and BC2, stated in chapter 6.1), different plastic property of the material.

6.4.1. Comparing boundary condition

The whole large part has been analyzed for two boundary conditions as described in chapter 6.1. Abaqus result is shown below:
Analysis of a large part of the ship side

![Graph showing deformation difference between two boundary conditions](image)

Figure 6-7: Deformation difference between two boundary conditions

[Plot legend meaning: WholePP_D_BC1: whole grillage, perfectly plastic material with boundary condition 1, point location 'D' (see Figure 6-1)]

This plot has been drawn for position 'D' for both boundary conditions. From the above plot, two curves are showing so close nature. That means during calculation of a large part; when pressure is local, far from the applied boundary condition; these two different boundary conditions don’t have so much effect in deformation. For the other locations, we can see the deformation and stress contour plot in Appendix (Figure A-6, Figure A-7) which are showing so close nature for both in all position.

### 6.4.2. Material comparison

Two assumptions regarding plastic property was considered.

1. Elastic pure plastic material
2. Elastic plasticity with 15% hardening.

Both of the material show approximately same behavior up to 100mm deformation (Figure 6-8). This analysis was done considering boundary condition BC1. For further results, pure plastic material model has been used as this is an assumption for deriving the IACS requirements.
Analysis of a large part of the ship side

6.4.3. Result of whole structure at different positions

Figure 6-8: Plasticity effect on Abaqus result

Figure 6-9: Load-deformation plot of whole grillage, at many points
Figure 6-10: Deformation contour plot in 1.7MPa load (showing points for plots in Figure 6-9)

**A**: this is the intersection point of heavy web and plate. Here structure is showing better capacity of 2.1 MPa, than other points within loaded area with a deformation of 25mm. buckling behavior is found in this position and allowing large deformation with post-buckling.

**D**: this point is the middle point of loading located at plate and ordinary web intersection. The capacity is considered 1.6 MPa giving deformation of 50mm. It is showing large deformation at a small increase of the load. After reaching at 100mm deflection it shows buckling behavior. Behavior of the point B, E are almost same.

**C**: this is point located at the web where buckling is occurring. At 2MPa load it starts to buckle. From the curve, it allows large deformation at this load.
From different position analysis it is observed that, as we go far from the load area, we are getting more capacity and at the edge positions the deformations are almost zero though the edges were not fixed. So for design load patch we get much local deformation. See appendix for the deformation plots.

6.4.4. Comparison between whole structure and single longitudinal results

Now, we will compare the results between the longitudinal analyzed individually and longitudinal with whole structure.

![Load-Deformation plot for longitudinal (single and in whole structure)](image)

Figure 6-11: Load-Deformation plot for longitudinal (single and in whole structure)

The longitudinal frame is showing higher capacity when it is analyzed in whole grillage model than the capacity when it was analyzed individually. But the longitudinal give higher deformation for whole condition. In whole structure, longitudinal is still showing less capacity than analytically calculated plastic capacity.

- The deformation in whole structure is higher due to line load; Q is double in whole structure analysis as applied pressure is same as individual frame analysis but loaded area is double.
- This larger deformation might be happening for local pressure effect. The loading in single frame analysis, the load was more uniform through the most of the area of the plate (Figure 5-9).
6.4.5. **Introducing additional stiffeners**

It is observed that a huge buckling occur at the lower portion of the main web frame which gives the whole part less capacity. Then if we introduce additional stiffeners to the main web of dimension 150x12 at spacing of 600mm then the improvement of capacity of the web increase so much. Before applying the additional stiffener, the web deformation increased infinitely without increasing the load (see figure below).

The capacity at the midpoint (position ‘D’) does not increase much. It is due to the additional stiffener can’t carry the local load at plating and the load transfer through plate, longitudinal to main web frame has not improved by adding the stiffener. So we are getting the same deformation nature at the mid-point of loading. May be capacity can improve by increasing plate thickness.

![Figure 6-12: Load-Deformation plot for modified grillage](image)

6.5. **Assessing limit loads**

There are many ways to estimate limit state or capacity. 3-hinge capacity is one of the limit states. If we consider the ideal case, deformation increment will be infinite in 3-hinge capacity load. This ideal case can be obtained by using
Analysis of a large part of the ship side

elastic-purely plastic plot but in real strain hardening and membrane effect occur. So in real case it is confusing to determine the capacity or limit load. There are many ways to estimate the limit load like twice elastic slope method (TES), tangent intersection method (TI), 0.1% residual strain method etc.

6.5.1. Twice elastic slope method

In load-displacement curve the elastic part is linear. If this linear part slope is tanθ then another line is drawn with a slope of 2tanθ. This second line will cut the load deformation in a point and corresponding load is considered as the capacity. This method is used in ASME III [18] and described in the assessment of that code by D G Moffat [19]. But the capacity is often higher than estimated capacity by this method [20]. So using this method will be conservative one.

![Twice elastic slope method](image)

Figure 6-13: Twice elastic slope method [19]

6.5.2. Tangent Intersection Method

This method is the intersection point of elastic tangent and plastic tangent line in the load deformation curve and the corresponding load of that intersection point is considered as the capacity load. This method is recommended in the CEN TC54 draft standard [19]. The confusing fact of this method is to
determine the tangent in the plastic portion. If I see the curves obtained in this thesis work, it is not easy to determine the tangent of the plastic curve.

![Graph showing tangent intersection method](image)

**Figure 6-14: Tangent Intersection Method**

### 6.5.3. Limit Loads

So I’ve used the TES method to determine the limit load for the structure. Limit load for the basic 3-hinge collapse mechanism (Figure 1-19) is obtained as figure below is 0.29 MPa with a deformation of 21mm.

![Graph showing limit load for 3-hinge mechanism](image)

**Figure 6-15: Limit load for 3-hinge mechanism**
Using twice elastic method it is found that, for single longitudinal model the limit load is 1.3MPa and for whole grillage model at position ‘D’ limit load is 1.42 MPa. Now if we compare with the analytical value, obtained from the collapse mechanism in chapter 5.6, of plastic capacity 2.1 MPa; this value is higher than the value obtained value for both case. May be as stated earlier TES give lower value than actual even then it should not be higher than 2.1 MPa. Because for the analytical calculation, it was assumed the hinges were purely bending hinge but in real the moment is less due to shear effect and membrane effect. Also from the previous discussion, the 2nd collapse model doesn’t present the actual collapse model.

Now if we look at the design load for IACS PC7, it is 3.3MPa. The obtained capacities for the frames are so less than the minimum design loads for this size FPSO.
Analysis of a large part of the ship side

Figure 6-17: Limit loads for web with additional stiffener

So after introducing additional stiffener at web, the capacity has increased so much and it satisfies the PC7 design load and no buckling occur at web but at ordinary web frame buckling occurs.

Figure 6-18: Deformation plot of modified grillage
7. Conclusions

IACS framing requirements are based on loading in a single frame and it should be modeled in such a way so that the results of single frame analysis match with the whole large part result within a considerable margin.

From the single frame analysis; for case 1a (see chapter 5.7), the analytical result gives 11% higher value and for case 1b, analytical gives only 6% lower value than simulation result. So considering only pure bending moment give overestimated capacity value but when considering shear and neglecting membrane effect give conservative value within an acceptable margin.

Case 2, simplified single longitudinal frame collapse model of regarding FPSO, gives 62% higher value than simulation limit load. This big difference is inconsiderable, so the assumption of not taking shear effect is not permissible to present a real model. This result has drawn a demand to make a modified model.

From Abaqus result, single frame analysis gives less capacity than whole grillage analysis. But for whole grillage initial displacement is higher than single frame analysis. It is may be due to local deformation. So in single frame analysis local deformation has to be treated may be by considering peak pressure factor (PPF).

Observing all the limit loads, it is clear that this whole part is not satisfying the design ice load of the lightest IACS Polar Class 7. Capacity, within the loaded area or close to loaded area, is maximum 2MPa which is much less than the IACS PC7 average ice patch load, 3.3 MPa. In addition, the minimum shear area requirement is double than the actual shear area of the longitudinal. The plate thickness is also less than the PC7 requirement. The structural stability requirements also don't go with the dimension of web and stringer. The capacity doesn't increase even after introducing additional stiffener at web frame except web frame. So it could be said that this FPSO doesn't comply with IACS PC7. But before giving a certain comment it should be mentioned that, this FPSO is under DNV class but other information i.e. exact DNV polar
class identification, is not investigated. Double hull, as shown in drawings (see appendix, Figure A-1), had also not been considered. So, further analysis by considering double hull or whole FPSO and a quantitative study of DNV polar class are necessary to make a certain comment regarding validity of this FPSO.
8. Recommendation for further work

- A deep comparative study of IACS UR with other classification society is suggested. Especially a brief study of DNV polar class could give this thesis work a better dimension.
- To understand the ice loading well it is recommended to work with energy models, including material models of ice. Then it can bring some arguments on IACS ice load calculation.
- Validity of IACS polar codes for a moored ship/FPSO is further to be assessed.
- Finding a compatible collapse mechanism model for the regarding single longitudinal combined with an ordinary web frame at middle, is the immediate demand to be matched with NLFEM results.

![Figure 8-1: Deformation of single longitudinal](image)

After having a good observation from the real deformation, the position of hinge ‘A’ showed in Figure 5-11 is not positioned correctly, observation for 2nd model was not correct. So another model could be proposed as follows in Figure 8-2. The location of hinge ‘A’ can be found by maximizing the external work with respect to distance ‘a’.
Assumption also has to be modified. The above model with taking the shear effect on bending can give a good analytical model for regarding FPSO.

- During FEM analysis cut-outs in the web frames were neglected. In addition, intersections of members were not well defined. Meshing of the model should be treated more precisely. So more details analysis is recommended.
- Introducing modified plate thickness, framing dimensions to this FPSO as IACS PC7 requirements and verifying the capacity with regarding design ice load can give a better review of IACS UR.
- This thesis work has motivated to analysis the full detailed FPSO.
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4. **Daley CG, Kendrick A.** *Derivation and use of formulations for framing design in the polar class unified requirements.* 2000.

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7. **Claude Daley, Kaj Riska.** *Conceptual Framework for an Ice Load Model.*


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A. Appendix

Matlab script

For finding the average pressure and design ice load patch dimensions:

```matlab
function []=IACS_requiremtns()

%%%%%%%%%%%%POLAR CLASS
CONSTANTS

CfC=[17.69; 9.89; 6.06; 4.5; 3.1; 2.4; 1.8];
Cff=[68.6; 46.8; 21.1; 13.4; 9.5; 4.06];
Cfd=[2.01; 1.75; 1.53; 1.42; 1.31; 1.17; 1.11];
Cfd=[250; 210; 180; 130; 70; 40; 22];
CfL=[7.46; 5.46; 4.17; 3.15; 2.5; 2.37; 1.81];
AF=[0.7; 0.65; 0.55; 0.55; 0.5; 0.45; 0.45];
corfact=[5; 5; 5; 4; 4; 3; 3];
PPF=1.5;

%%%%%%%%%%%%%GIVEN

D=[10; 30; 60; 90; 120; 150; 186.12; 200; 250];
n=9;
DF = zeros(7,1);
s=0.6;
l=4.43;
sigma=315;

CALCULATION

P=zeros(7,n);
t=zeros(7,n);
b=zeros(7,n);
w=zeros(7,n);

for j=1:n
    for i = 1:7
        if D(j)<=CFdis(i)
            DF(i) = D(j).^0.64;
        else
            DF(i) = CFdis(i).^0.64+0.1*(D(j)-CFdis(i));
        end
    end

F=0.36.*CFc.*DF;
Q=0.639.*F.^0.61.*CFd;
w(:,j)=F./Q;
b(:,j)=w(:,j)./3.6;
P(:,j)=F./(b(:,j).*w(:,j));
    for i=1:7
        if b(i)>=s
```

```
\[ t(i,j) = 500s \cdot (1/(1+s/(2*l))) \cdot \sqrt{(PPF \cdot AF(i) \cdot P(i,j))/315} + \text{corfact}(i); \]

\[ \text{else} \quad t(i,j) = 500s \cdot (2 \cdot b(i))/s - (b(i)/s)^2 \cdot 0.5 \cdot (1/(1+s/(2*l))) \cdot \sqrt{(PPF \cdot AF(i) \cdot P(i,j))/315} + \text{corfact}(i); \]

end

\% P(:,j)
\% t(:,j)
end
\% xlswrite('output.xlsx',P,1,'C3:K9')
\% xlswrite('output.xlsx',t,1,'C11:K17')
xlswrite('output.xlsx',w,1,'C61:K67')
xlswrite('output.xlsx',b,1,'C53:K59')
\% figure(1)
\% plot(D,P);
\% xlabel('Displacement(KT)')
\% ylabel('Pressure(MPa)')
\% legend('PC1','PC2','PC3','PC4','PC5','PC6','PC7',-1)
\% figure(2)
\% plot(D,t);
\% xlabel('Displacement(KT)')
\% ylabel('Thickness(mm)')
\% legend('PC1','PC2','PC3','PC4','PC5','PC6','PC7',1)
Appendix

Provided Drawings

Figure A-1: Drawing of Web frame

Figure A-2: Drawing of Ordinary web frame
Figure A-3: Modified grillage model
Appendix

Plots

Figure A-4: Displacement contour plot of longitudinal

Figure A-5: Deformation at 2.1MPa load
Figure A-6: Deformation contour plot for BC1 and BC2 at 2MPa load

Figure A-7: Stress contour plot for BC1 and BC2 in 2MPa load
### Calculations

Average pressure for different displacements

<table>
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<tr>
<th>Displacement</th>
<th>10</th>
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<th>60</th>
<th>90</th>
<th>120</th>
<th>150</th>
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<th>200</th>
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**Figure A-8: Deformation at 3.3MPa load**
Required Plate Thickness:

1. Span length=2.215m, frame spacing=600mm

<table>
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<th>Disp.</th>
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<th>90</th>
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2. Span length=2.21m, frame spacing=400mm

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3. Span length=4.43m, frame spacing=600mm

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